



Photoproduction of the $f_1(1285)$ Meson

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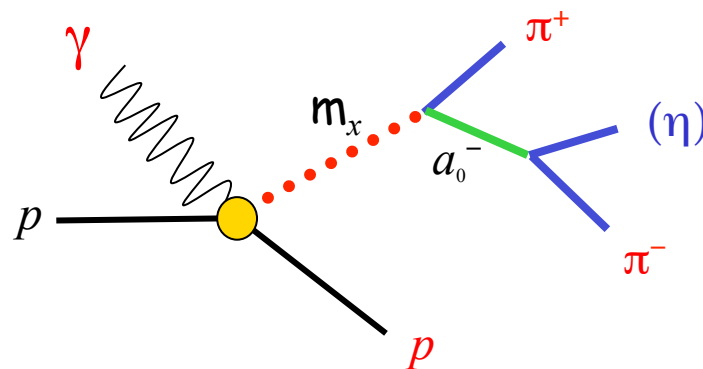
Ph.D. work of Ryan Dickson, completed 2011

[arXiv:1604.07425 \[nucl-ex\]](https://arxiv.org/abs/1604.07425), Accepted by Phys. Rev. C



Outline

- What are the $f_1(1285)$ and $\eta(1295)$ mesons?
- Identification of the state in CLAS/g11
- Results for:
 - Mass and Width
 - Differential cross sections - model comparisons
 - Branching ratios $\eta\pi\pi$, $\gamma\rho^0$, $K K \pi^-$
 - Dalitz plot analysis
 - spin and parity determination

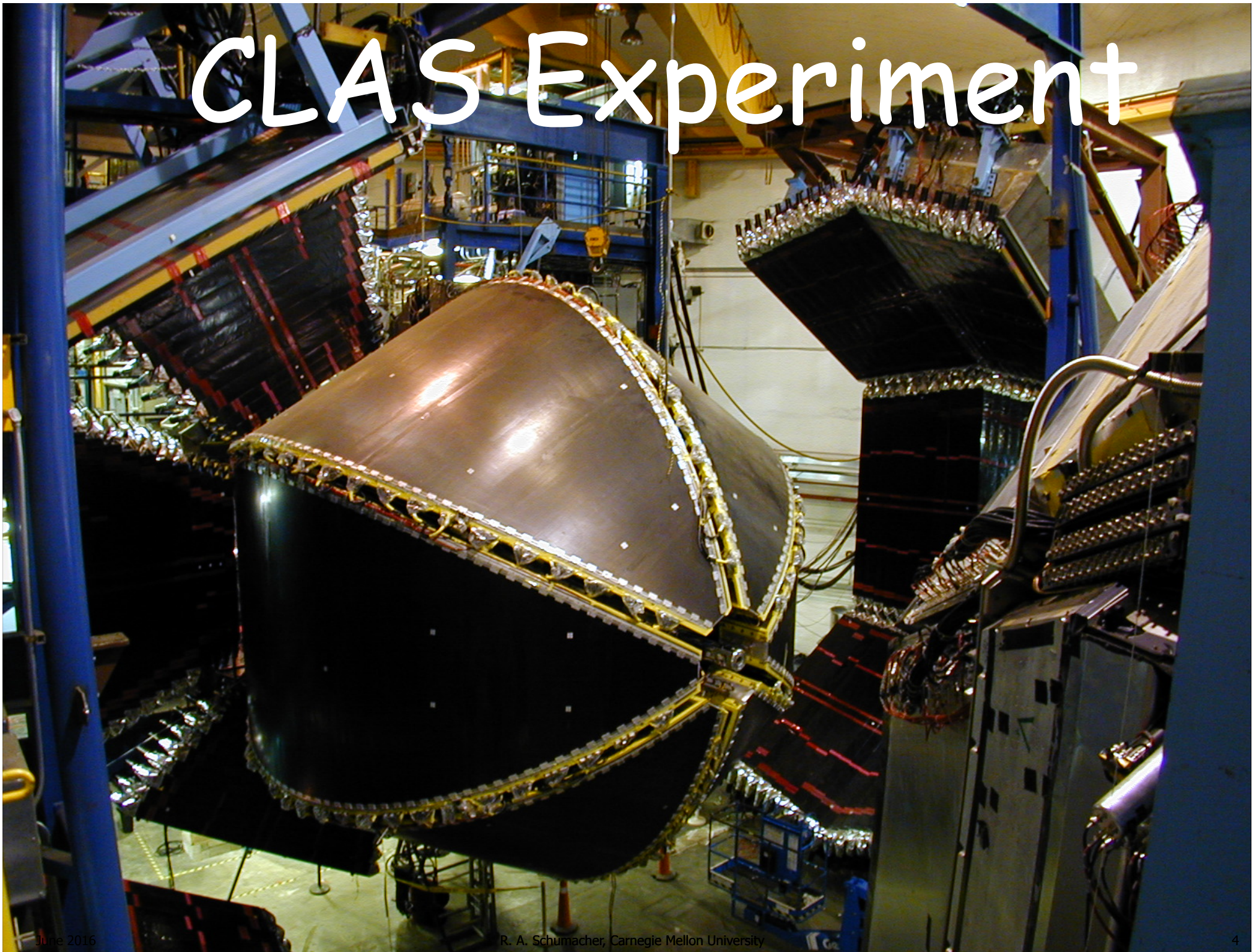




Two Players:

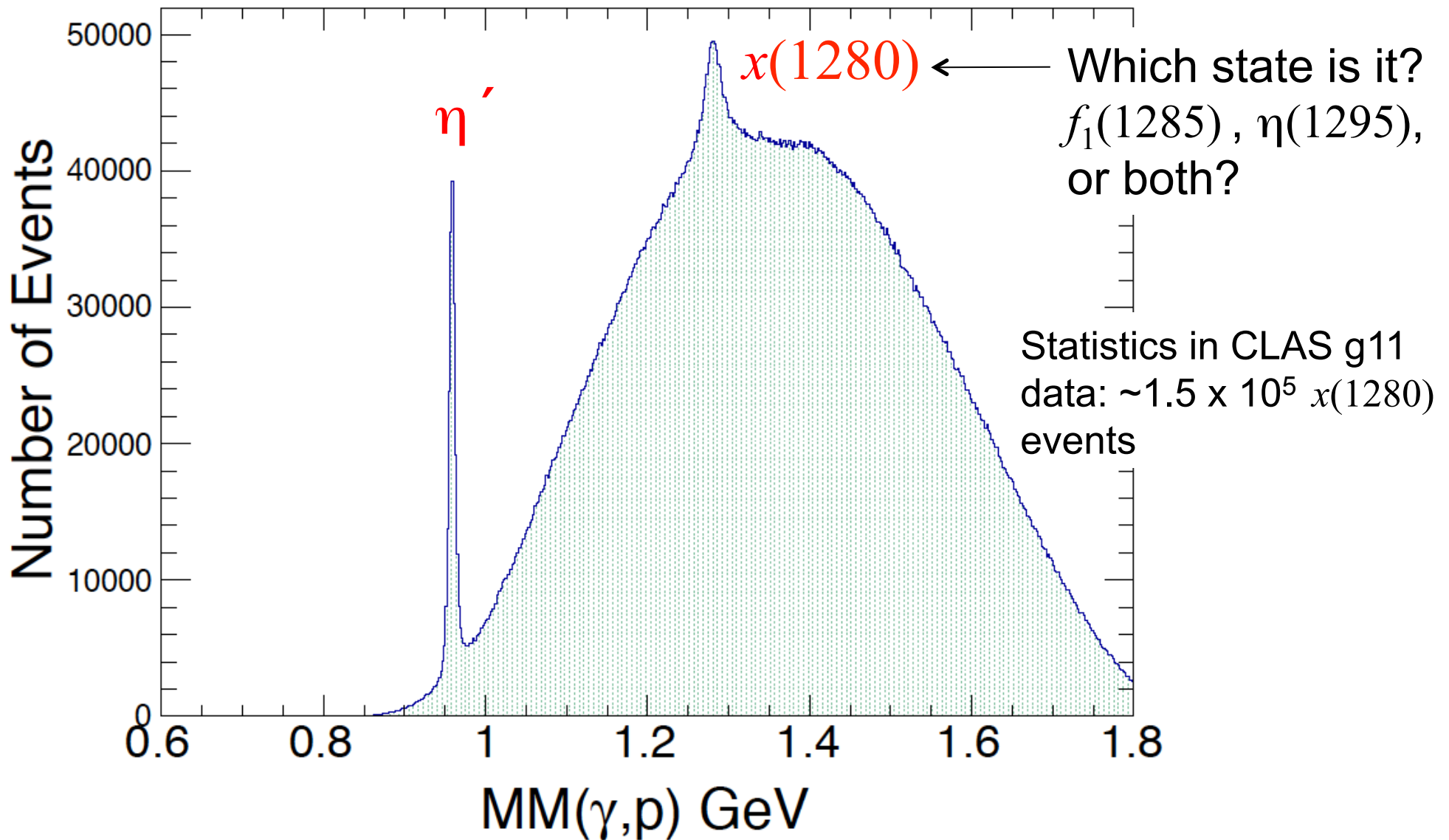
- $f_1(1285) \quad I^G(J^{PC}) = 0^+(1^{++})$
 - Well-established axial-vector meson seen in hadronic reactions;
 - Seen in experimental PWA analyses
 - Seen in Lattice QCD
 - Possible "dynamically generated" $K\bar{K}^* - \text{c.c.}$ state
- $\eta(1295) \quad I^G(J^{PC}) = 0^+(0^{-+})$
 - A "controversial" state seen in $\pi^- p \rightarrow \eta \pi^+ \pi^- n$
 - Seen only in PWA, e.g. J. Manak et al., E852/BNL
 - Important in the enumeration of mesonic states

CLAS Experiment



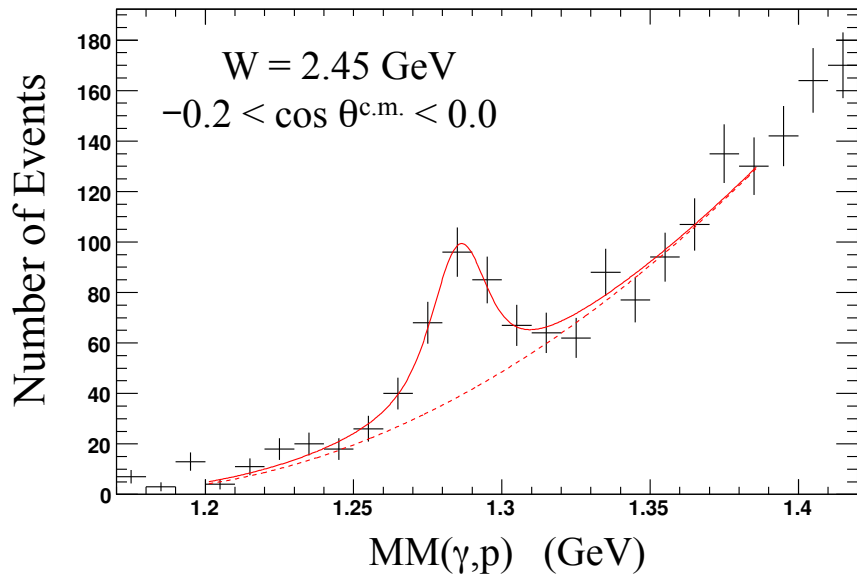
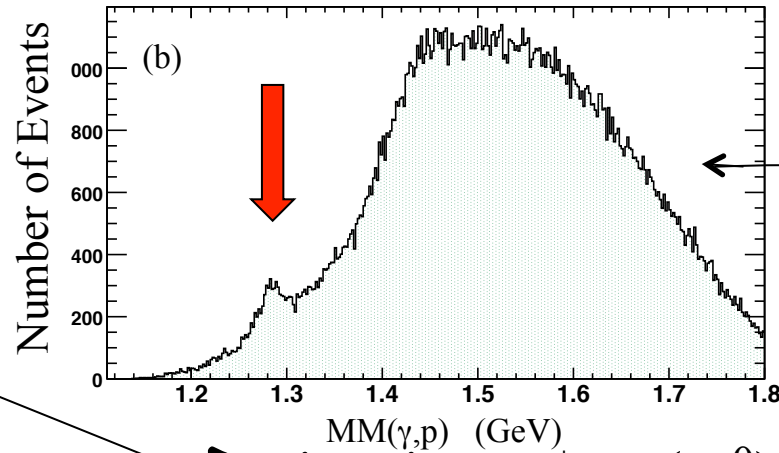
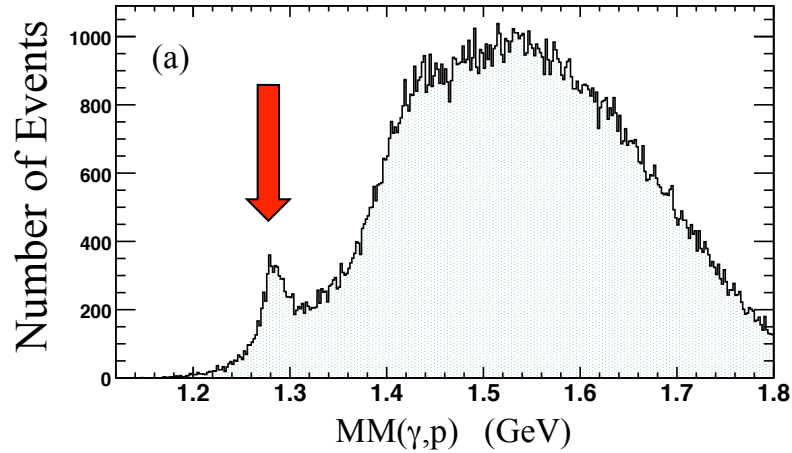


First Observation of $f_1(1285)$ or $\eta(1295)$ in $\gamma p \rightarrow p x \rightarrow p \pi^+ \pi^- (\eta)$

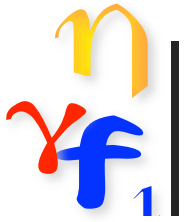




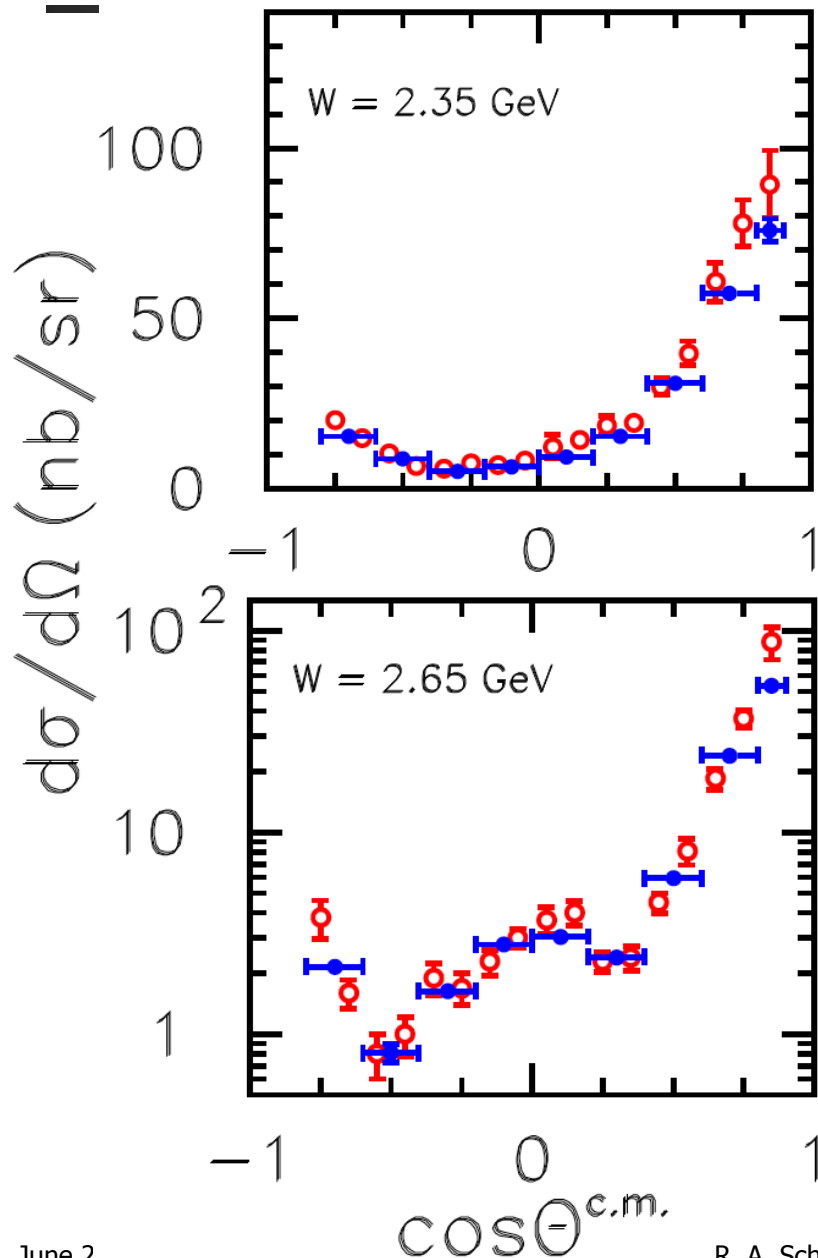
Two $x \rightarrow K K \pi$ decay modes



- Detect $p K^+ \pi^-$ (K^0)
 - (left)
- Detect $p K^- \pi^+$ (\bar{K}^0)
 - (right)
- Combine channels prior to yield extraction using Voigtian + polynomial



Cross-check η' cross section



- Compare two CLAS analyses of η' photoproduction
 - Same data set, using different methods
 - Red: Williams & Krahn *et al.**
 - Blue: Dickson *et al.* (this work)
 - Good agreement between independent analyses
- Use (small) differences to quantify systematic uncertainty

(Note log scale)

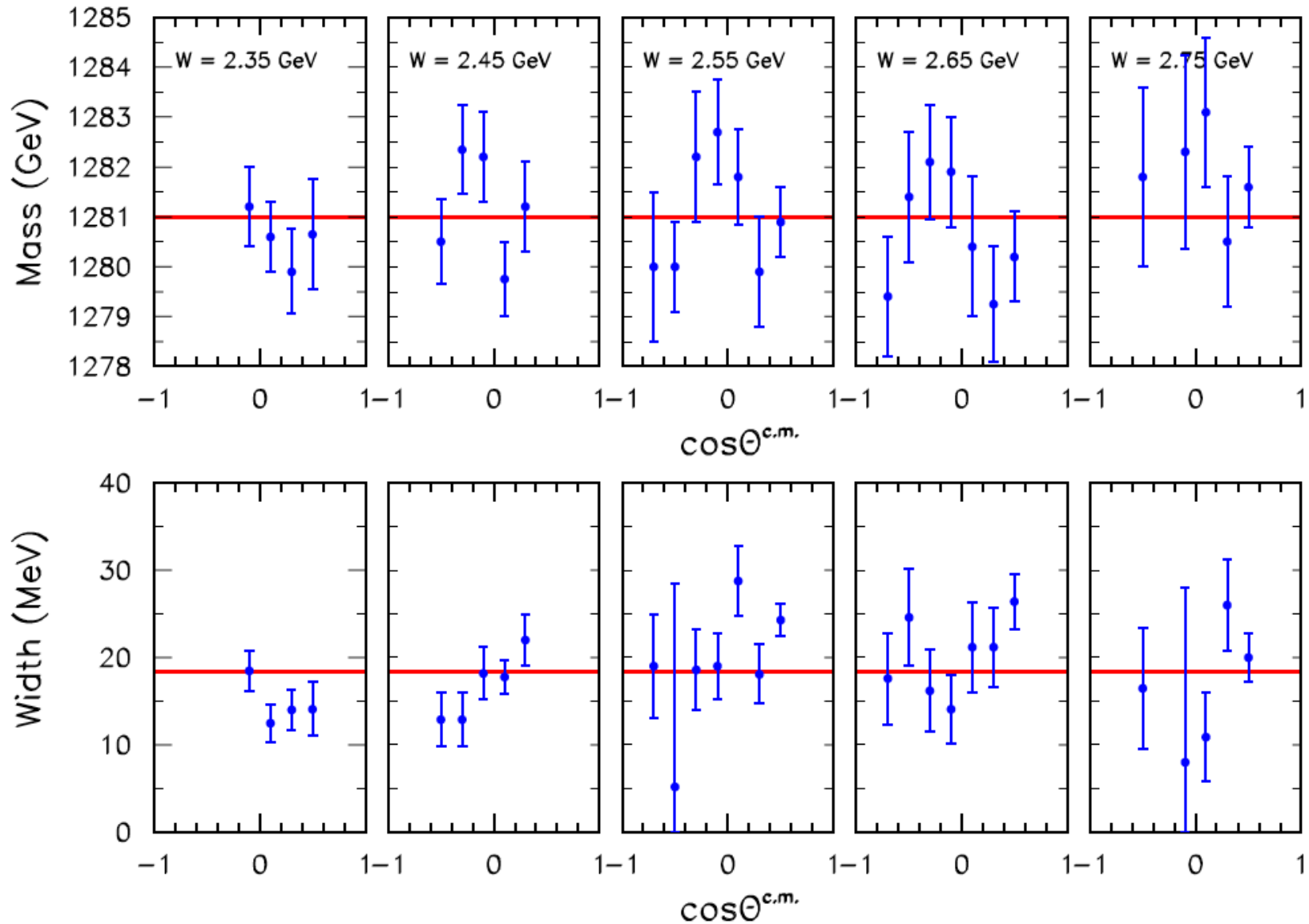


Results

arXiv:1604.07425 [nucl-ex], Accepted by Phys. Rev. C
R. Dickson et al., CLAS Collaboration



Mass & Width Measurement

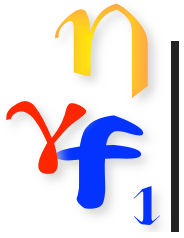




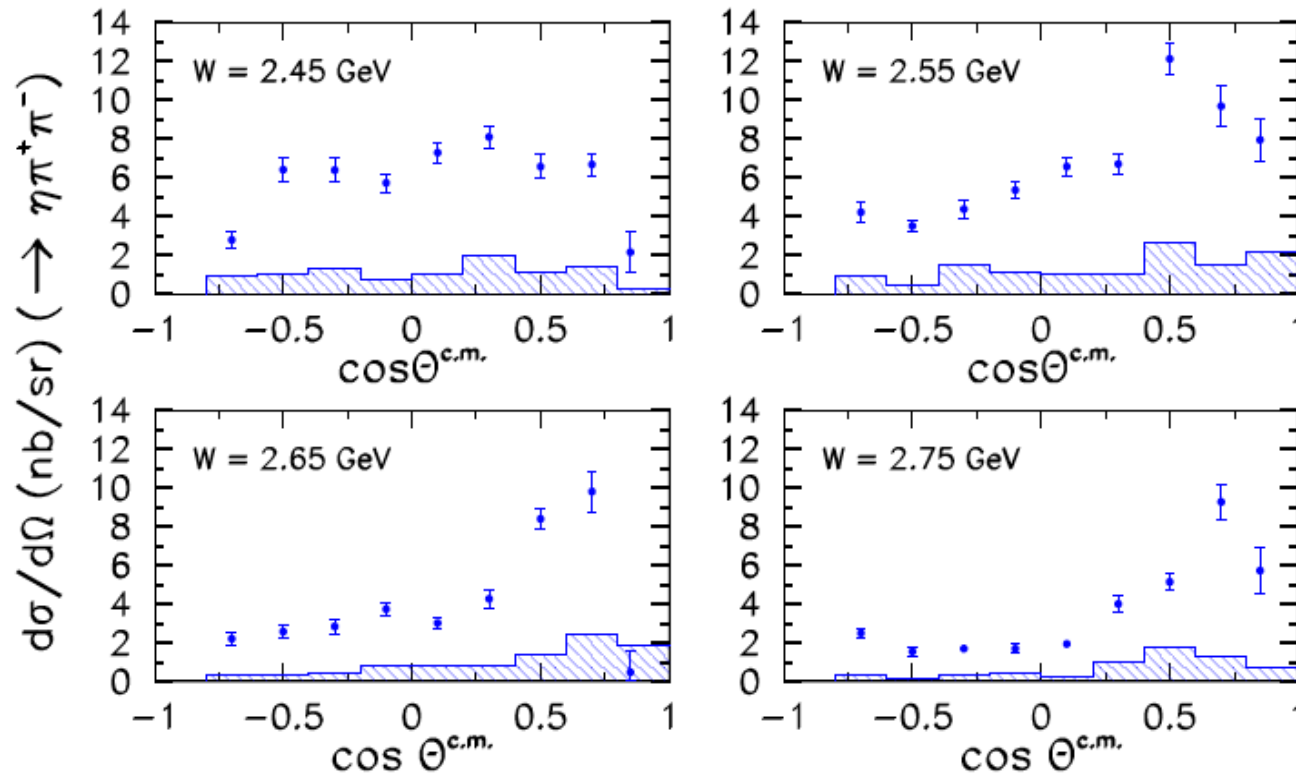
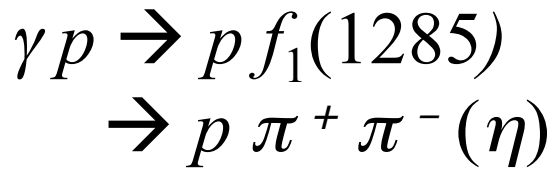
Mass & Width Measurement

Channel		Mass (MeV/c ²)	Width (MeV/c ²)
$\eta' \rightarrow \eta\pi^+\pi^-$	CLAS	958.48 ± 0.04	$\Gamma \ll \sigma_{exp}$
$x \rightarrow \eta\pi^+\pi^-$	CLAS	1281.0 ± 0.8	18.4 ± 1.4
η'	PDG	957.78 ± 0.06	0.198 ± 0.009
$f_1(1285)$	PDG	1281.9 ± 0.5	24.2 ± 1.1
$\eta(1295)$	PDG	1294 ± 4	55 ± 5

- Mass consistent with PDG value for $f_1(1285)$ not $\eta(1295)$
- Width is smaller than PDG by several σ



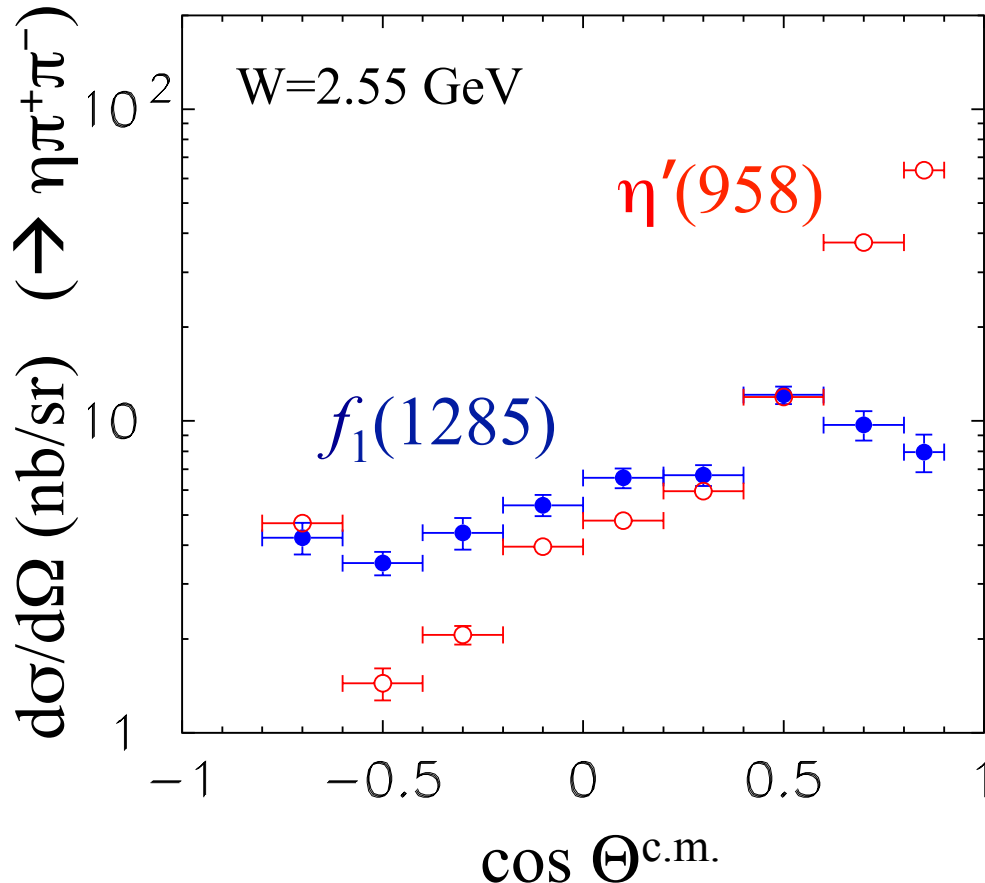
Cross Section vs. Angle and W



- Differential cross-sections
 - $\eta\pi^+\pi^-$ final state
 - total rate not measured
- Systematic uncertainty
- Very weak forward peaking seen
 - Cross section falls at very forward angles



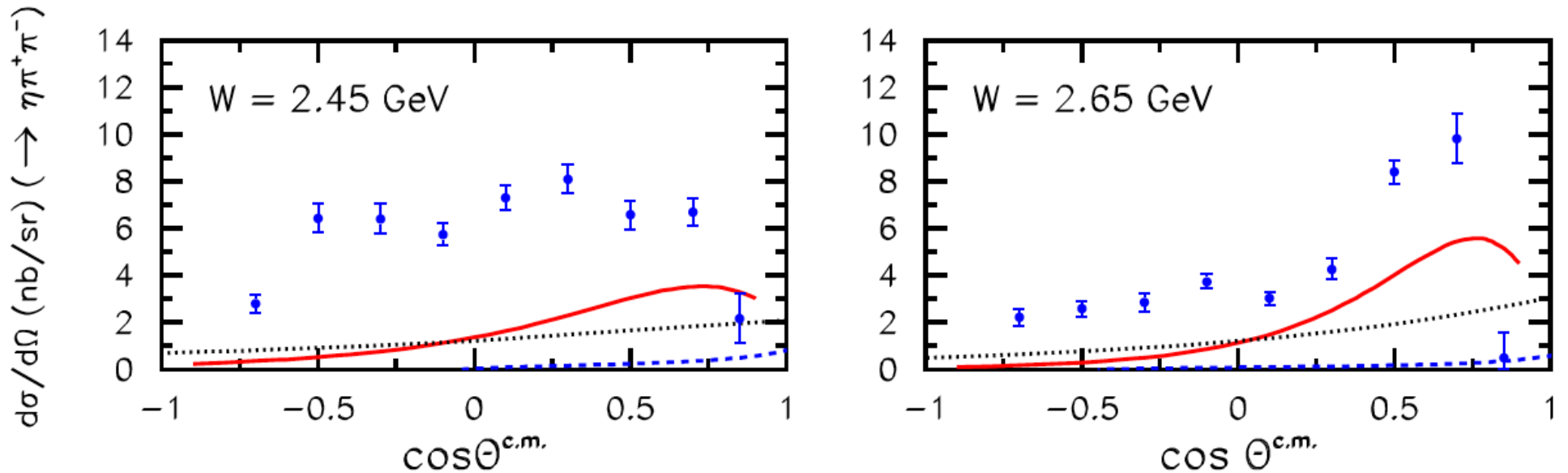
Compare Mesons: f_1 and $\eta'(958)$



- $f_1(1285)$ is produced "flatter" than the η'
- (Note logarithmic scale)
- Clue about production: not meson-exchange dominated like the η'



Comparison with Models

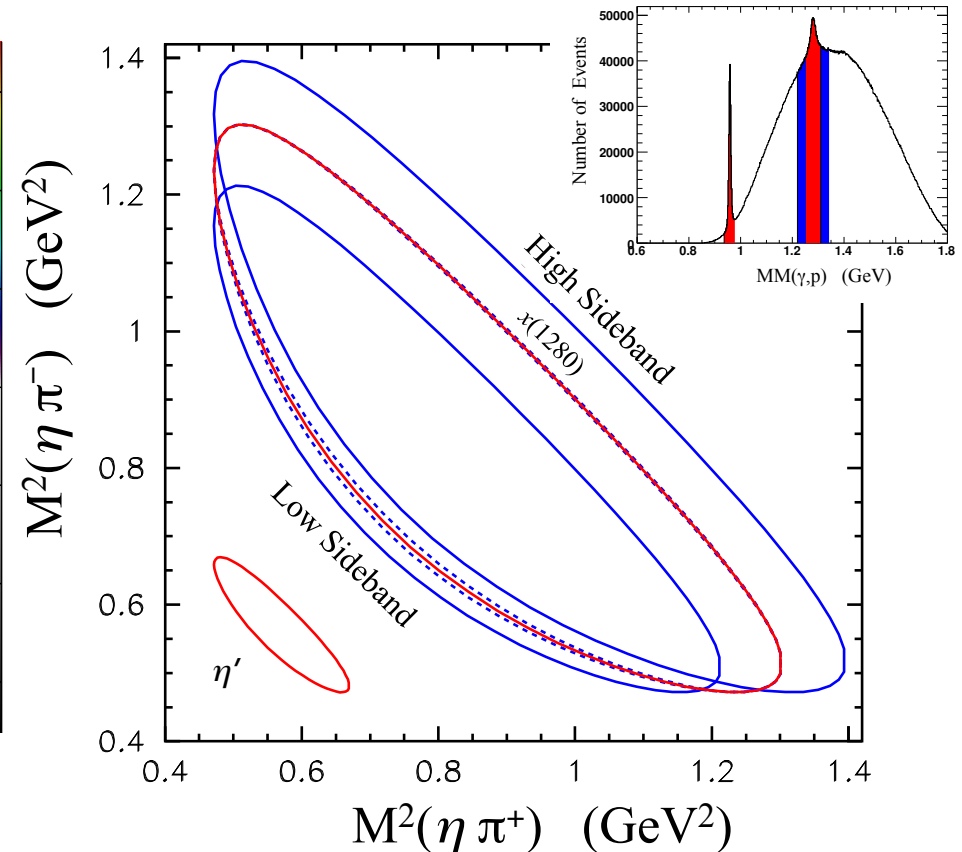
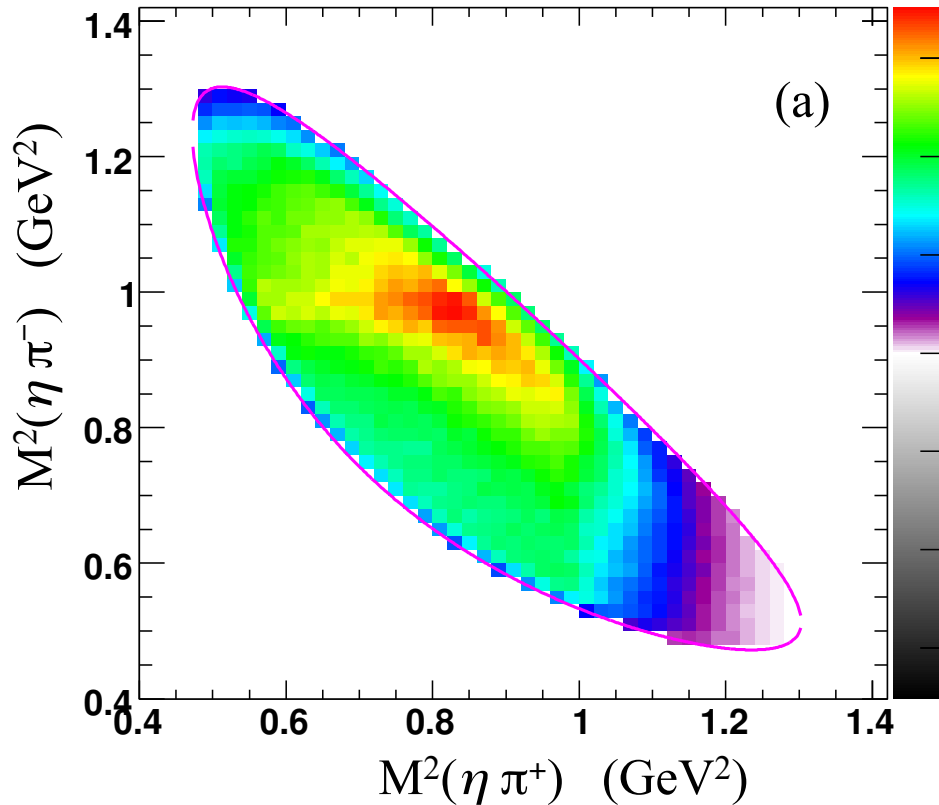


- Solid red: Effective Lagrangian with meson exchange
 - Kochelev *et al.*
- Dashed: Effective Lagrangian with meson exchange
 - Uncontrolled hadronic form factor cut-offs
 - J-J. Xie (unpublished, private comm.)
- Dotted: "Holographic QCD" model
 - S. Domokos: meson exchange with specific recipe to compute couplings



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

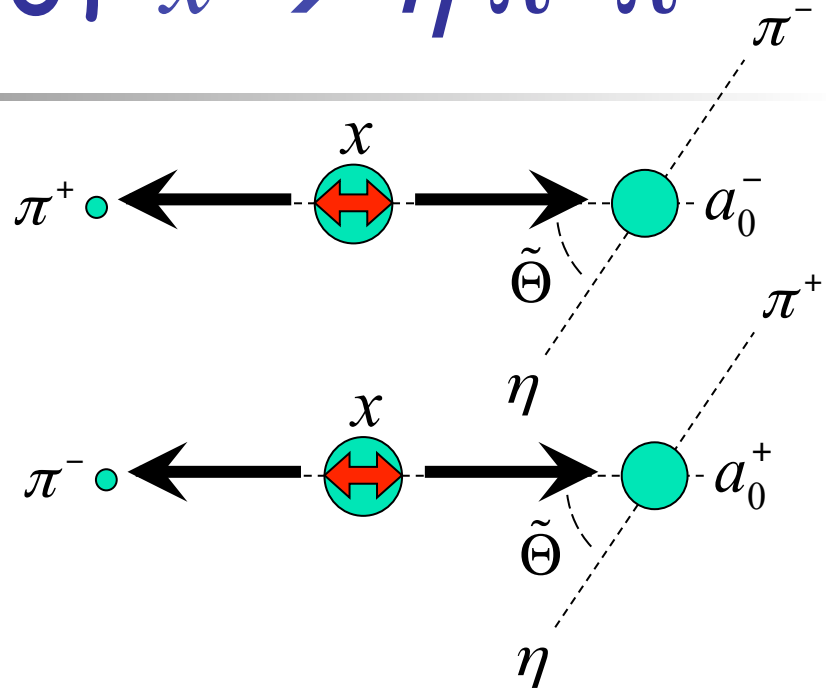
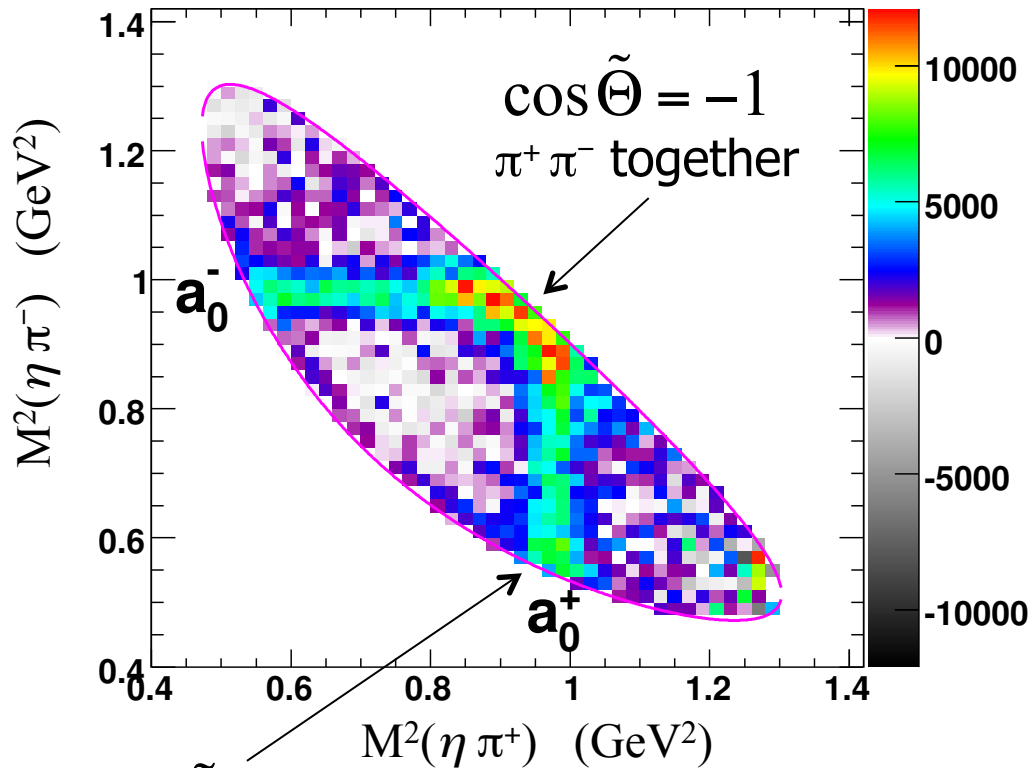
Raw Event Distribution



- Event-by-event, rescale meson sidebands to lie within the Dalitz plot contour
- Algebraic method developed to do this projection...



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$



-two amplitudes $A_{m=\pm 1}(m_{a_0^+ \pi^-}, m_{a_0^- \pi^+})$ to sum for each event

- Background-subtracted acceptance-corrected Dalitz plot reveals dominance of decay via $a_0^\pm \pi^\mp$ intermediate states.
- Strong interference of bands seen. Amplitude analysis!

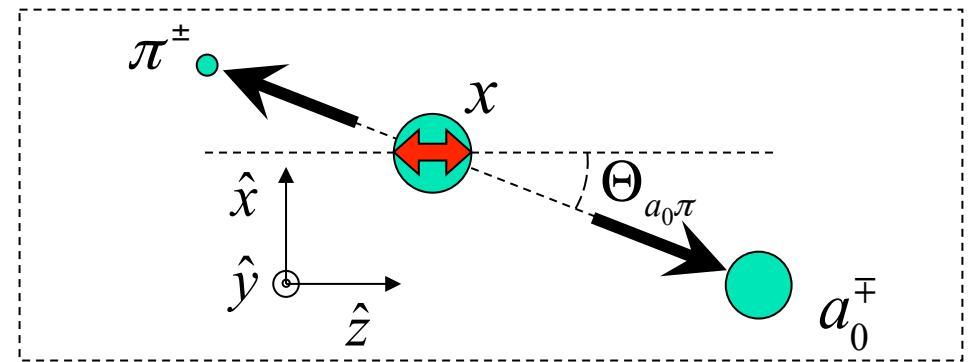


From decay: find spin & parity

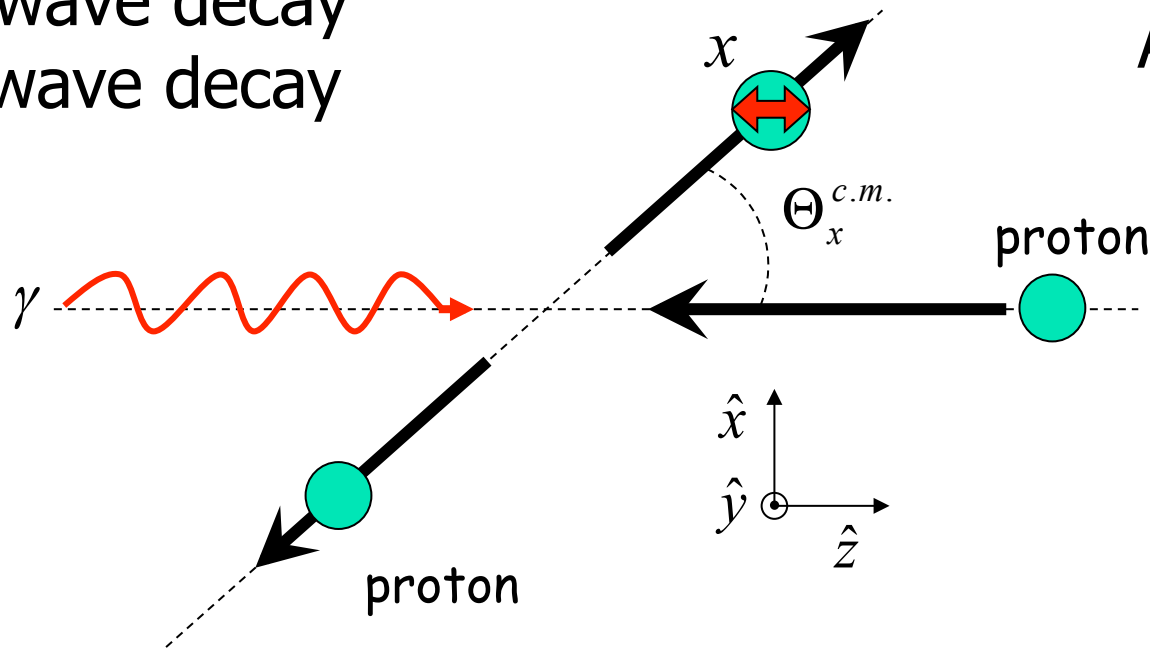
$$x \rightarrow a_0^\pm + \pi^\mp$$

$$J^P \rightarrow 0^+ + 0^- + L^{-1L}$$

f_1 : p -wave decay
 η : s -wave decay



Adair system

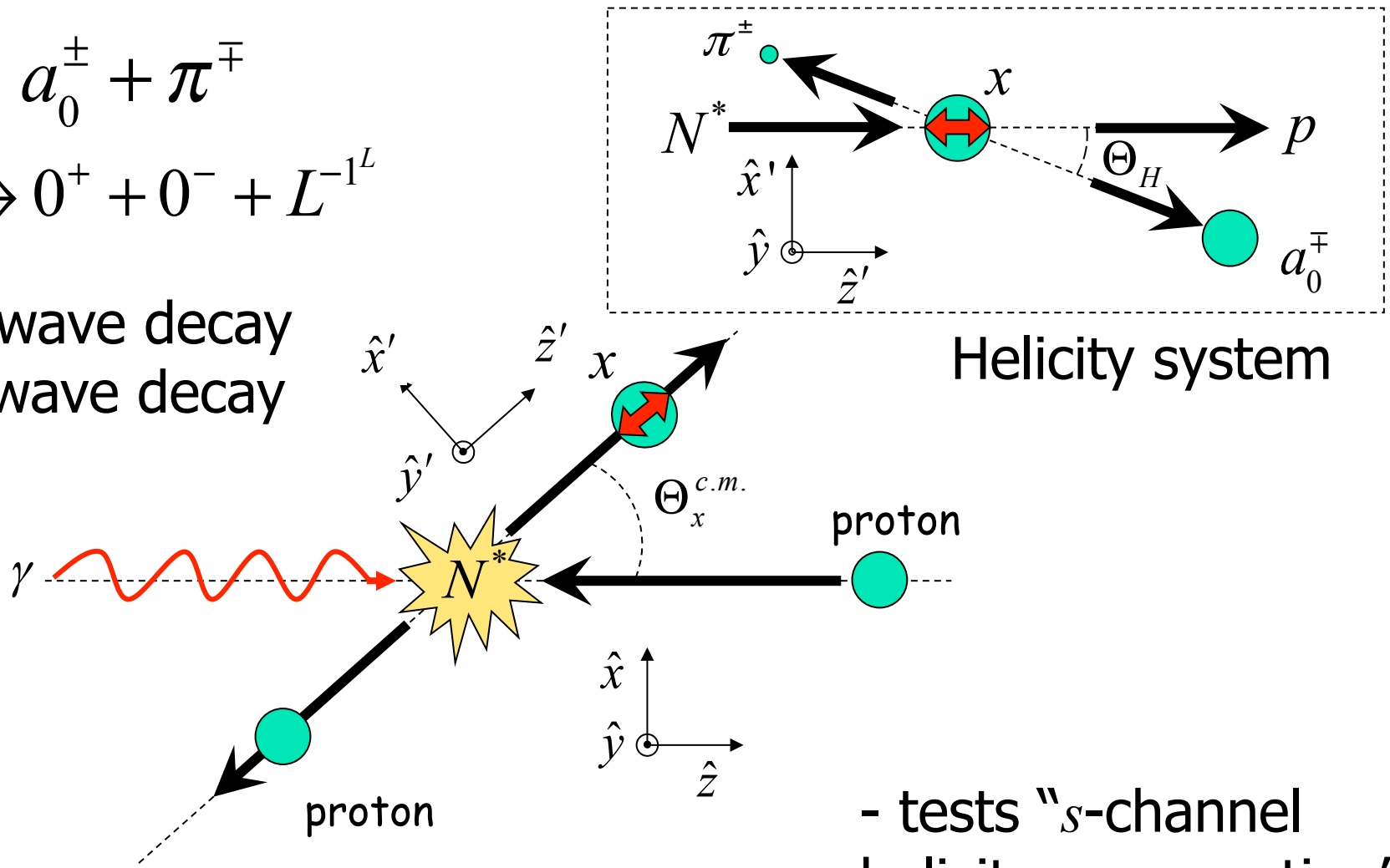


η f_1 From decay: find spin & parity

$$x \rightarrow a_0^\pm + \pi^\mp$$

$$J^P \rightarrow 0^+ + 0^- + L^{-1L}$$

f_1 : p -wave decay
 η : s -wave decay

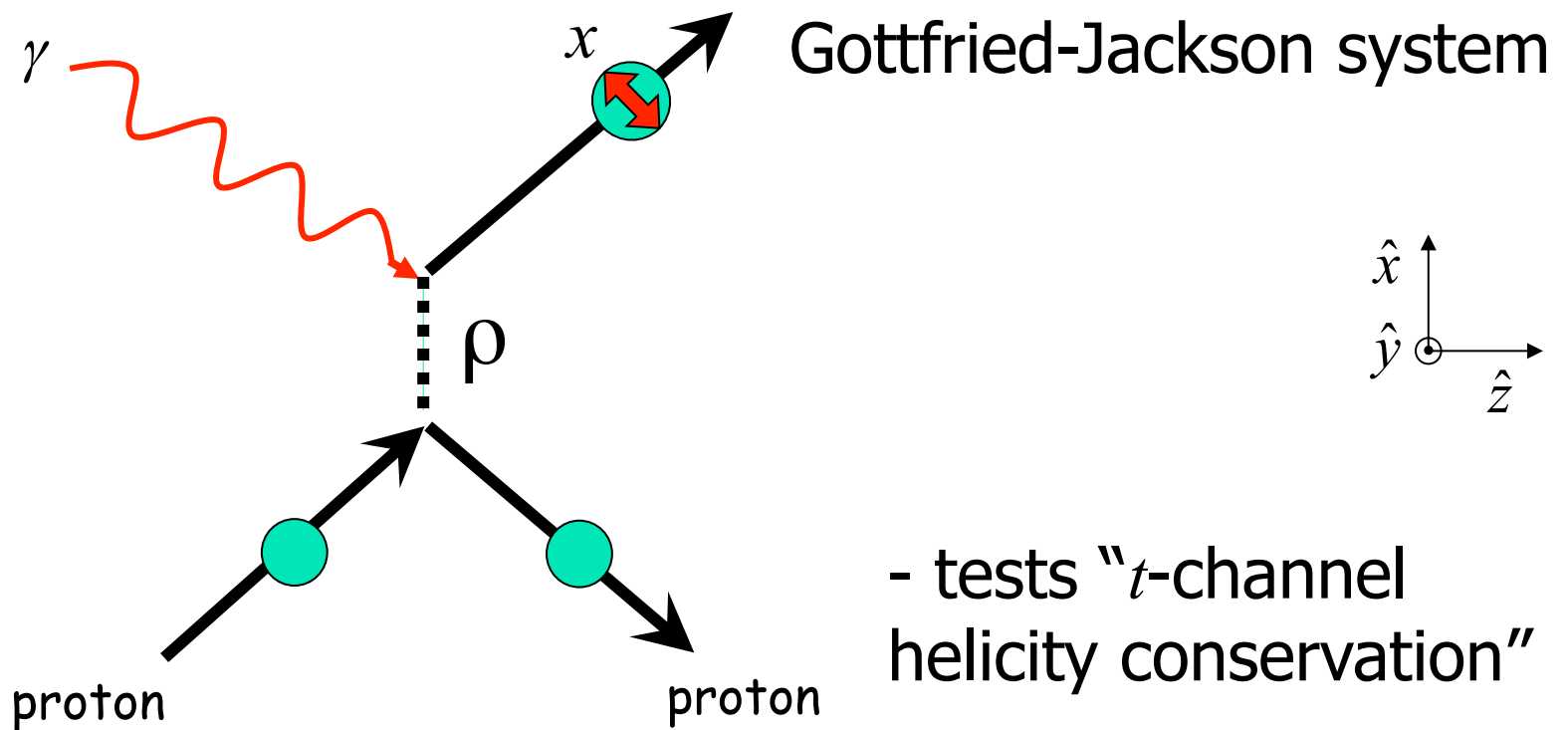
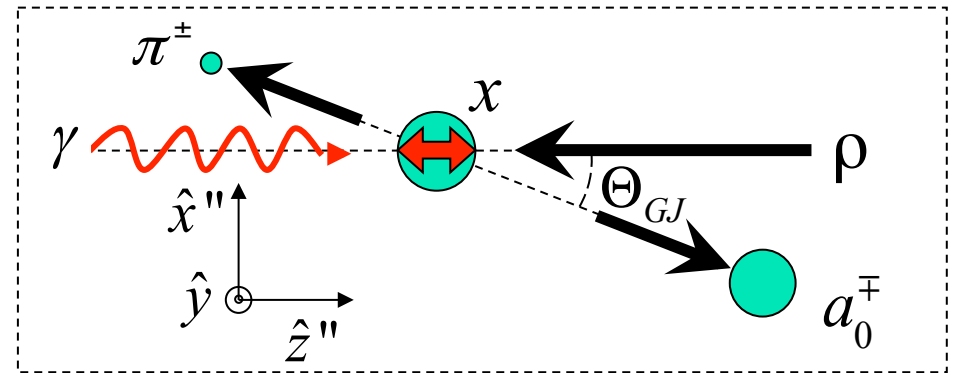


- tests “ s -channel helicity conservation”

γf_1 From decay: find spin & parity

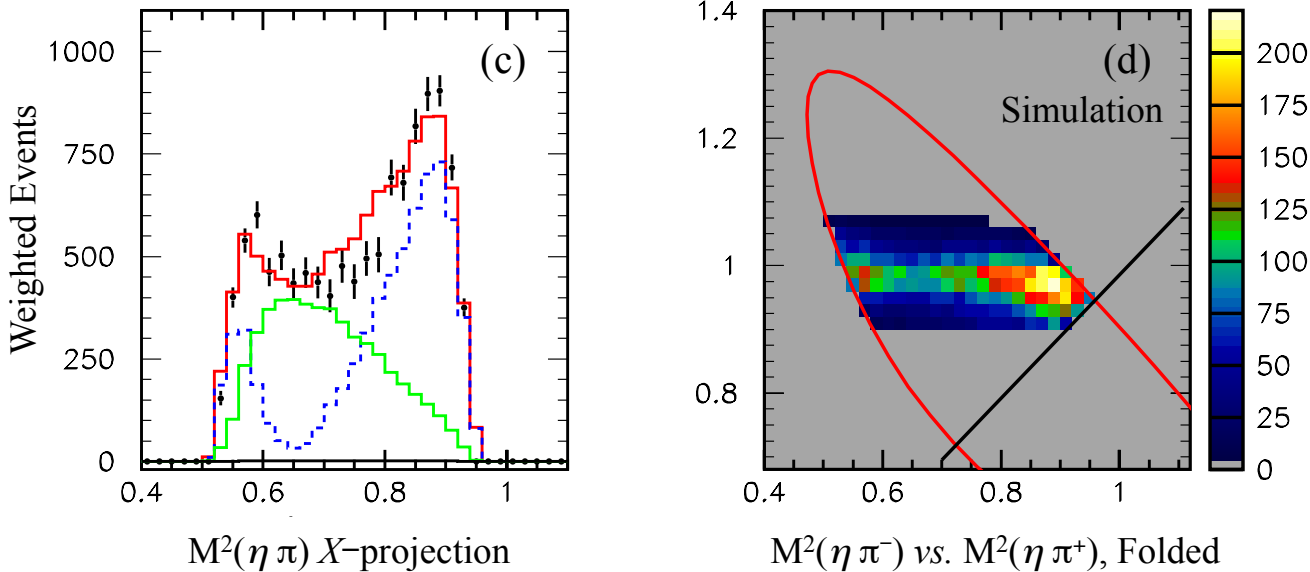
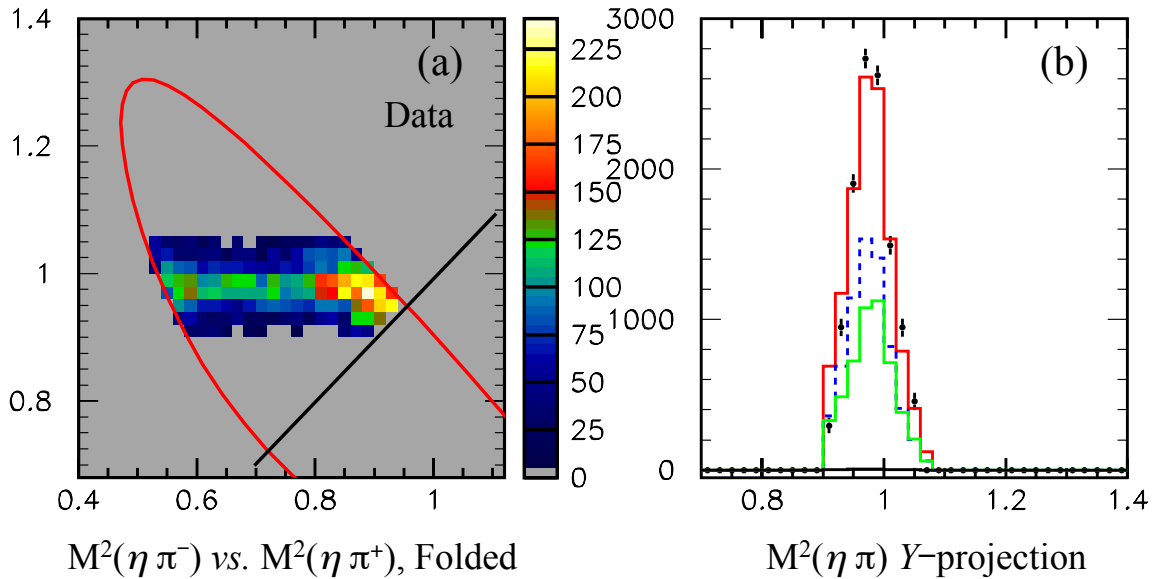
$$x \rightarrow a_0^\pm + \pi^\mp$$

$$J^P \rightarrow 0^+ + 0^- + L^{-1L}$$





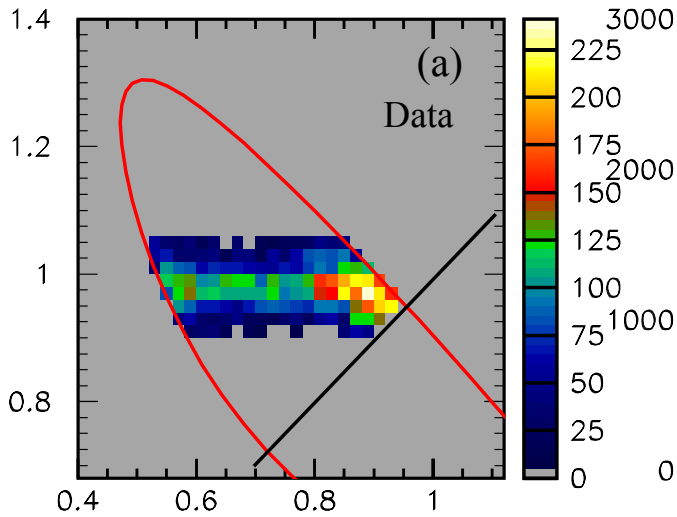
Helicity system fit



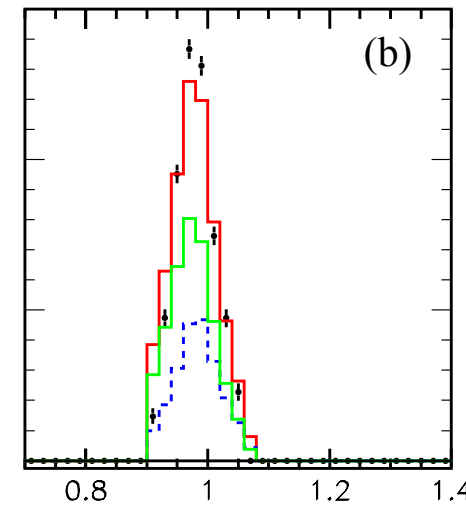
- s -channel helicity system
- Components:
 - Blue: $L=1, m=0$
 - Green: $L=1, m=\pm 1$
 - Red: Total
- a_0^\pm interference reproduced
- p -wave decay and negative parity demonstrated
- Decaying meson is definitely the $f_1(1285)$



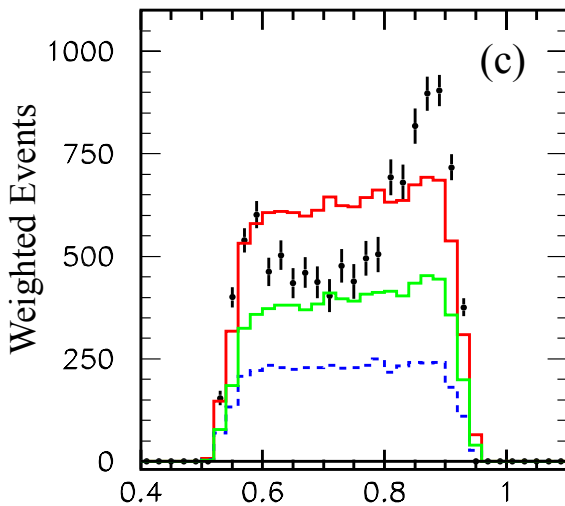
Gottfried-Jackson system fit



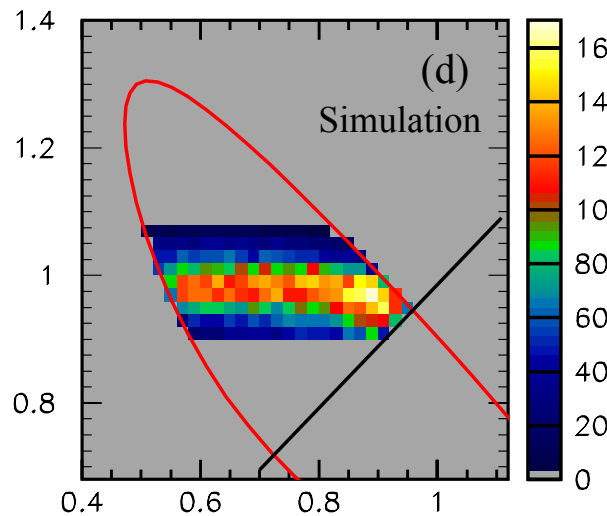
$M^2(\eta \pi^-)$ vs. $M^2(\eta \pi^+)$, Folded



$M^2(\eta \pi)$ Y-projection



$M^2(\eta \pi)$ X-projection



$M^2(\eta \pi^-)$ vs. $M^2(\eta \pi^+)$, Folded

- t -channel helicity system

- Components:

- Blue: $L=1, m=0$
- Green: $L=1, m=\pm 1$
- Red: Total
- Cyan: $L=0$ fit

- a_0 interference NOT reproduced

- Decaying meson is not aligned in this system



Properties of $f_1(1285)$ vs. $\eta(1295)$

	$f_1(1285)$	$\eta(1295)$	CLAS
$I^G(J^{PC})$	$0^+(1^{++})$	$0^+(0^{-+})$	$J^P = 1^+$
Mass (MeV)	$1281.9 \pm .5$	1294 ± 4	1281.0 ± 0.8
Width, Γ (MeV)	24.2 ± 1.1	55 ± 5	18.4 ± 1.4
Decays:			
4π	$33 \pm 2\%$	-	-
$\eta \pi \pi$	$52 \pm 2\%$	Seen	-
$\frac{\Gamma(a_0\pi (noKK))}{\Gamma(\eta\pi\pi (total))}$	$69 \pm 13\%$	-	$74 \pm 9\%$
$\frac{\Gamma(K\bar{K}\pi)}{\Gamma(\eta\pi\pi)}$	$17.1 \pm 1.3\%$	-	$21.6 \pm 3.1\%$
$\frac{\Gamma(\gamma\rho^0)}{\Gamma(\eta\pi\pi)}$	$10.5 \pm 2.2\%$	Not seen	$4.7 \pm 1.8\%$



Conclusions:

arXiv:1604.07425 [nucl-ex], Accepted by Phys. Rev. C
R. Dickson et al., CLAS Collaboration

- The photoproduced meson CLAS sees at 1281 MeV is the $f_1(1285)$.
- Production mechanism is more consistent with s -channel process (N^* -decay...) than t -channel process (meson-exchange)
 - Cross section is much "flatter" than η' production
 - The $f_1(1285)$ is aligned in the s -channel helicity system, seen via $\eta \pi^+ \pi^-$ Dalitz-plot amplitude analysis
- $\Gamma \sim 18.2$ MeV; narrower than PDG average
- Branching ratios measured:
 - $K K \pi / \eta \pi \pi$, $a_0 \pi / \eta \pi \pi$ and $\gamma \rho^0 / \eta \pi \pi$



Backup Slides

CLAS Experiment

- Photoproduction:
 - Targets: unpolarized LH_2 , polarized p, & HD-ice
 - Beams: unpolarized, circular, linear, to $\sim 5 \text{ GeV}$
 - Reconstructed $\text{K}^+p\pi^- (\pi^0)$ or $\text{K}^+\pi^+\pi^- (n)$
 - 20×10^9 triggers $\rightarrow 1.41 \times 10^6$ $\text{KY}\pi$ events in g11a
- Electroproduction:
 - Q^2 from ~ 0.5 to $\sim 3 (\text{GeV}/c)^2$
 - Structure functions from Rosenbluth and beam-helicity separations



Quark Model for Mesons PDG 2014

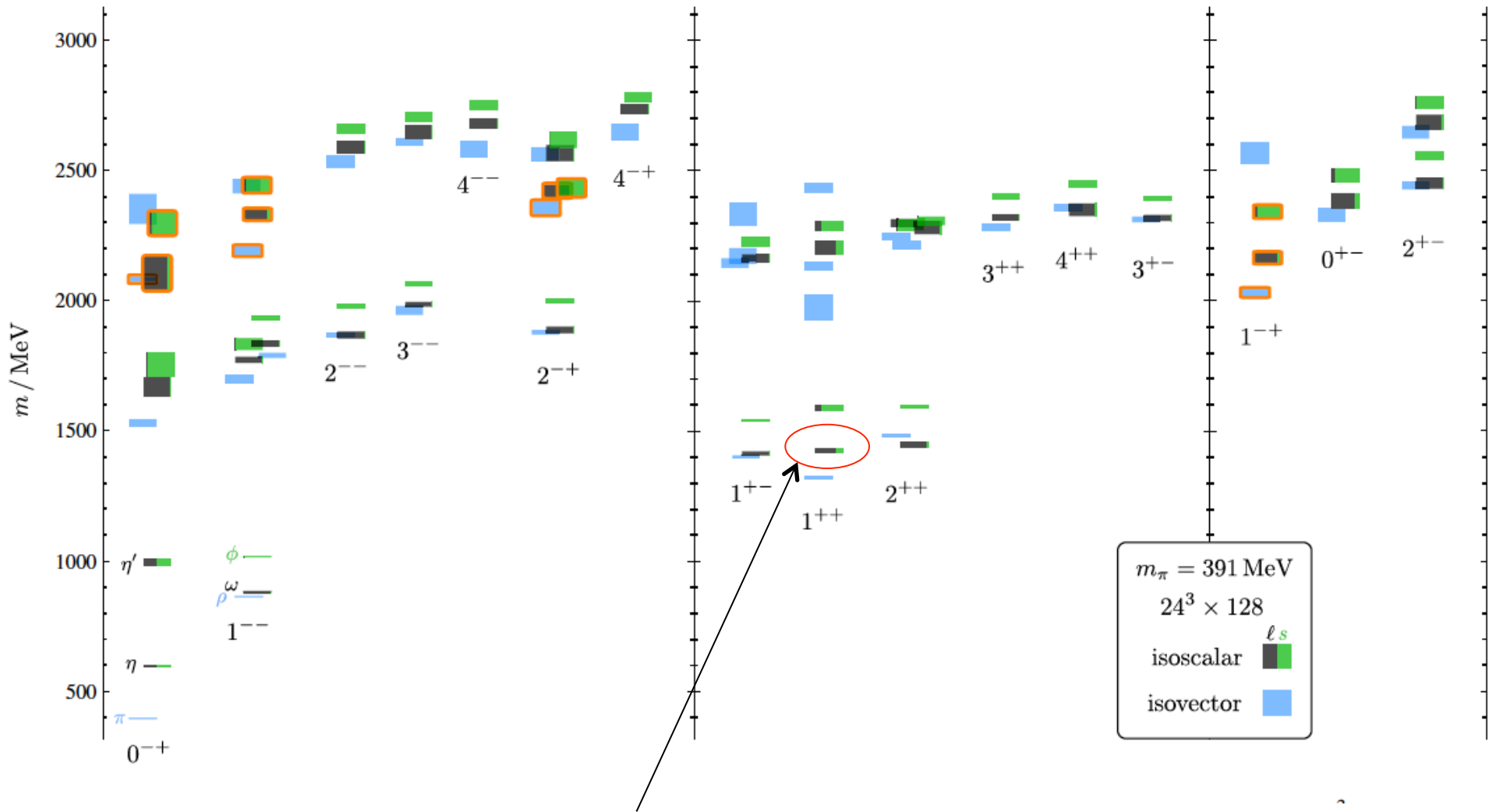
Table 15.2: Suggested $q\bar{q}$ quark-model assignments for some of the observed light mesons. Mesons in bold face are included in the Meson Summary Table. The wave functions f and f' are given in the text. The singlet-octet mixing angles from the quadratic and linear mass formulae are also given for the well established nonets. The classification of the 0^{++} mesons is tentative: The light scalars $a_0(980)$, $f_0(980)$, and $f_0(500)$ are often considered as meson-meson resonances or four-quark states, and are omitted from the table. Not shown either is the $f_0(1500)$ which is hard to accommodate in the nonet. The isoscalar 0^{++} mesons are expected to mix. See the “Note on Scalar Mesons” in the Meson Listings for details and alternative schemes.

$n \ 2s+1 \ell_J$	J^{PC}	$l = 1$ $u\bar{d}, \bar{u}d, \frac{1}{\sqrt{2}}(d\bar{d} - u\bar{u})$	$l = \frac{1}{2}$ $u\bar{s}, d\bar{s}, \bar{d}s, -\bar{u}s$	$l = 0$ f'	$l = 0$ f	θ_{quad} [°]	θ_{lin} [°]
$1 \ 1S_0$	0^{-+}	π	K	η	$\eta'(958)$	-11.4	-24.5
$1 \ 3S_1$	1^{--}	$\rho(770)$	$K^*(892)$	$\phi(1020)$	$\omega(782)$	39.1	36.4
$1 \ 1P_1$	1^{+-}	$b_1(1235)$	K_{1B}^\dagger	$h_1(1380)$	$h_1(1170)$		
$1 \ 3P_0$	0^{++}	$a_0(1450)$	$K_0^*(1430)$	$f_0(1710)$	$f_0(1370)$		
$1 \ 3P_1$	1^{++}	$a_1(1260)$	K_{1A}^\dagger	$f_1(1420)$	$f_1(1285)$		
$1 \ 3P_2$	2^{++}	$a_2(1320)$	$K_2^*(1430)$	$f_2'(1525)$	$f_2(1270)$	32.1	30.5
$1 \ 1D_2$	2^{-+}	$\pi_2(1670)$	$K_2(1770)^\dagger$	$\eta_2(1870)$	$\eta_2(1645)$		
$1 \ 3D_1$	1^{--}	$\rho(1700)$	$K^*(1680)$		$\omega(1650)$		
$1 \ 3D_2$	2^{--}		$K_2(1820)$				
$1 \ 3D_3$	3^{--}	$\rho_3(1690)$	$K_3^*(1780)$	$\phi_3(1850)$	$\omega_3(1670)$	31.8	30.8
$1 \ 3F_4$	4^{++}	$a_4(2040)$	$K_4^*(2045)$		$f_4(2050)$		
$1 \ 3G_5$	5^{--}	$\rho_5(2350)$	$K_5^*(2380)$				
$1 \ 3H_6$	6^{++}	$a_6(2450)$			$f_6(2510)$		
$2 \ 1S_0$	0^{-+}	$\pi(1300)$	$K(1460)$	$\eta(1475)$	$\eta(1295)$		
$2 \ 3S_1$	1^{--}	$\rho(1450)$	$K^*(1410)$	$\phi(1680)$	$\omega(1420)$		

[†] The $1^{+\pm}$ and $2^{-\pm}$ isospin $\frac{1}{2}$ states mix. In particular, the K_{1A} and K_{1B} are nearly equal (45°) mixtures of the $K_1(1270)$ and $K_1(1400)$. The physical vector mesons listed under 1^3D_1 and 2^3S_1 may be mixtures of 1^3D_1 and 2^3S_1 , or even have hybrid components.



LQCD: Excited Isoscalar Mesons



The $J^{PC} = 1^{++}$ mesons, including the $f_1(1285)$, are 'seen' in recent lattice calculations...

J. Dudek *et al.* Phys. Rev. D **88**, 094505 (2013)



Dynamically Generated Mesons

- The $f_1(1285)$ as a $\{K\bar{K}^* + \text{c.c.}\}$ composite state
 - Chiral Lagrangian + unitarization of the pseudoscalar - vector meson nonet interaction
 - Lattice calculations
 - Expect “non-standard” production mechanisms, if true

M. F. M. Lutz and E. E. Kolomeitsev Nucl Phys **A730** 392, (2004)
L. Roca, E. Oset, J. Singh Phys Rev **D72**, 014002 (2005)
F. Aceti, Ju-Jun Xie, E. Oset, arXiv:1505.06134 (2015)



Branching Ratios

Item	Value	Stat. Uncert.	Syst. Uncert.	PDG $f_1(1285)$
$\eta\pi^+\pi^-$ Event Yield	1.33×10^5	4.9×10^3	2.9×10^3	
$\eta\pi^+\pi^-$ Acceptance	0.0652	9.7×10^{-5}	0.0072	
$K^\pm K^0 \pi^\mp$ Event Yield	6570	180	340	
$K^\pm K^0 \pi^\mp$ Acceptance	0.0149	3.18×10^{-5}	0.0016	
$\gamma\rho^0$ Event Yield	3790	790	850	
$\gamma\rho^0$ Acceptance	0.0248	6.4×10^{-5}	0.0050	
Isospin C.G. $\Gamma(K^\pm K^0 \pi^\mp)/\Gamma(K\bar{K}\pi)$	2/3			
Isospin C.G. $\Gamma(\eta\pi^+\pi^-)/\Gamma(\eta\pi\pi)$	2/3			
$\gamma\rho^0$ correction from η' $d\sigma/d\Omega$	0.95			
Branching Fraction $\Gamma(K\bar{K}\pi)/\Gamma(\eta\pi\pi)$	0.216	0.010	0.031	0.171 ± 0.013
Branching Fraction $\Gamma(\gamma\rho^0)/\Gamma(\eta\pi\pi)$	0.047	0.010	0.015	0.105 ± 0.022

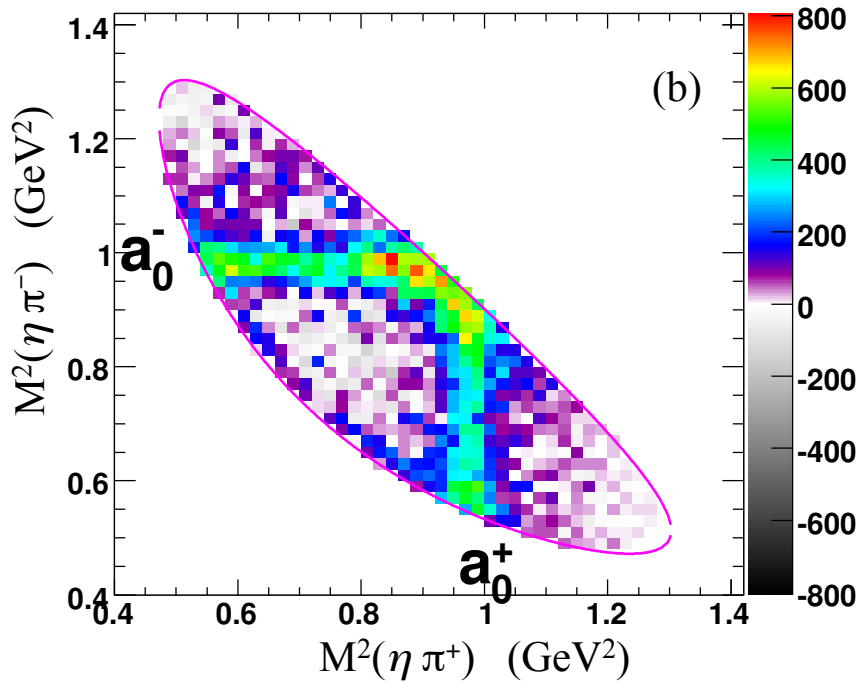
TABLE III. Relative branching fractions of the $f_1(1285)$ meson, with estimated uncertainties from all sources.

- $K\bar{K}\pi / \eta\pi\pi$ ratio agrees with PDG average
 - (isospin factors applied)
- $\gamma\rho^0 / \eta\pi\pi$ ratio smaller than PDG average by 55%

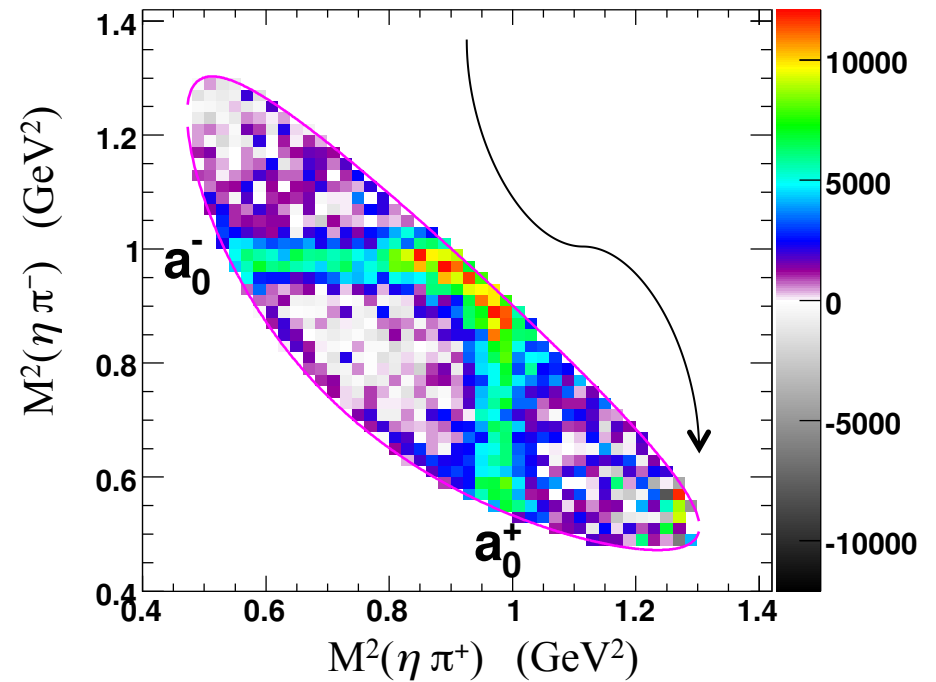


Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

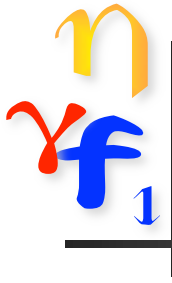
Background Subtracted



Acceptance Corrected



- Subtract huge multi-pion background to reveal...
- ... dominance of decay via $a_0^\pm \pi^\mp$ intermediate state.
- Strong interference of bands seen. Amplitude analysis!



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

$$A_{m=\pm 1}(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}) = BW(m_{a_0^+\pi^-}) W_{1,\pm 1}(\Theta_{a_0^+\pi^-}, \phi_{a_0^+\pi^-}) + BW(m_{a_0^-\pi^+}) W_{1,\pm 1}(\Theta_{a_0^-\pi^+}, \phi_{a_0^-\pi^+})$$

$$A_{m=0}(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}) = BW(m_{a_0^+\pi^-}) (W_{1,0}(\Theta_{a_0^+\pi^-}, \phi_{a_0^+\pi^-}) + W_{0,0}) + BW(m_{a_0^-\pi^+}) (W_{1,0}(\Theta_{a_0^-\pi^+}, \phi_{a_0^-\pi^+}) + W_{0,0})$$

$$BW(m | m_0, \Gamma_0) = \frac{\sqrt{m_0 \Gamma_0}}{m_0^2 - m^2 - im_0 \Gamma_0} \frac{q(m)}{q(m_0)} \quad \text{- a Breit-Wigner for each } a_0$$

- angular distribution in the selected system

$$f_1: W_{L=1, m=0, \pm 1}(\Theta_H, \phi) = a Y_{1,+1}(\Theta_H, \phi) + b Y_{1,0}(\Theta_H, \phi) + a Y_{1,-1}(\Theta_H, \phi)$$

$$\eta: W_{L=0, m=0}(\Theta_H, \phi) = c Y_{0,0}$$

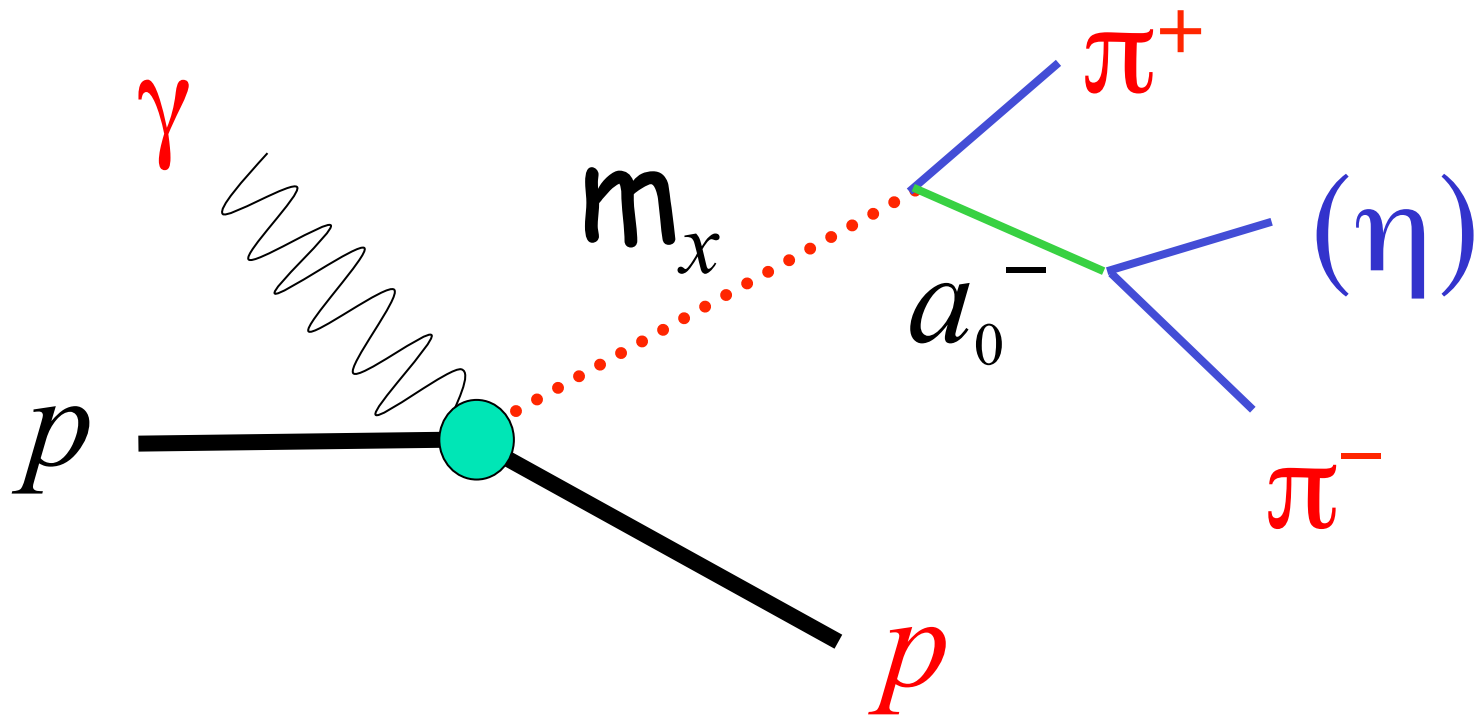
-total decay-weighted magnitude squared

$$T(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}) = \frac{q(m_{a_0^+\pi^-}) q(m_{a_0^-\pi^+})}{q(m_0) q(m_0)} \left(\left| A_{m=\pm 1}(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}) \right|^2 + \left| A_{m=0}(m_{a_0^+\pi^-}, m_{a_0^-\pi^+}) \right|^2 \right)$$



One Reaction Topology

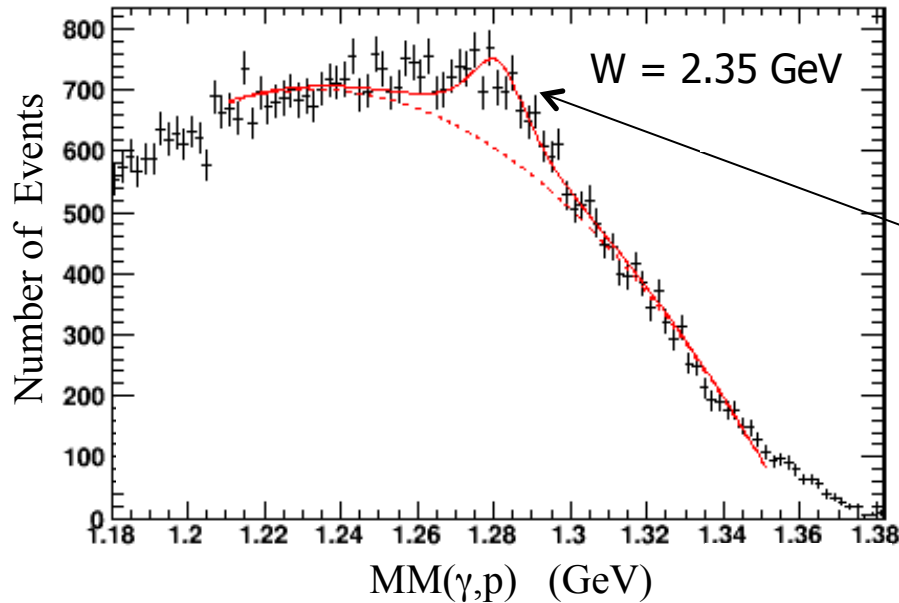
(example)



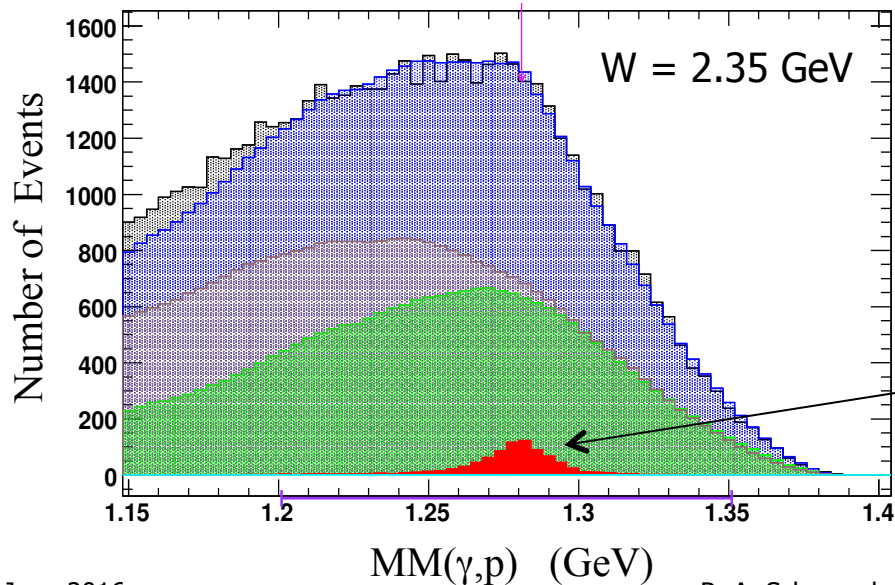
red = measured particles



Two yield extraction methods



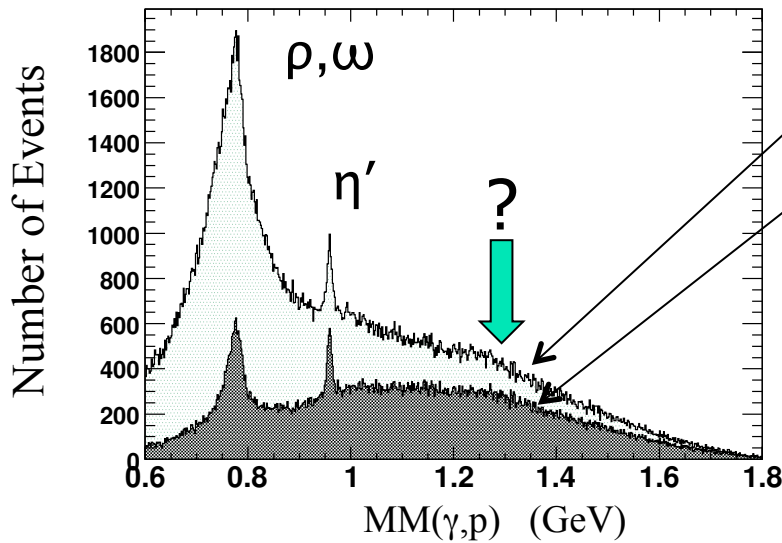
- Voigtian lines shape using known CLAS resolution
- Convolution of BW and Gaussian



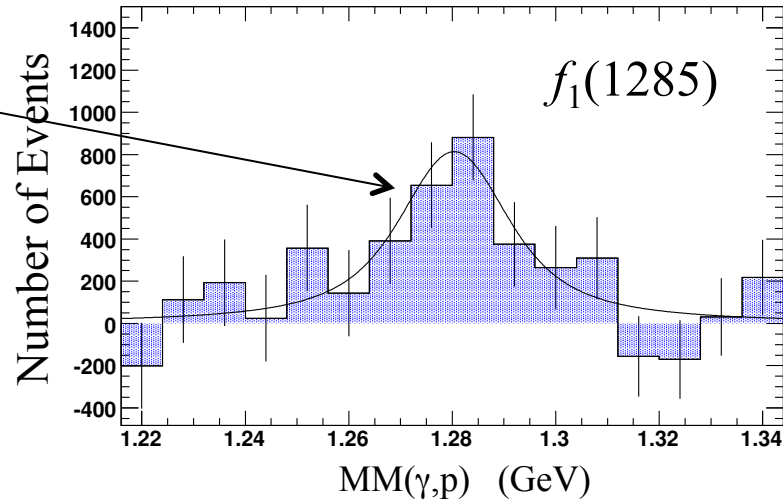
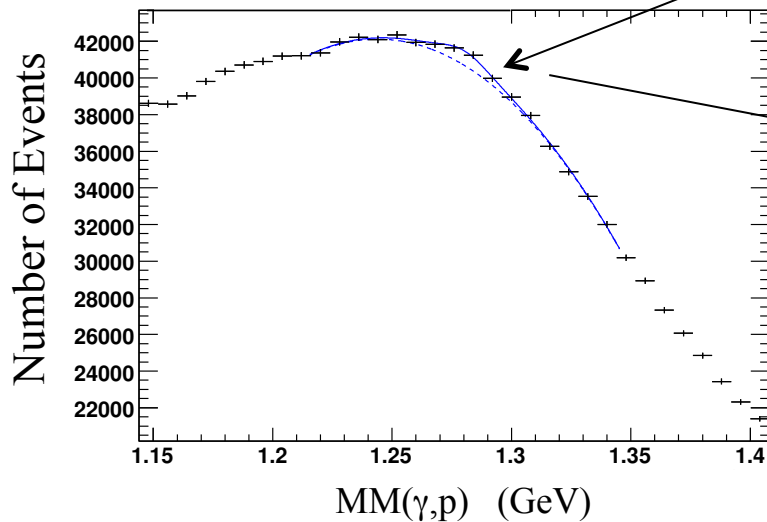
- Monte Carlo fitting using signal and estimated multi-pion backgrounds
- $p \rho \pi \pi$ (green)
- $p \phi_1(1370)$ (purple)
- $p x(1280)$ (red) - signal
- Total (blue)



Looking for $\gamma\rho^0$ decays

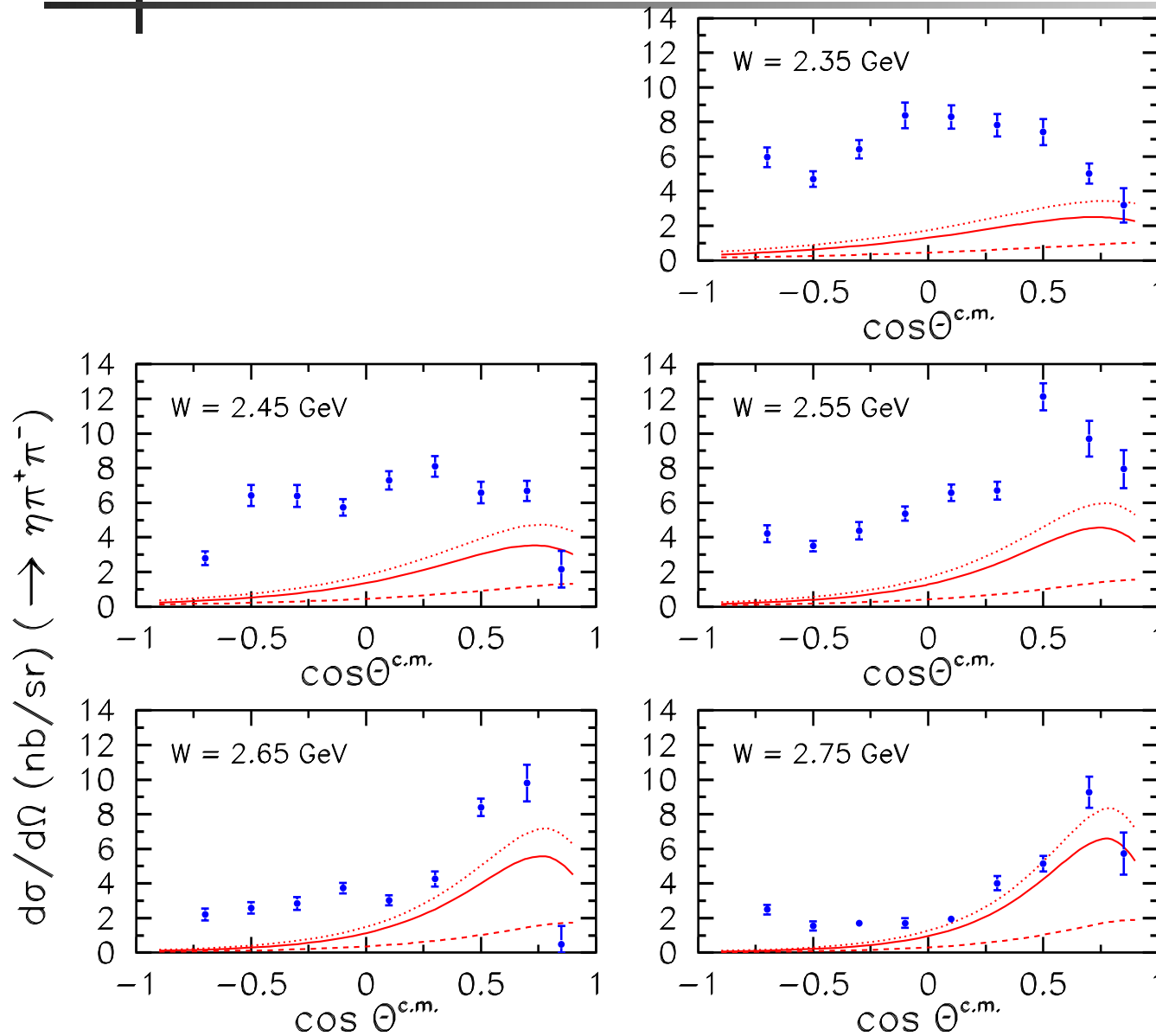


- Kinematic fit to $\gamma p \rightarrow p\pi^+\pi^-(\gamma)$
- Select $p_{\text{perp}} > 40 \text{ MeV}/c$
- 2nd kin. fit to $\gamma p \rightarrow p\pi^+\pi^-(\pi^0)$ to reject π^0 background
- Very small signal: only extract branching ratio to $\eta \pi^+ \pi^-$
 - Sum over all kinematics

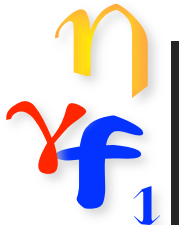




Comparison with Models

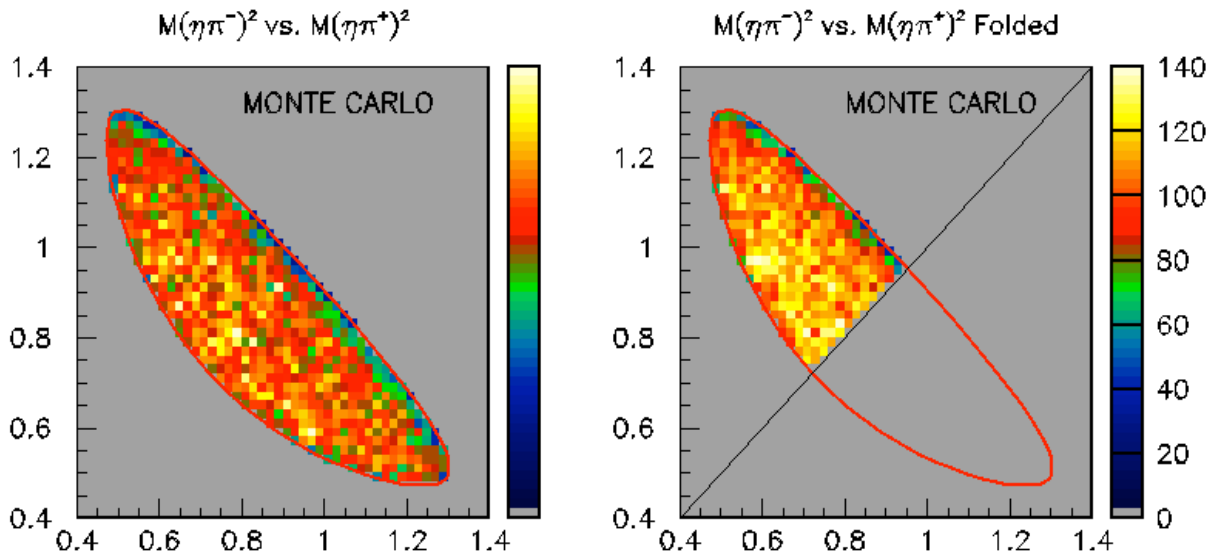
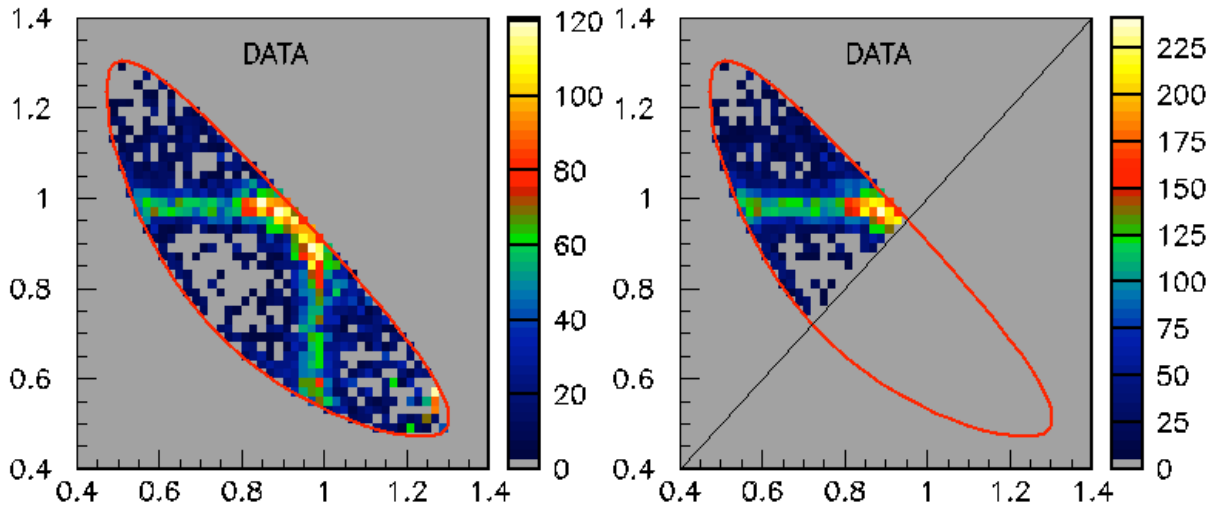


- N. Kochelev model
 - Effective Lagrangian
 - t-channel ρ and ω exchange
 - Solid: $f_1(1285)$
 - Dashed: $\eta(1295)$
 - Dotted: sum
- Poor match to data



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

$x(1280) \rightarrow \eta \pi \pi$ Dalitz Analysis

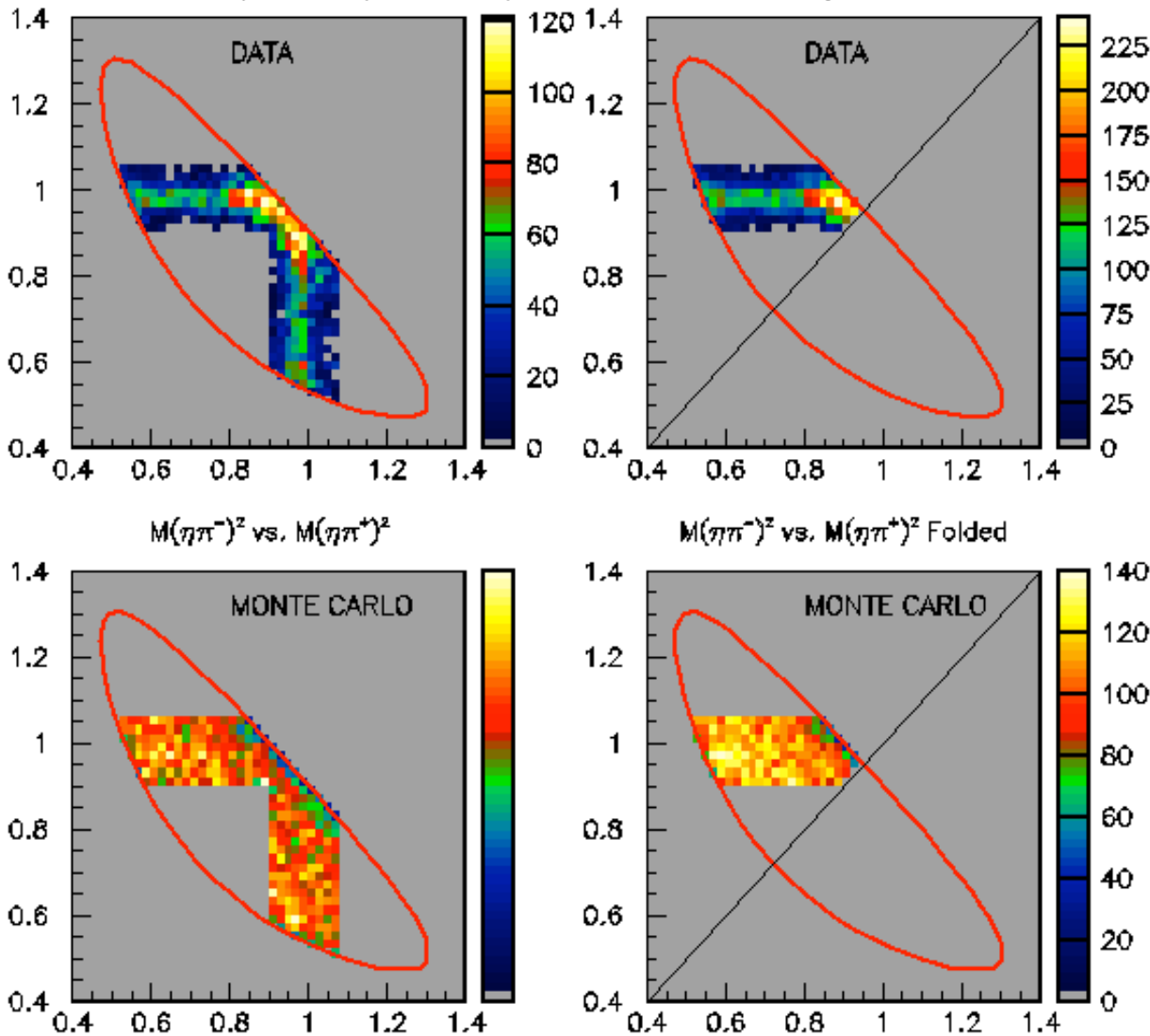


- Fold data on symmetry axis
- Generate "phase space" Monte Carlo events with finite width of meson and CLAS resolution included
- "Weight" the events with amplitude-based intensity



Dalitz analysis of $x \rightarrow \eta \pi^+ \pi^-$

$x(1280) \rightarrow \eta \pi \pi$ Dalitz Analysis



- Fit to full plot did not converge, so trim data to focus on 'bands'.
- Structure in unweighted Monte Carlo due to finite width and resolution effects



Helicity system fit

- The $f_1(1285)$ is “aligned” in the helicity system.
- The mix of $m = 0$ and $m = \pm 1$ is a property of the production mechanism in the range $2.30 < W < 2.80$ GeV.

$$P_{\pm} : P_0 = 31.8 : 69.2, \pm 1.4\%.$$

- Discuss later...
- We also measure the ratio

$$\frac{\Gamma(a_0\pi(n\pi KK))}{\Gamma(\eta\pi\pi(total))} = 74 \pm 2(stat) \pm 9(syst)\%$$

- Consistent with PDG value



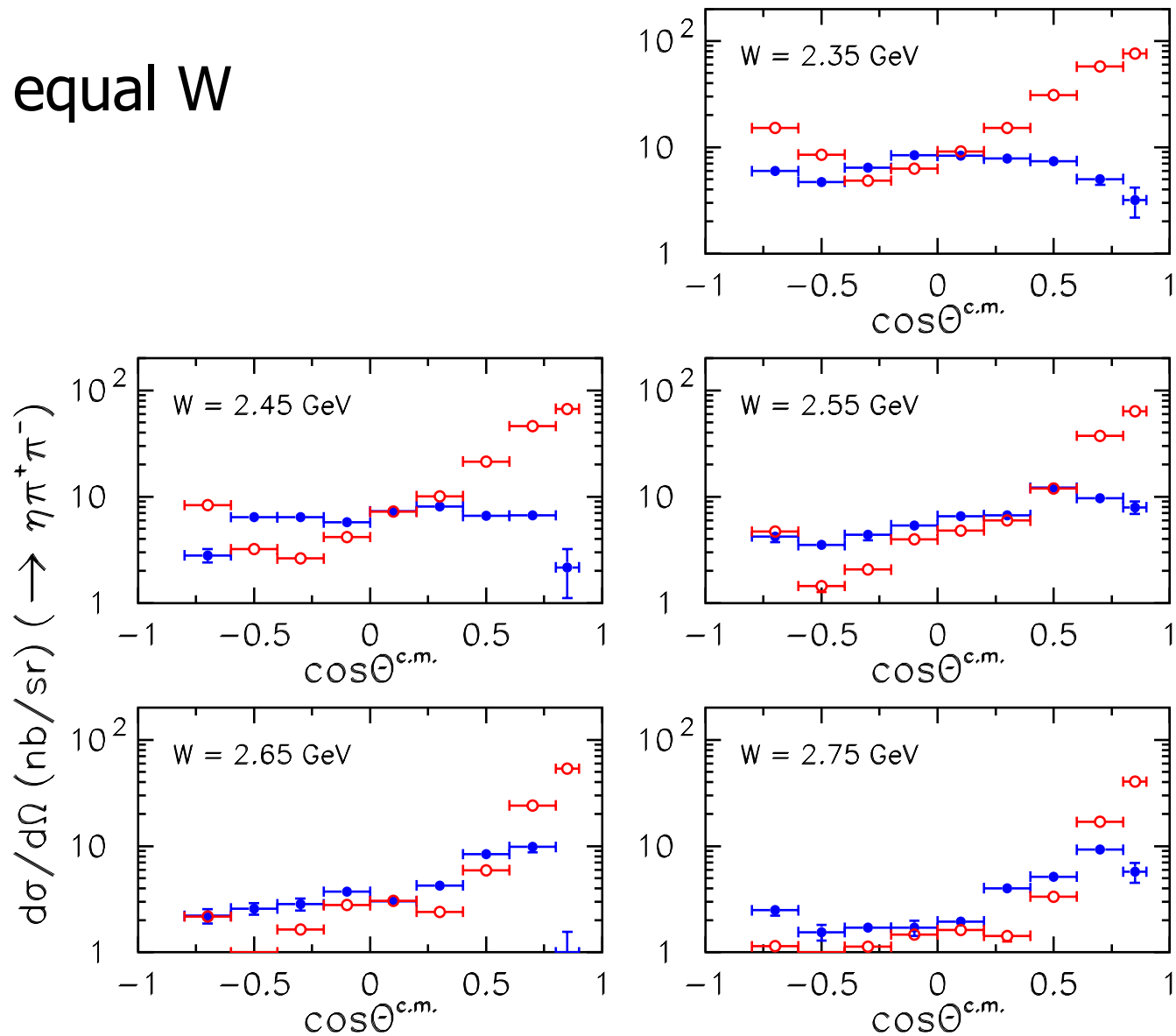
Speculation re $f_1(1285)$ production

- Alignment in helicity system suggests s -channel N^* production decays to $f_1(1285) p$
 - Can we infer J^P of the N^* baryon resonance?
 - $3/2^+ \rightarrow 1^+ + 1/2^+$ in s -wave leads to $P_{\pm} : P_0 = 1 : 2$ as seen in the data
 - $1/2^+ \rightarrow 1^+ + 1/2^+$ in s -wave leads to $P_{\pm} : P_0 = 2 : 1$, opposite to what data show
- But there are no known N^* states with low J at $W \sim 2.5$ GeV, so the question remains open



Compare meson types

At equal W





Compare meson types

At equal excess energy
above threshold

