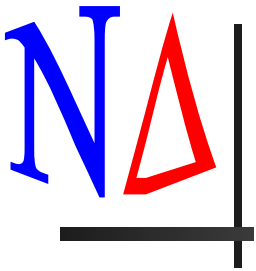


Photoproduction of Structure in the $d\pi$ System Near the N Δ Mass: Sign of a Quasi- Bound State?



Reinhard Schumacher
Carnegie Mellon University

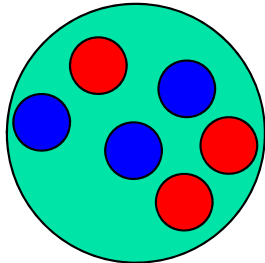
work with: Paul Mattione
Jefferson Lab CLAS Collaboration

$N\Delta$ | Outline / Overview

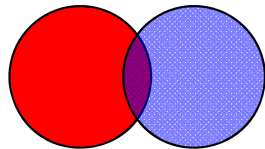
- Theoretical expectations about two-baryon resonant states
- Experimental observations
 - $\Delta\Delta$ quasi-bound state: WASA/COSY
 - πd & pp elastic scattering: SAID analysis
- Photoproduction at CLAS/JLab
 - $\gamma d \rightarrow d \pi^+ \pi^-$ exclusive channel
 - $N\Delta$ quasi-bound state or ISI/FSI?

N Δ

Two-baryon resonances

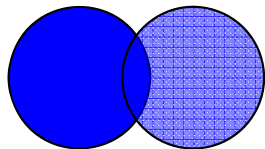


3S_1



$I(J^P) = 0(1^+)$
“ $\mathcal{D}_{11} = \mathcal{D}_{01}$ ”

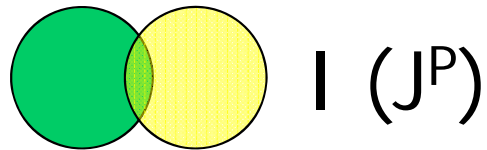
1S_0



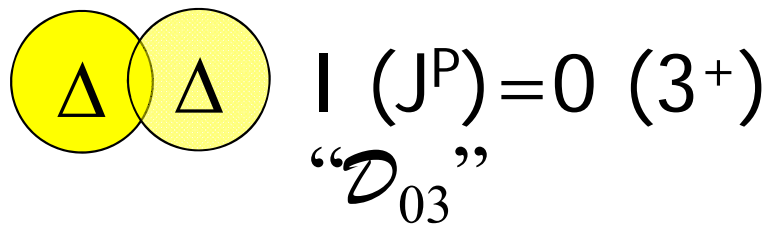
$I(J^P) = 1(0^+)$
“ \mathcal{D}_{10} ”

- 6 quarks in a bag
- The deuteron
 - 2.2 MeV bound
 - The only clear-cut “dibaryonic molecule”
- Recall the nn , pp , and np strong spin singlet states are unbound...
 - ... by only ~ 100 keV
 - One of the great “fine-tuning” mysteries of nature!!

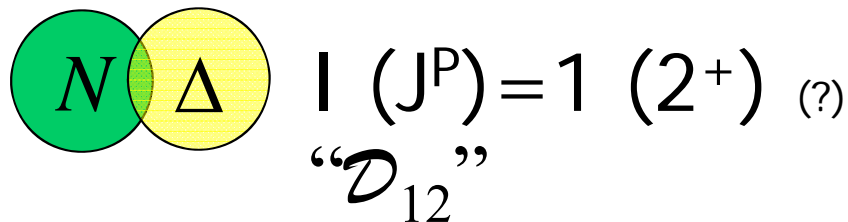
$N\Delta$ | Two-baryon resonances



- Bound $N\Delta$, $\Delta\Delta$, $\Lambda\Lambda$ (H-particle)
 - Binding?
 - Width: 'narrow' or 'wide'?
 - Spin, Isospin ?



- Recent WASA@COSY claim of discovery



- CLAS study: new observations

$N\Delta$ | Some Thresholds

$$m_{\Delta^+} + m_N = 1232 + 939 = 2171 \text{ MeV}$$

$$m_d + m_{\pi} = 1875 + 140 = \underline{2015 \text{ MeV}}$$

$$156 \text{ MeV}$$

The decay of $N\Delta$ to $d\pi$ liberates about 156 MeV at the centroid of the (quasi-) bound state.

For comparison:

$$m_{\Delta^+} + m_{\Delta^+} = 2 \times 1232 = 2464 \text{ MeV}$$

$N\Delta$ Theoretical Expectations

- “ $Y=2$ states in $SU(6)$ theory”
 - F. Dyson & N. Xuong, PRL (1964)
 - $l=1$ $J=2$ state and $l=2$ $J=1$ state in $\overline{27}$ multiplet
- “Multi-quark states Q^6 dibaryon resonances”
 - Mulders, Aerts, De Swart, PRD (1980)
 - Bag model: $N\Delta$ state in a 5S_2 configuration decaying to the 1D_2 NN partial wave channel
- “Flavor octet dibaryons in the quark model”
 - M. Oka PRD (1988)
 - One-gluon exchange color magnetic interaction leads to certain strange dibaryons

$N\Delta$ | Theoretical Expectations

- “ NN core interactions...from 1 gluon exchange”
 - T. Barnes, S. Capstick, M.D. Kovarik, E.S. Swanson, PRC (1983)
 - OGE and quark-exchange model
 - Deuteron and $N\Delta$ states *not* found, but “molecular” (weakly bound) $\Delta\Delta$ was found
- “Deeply-bound dibaryon resonances”
 - K. Maltman, Nucl Phys (1984)
 - QCD-like potential model with hyperfine effects
 - $I=0$ $S=3$, well below the $\Delta\Delta$ & $N\Delta\pi$ thresholds

$N\Delta$ | Theoretical Expectations

- “3-body model calculations of $N\Delta$ and $\Delta\Delta$ dibaryon resonances”
 - A. Gal, H. Garcilazo, Nucl. Phys. **A928** 73 (2014)
 - πNN model with separable pairwise interactions
 - Solve πNN and $\pi N\Delta$ Faddeev equations
 - \mathcal{D}_{12} $N\Delta$ found for $I(J^P) = 1(2^+) & 2(1^+)$
 - \mathcal{D}_{03} $\Delta\Delta$ found for $I(J^P) = 0(3^+) & 3(0^+)$



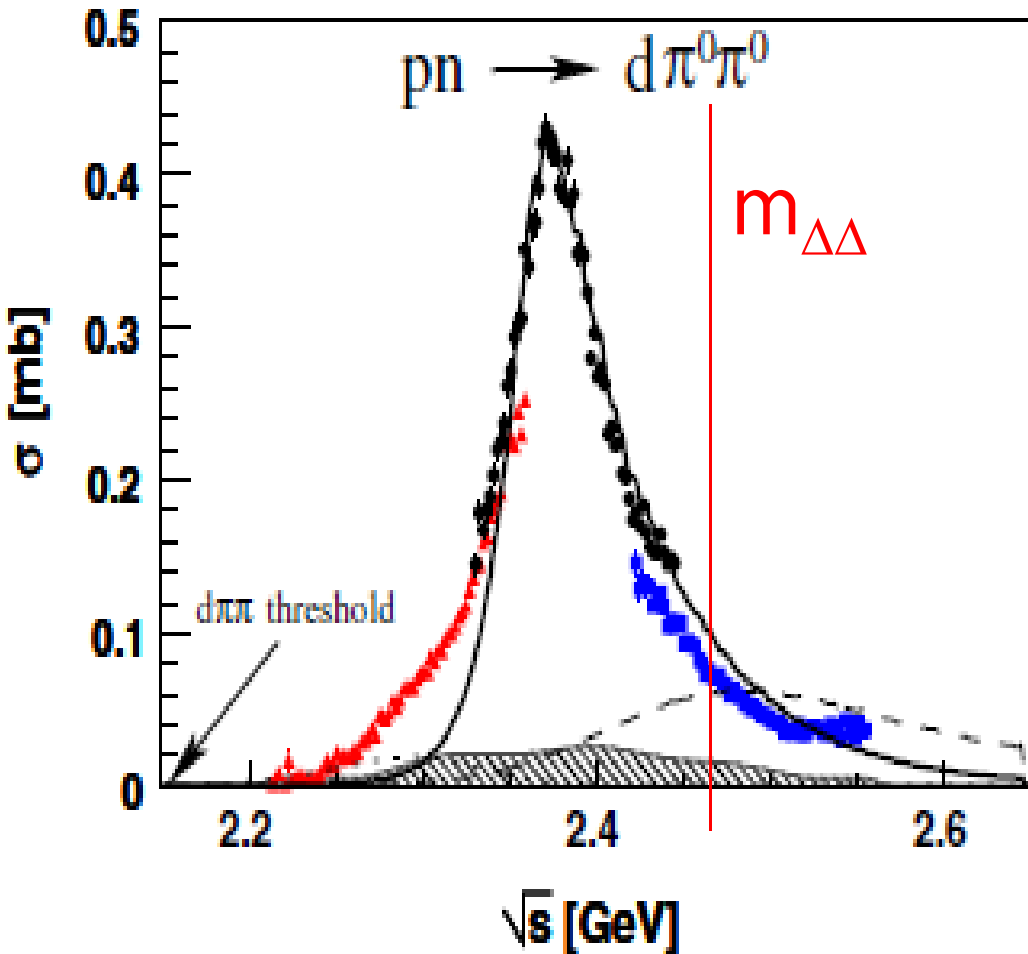
Figure 2: Diagrammatic representation of the πNN Faddeev equations solved in the present work to calculate $N\Delta$ dibaryon resonance poles.

N Δ | Quasi-bound states

- Evidence for $\Delta\Delta$ (“ \mathcal{D}_{03} ”)
 - WASA-at-COSY experiments (Jülich)

P. Adlarson et al, Phys Rev Lett 106, 242302 (2011)
...and numerous others since.

$N\Delta$ | $d^*(2380)$ Resonance in $I(J^P) = 0(3^+)$



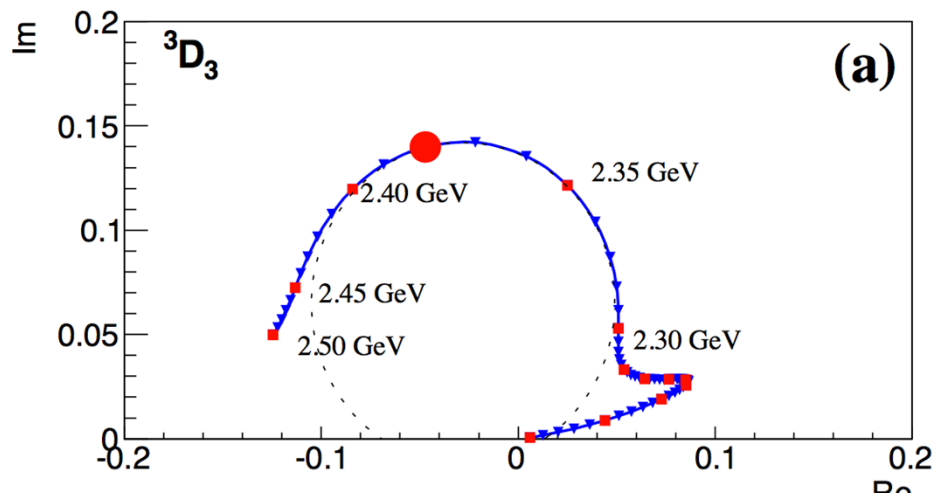
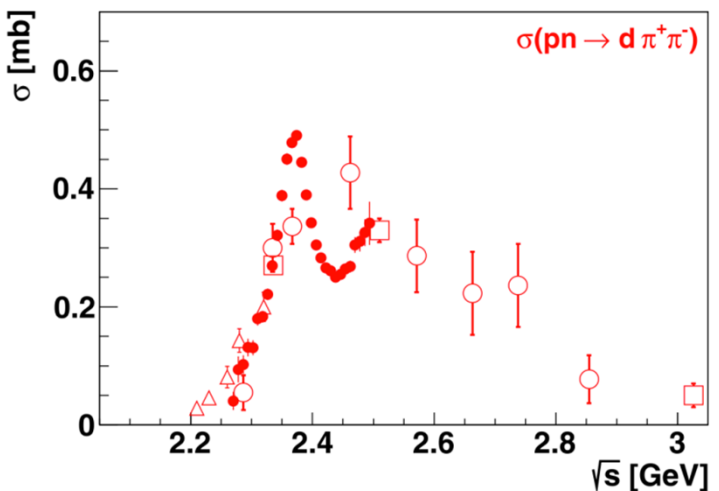
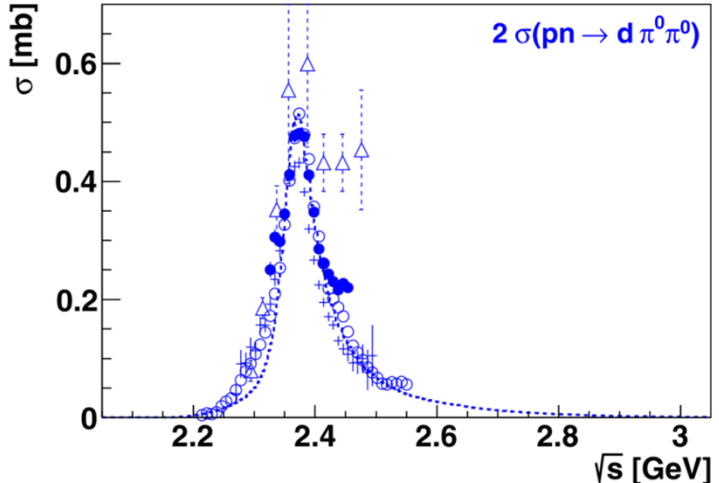
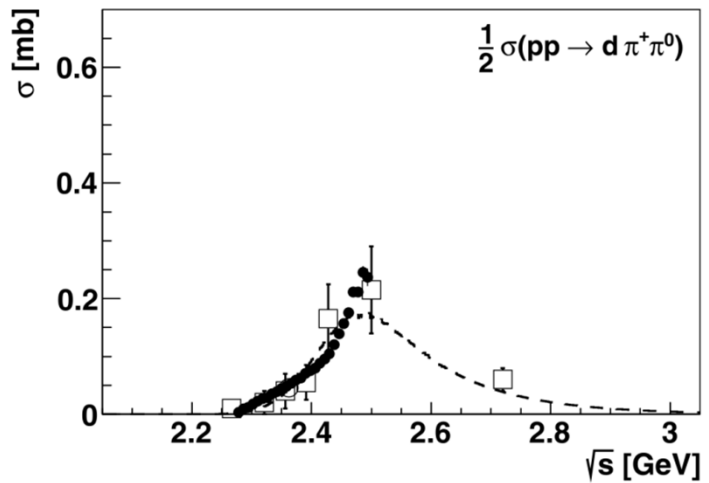
- The WASA@COSY result for $\Delta\Delta$ state
- $M \sim 2370$ MeV
 $= 2m_{\Delta} - 90$ MeV
- $\Gamma \sim 70$ MeV $< 1/3 \Gamma_{\Delta\Delta}$
- $\Delta\Delta$ state interpretation has been disputed*

P. Adlarson et al, Phys Rev Lett 106, 242302 (2011)
...and numerous others since.

* D. V. Bugg, Eur.Phys.J. **A50** 104 (2014)

N Δ WASA@COSY $d^*(2380)$ Resonance

- Evidence for $d^*(2380)$ \mathcal{D}_{03} state in $NN \rightarrow d\pi\pi$ in several isospin channels
- SAID Analysis pole position: $2380(10) - i40(5)$ MeV



P. Adlarson *et al.* (WASA-at-COSY Collaboration), Phys. Rev. C **88**, 055208 (2013).

P. Adlarson *et al.* (WASA-at-COSY & SAID Data Analysis Center), Phys Rev C **90**, 035204 (2014).

$N\Delta$ | A Scenario for $d^*(2380)$ Decay

- Interpretation of WASA/COSY results for reaction $p n \rightarrow d \pi^0 \pi^0$
- Interference mechanism in d^* decay:
 - Sequential decay thru D_{12} ($I J^P = 1 2^+$) state
 - $D_{03} \rightarrow D_{03} + \pi \rightarrow d + (\pi\pi)_0$
 - σ channel ($\pi\pi$ - S wave)
 - $D_{03} \rightarrow d + \sigma \rightarrow d + (\pi\pi)_0$

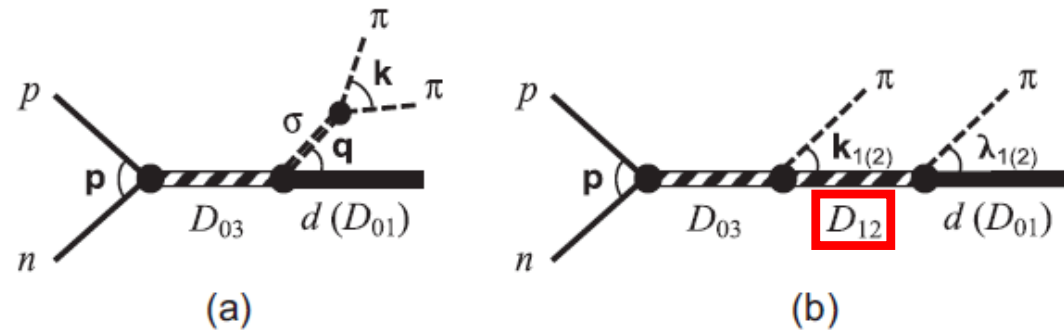


FIG. 1. The leading mechanisms for the reaction $pn \rightarrow d + (\pi\pi)_0$ in the ABC region. The three-momenta in the c.m. frame of two particles are indicated between the respective lines.

N Δ | A Scenario for $d^*(2380)$ Decay

- Interference in decay of d^* ($I J^P = 0 3^+$):

- Sequential decay thru \mathcal{D}_{12} ($I J^P = 1 2^+$) state

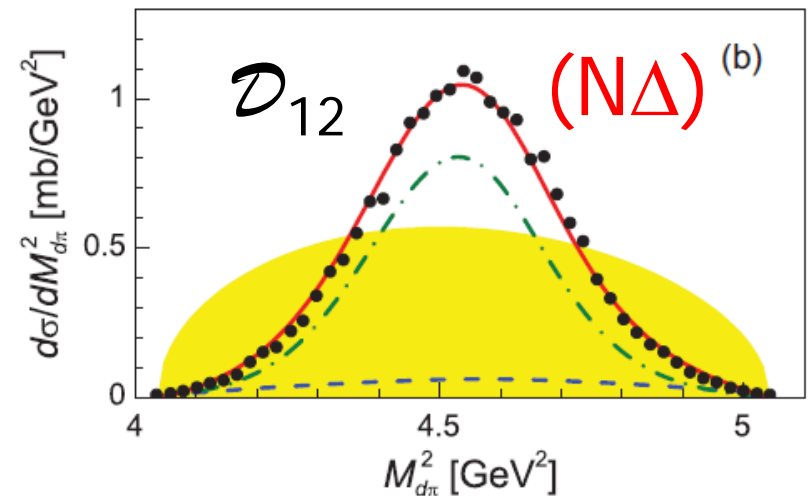
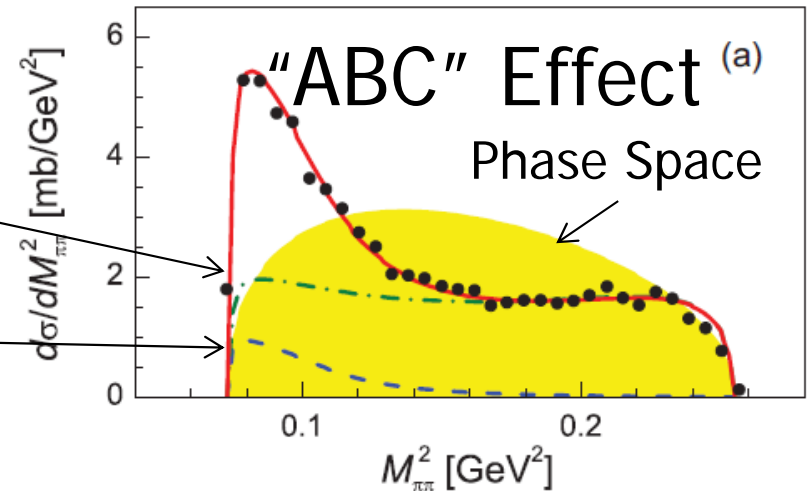
- $\mathcal{D}_{03} \rightarrow \mathcal{D}_{12} + \pi \rightarrow d + (\pi\pi)_0$

- σ channel ($\pi\pi$ - s wave)

- $\mathcal{D}_{03} \rightarrow d + \sigma \rightarrow d + (\pi\pi)_0$

- σ mass and width small compared to PDG

- sign of partial chiral symmetry restoration in dense matter?



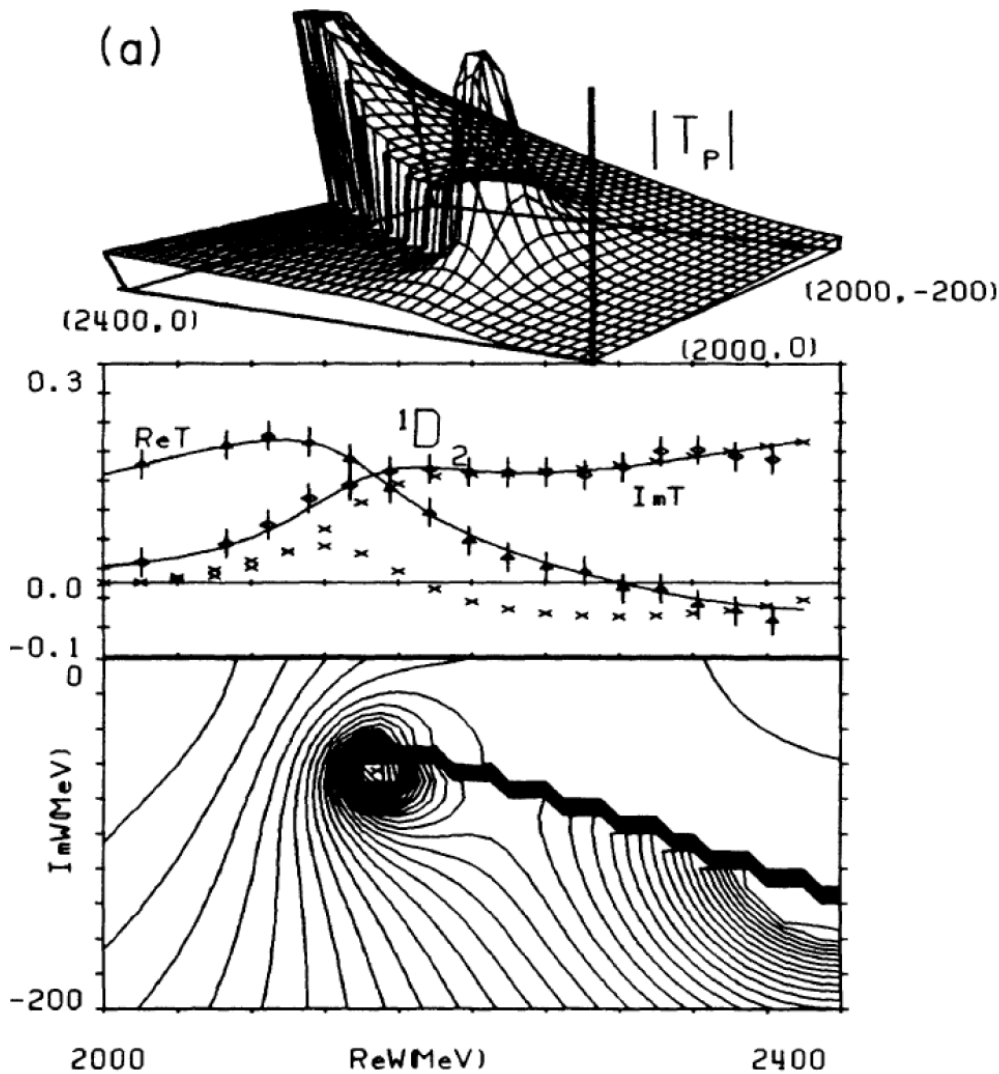
M.N. Platonova, V.I. Kukulín, Phys Rev C **87**, 025202 (2013)

P. Adlarson (Wasa@COSY) *et al.*, Phys. Rev. Lett. 106, 242202 (2011)

N Δ | Quasi-bound states

- What about N Δ ?
 - If a $\Delta\Delta$ (“ \mathcal{D}_{03} ”) state exists, so should N Δ
 - Expect N Δ to have $I J^P = 1 2^+$ (“ \mathcal{D}_{12} ”)

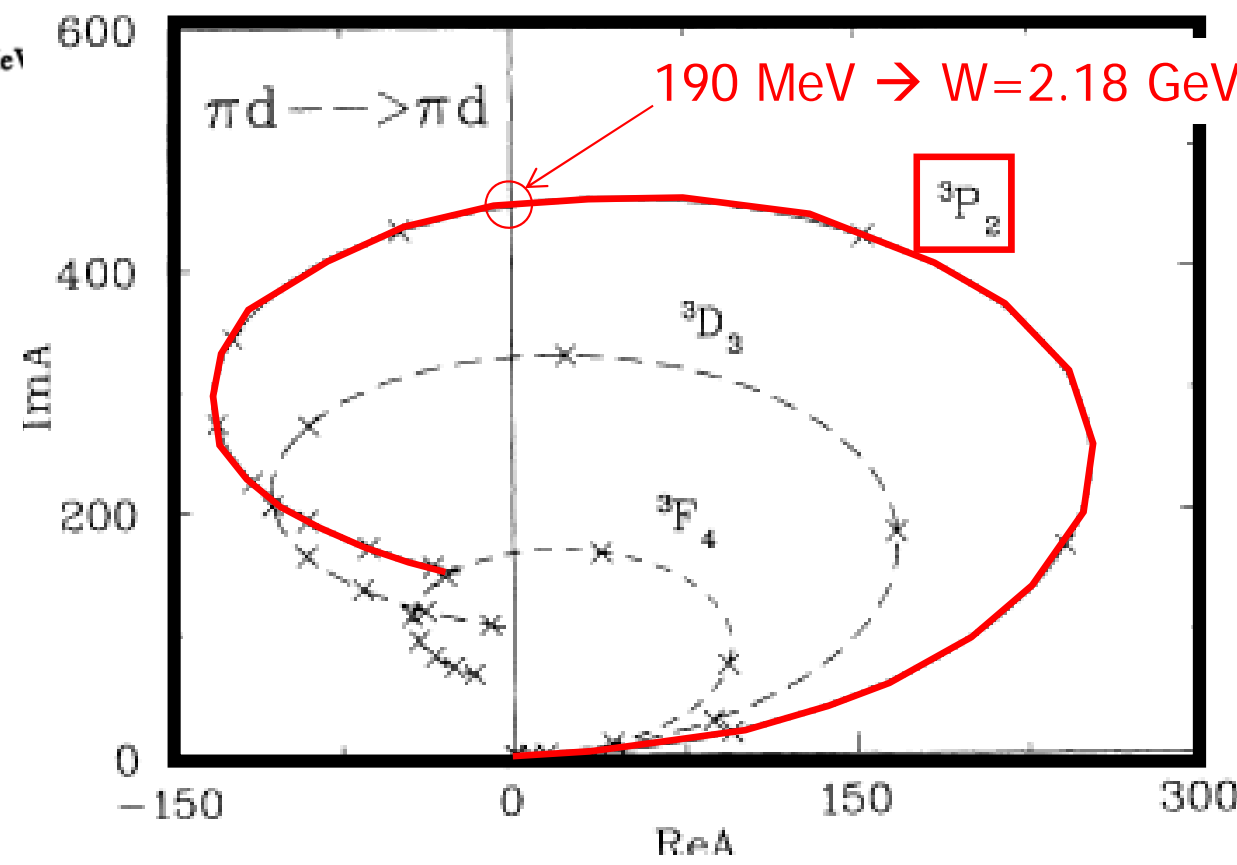
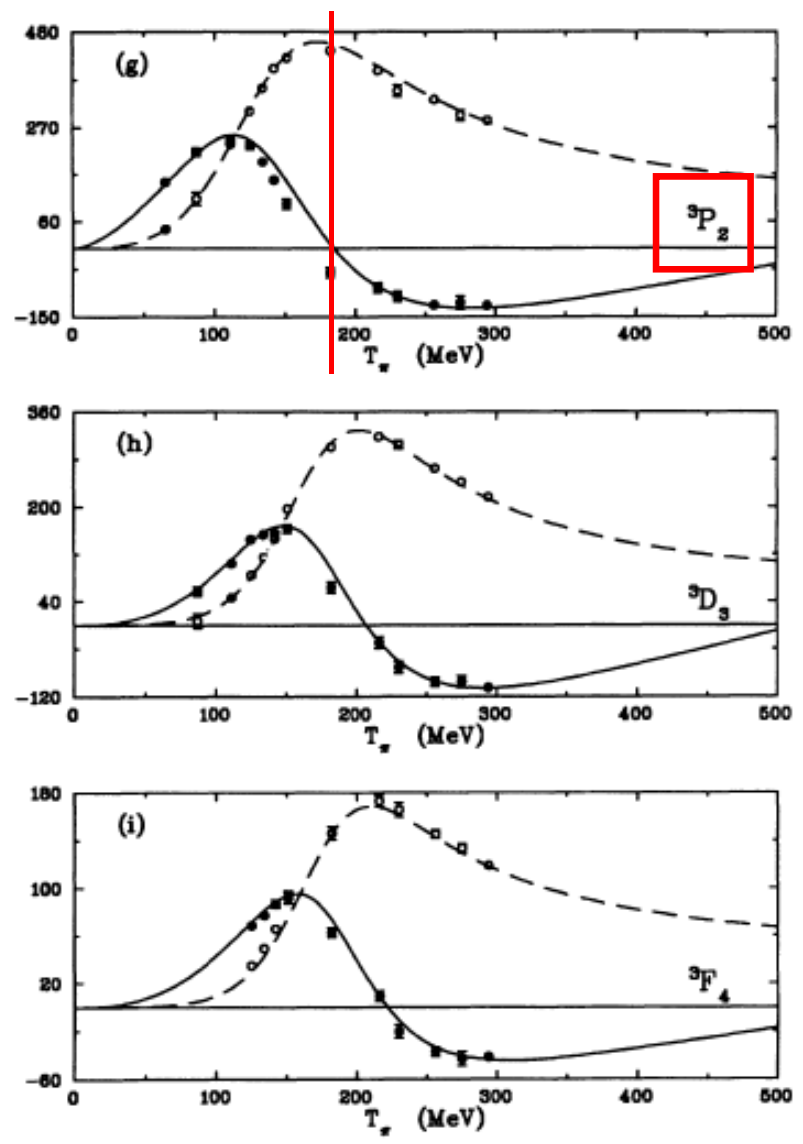
$N\Delta$ | pp Elastic Scattering



- Partial Wave Analysis
- $1D_2$ wave in pp elastic scattering: structure at $2148 - i63$ MeV
- Most prominent "resonance pole" seen in SAID analysis
- Textbook exercise: If an $N\Delta$ quasi-bound state exists, it can decay to pp ONLY if $J_{N\Delta}^P = 2^+$

N Δ | $\pi d \rightarrow \pi d$ Elastic PWA

ANALYSIS OF πd ELASTIC SCATTERING DATA TO 500 MeV

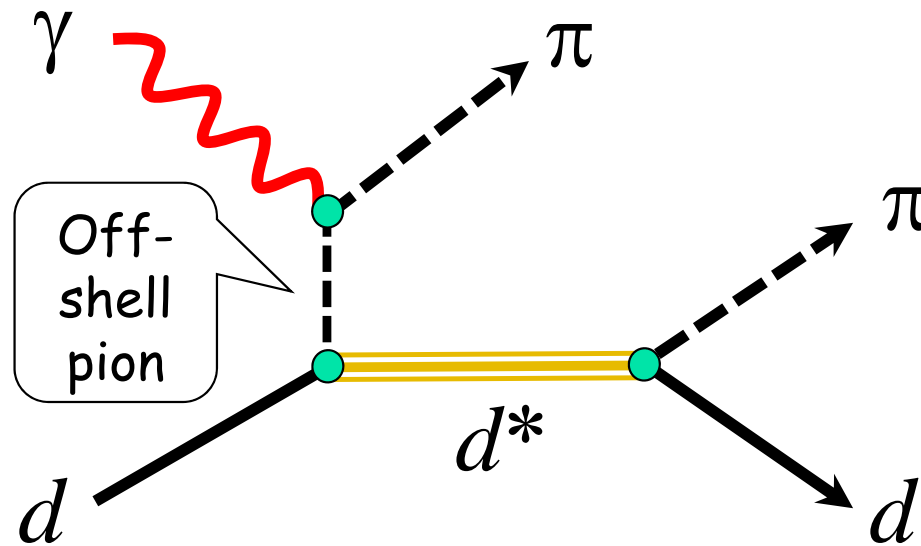


- 3P_2 wave in πd elastic scattering is most prominent
- SAID analysis: "resonance-like" behavior in several partial waves

$N\Delta$ | S-matrix poles for $N\Delta$ (\mathcal{D}_{12})

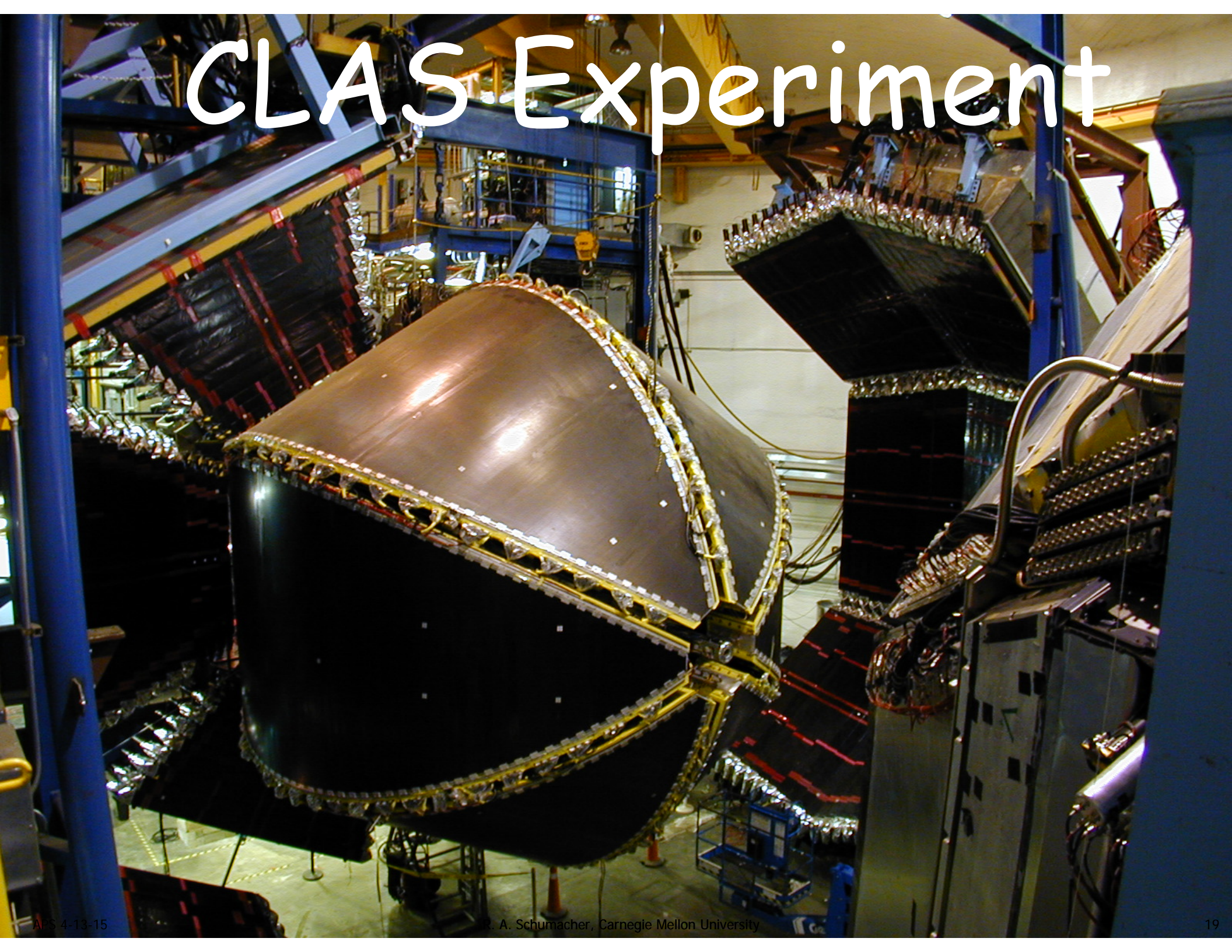
Pole Position \mathcal{D}_{12} (MeV)	Model Approach	Ref.
2147 – i60	Faddeev model	A. Gal, H. Garcilazo, Nucl. Phys. A928 73 (2014)
2148 – i63	$pp(^1D_2) \leftrightarrow \pi d(^3P_2)$ coupled channels	R.A. Arndt, J.S. Hyslop, L.D. Roper, Phys. Rev. D 35 (1987) 128.
2144 – i55	$pp(^1D_2) \leftrightarrow \pi d(^3P_2)$ coupled channels	N. Hoshizaki, Phys. Rev. C 45 (1992), R1424, Prog. Theor. Phys. 89 (1993) 563.

Photoproduction Scenario



- Resembles πd elastic scattering but with an off-shell pion.
 - Suppose it to be dominant at small $-t$

CLAS Experiment

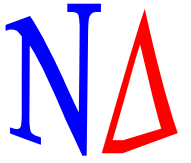


$N\Delta$ | What can CLAS see?

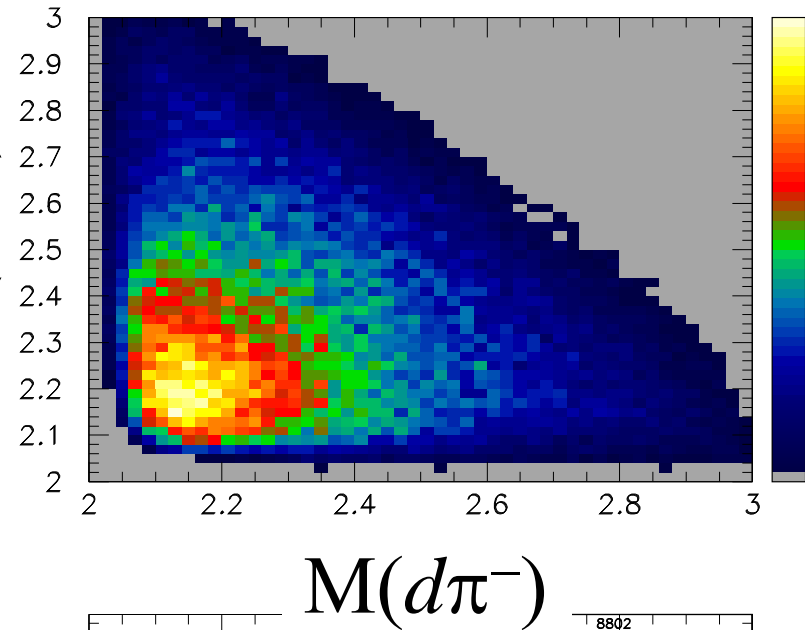
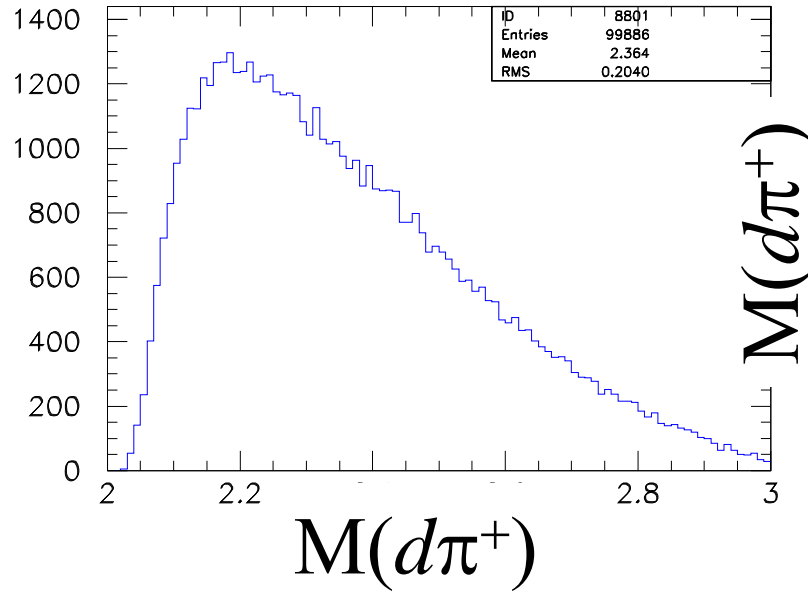
- Photons on a deuteron target
 - g_{10}, g_{13}, g_{14} data sets
- Spin-1 photon & spin-1 deuteron:
 - $\vec{1} + \vec{1} \rightarrow \vec{J} = \vec{0}, \vec{1}, \vec{2}$ in S wave, is favorable
- Isospin $I = \{0, 1\} + 0 \rightarrow 0, 1$ allowed
- We looked for both $N\Delta$ and $\Delta\Delta$ structures
- $\gamma d \rightarrow p p \pi^-$ - messy mix of partial waves
- $\gamma d \rightarrow d \pi^+ \pi^-$ - coherent exclusive production: clean!

N Δ | Parametric Monte Carlo

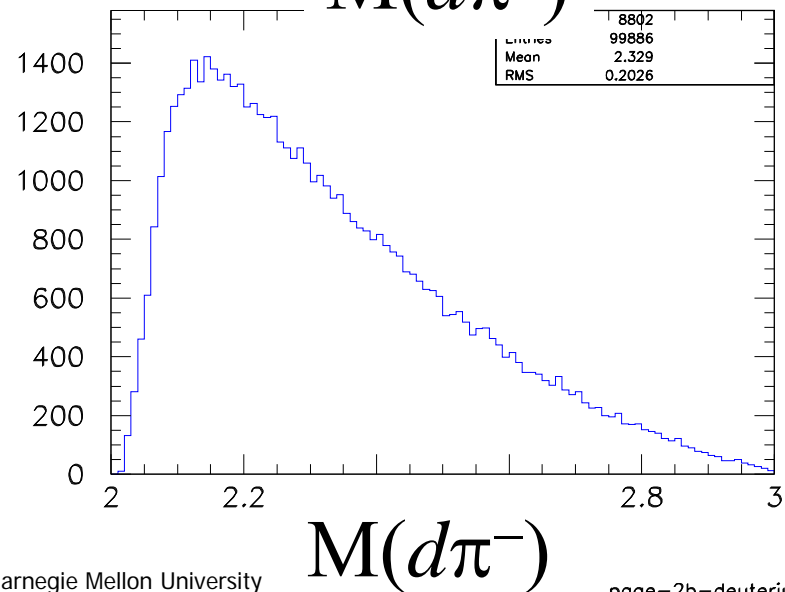
- $\gamma d \rightarrow \{d \pi\} \pi$ - signal channel
 - $\gamma d \rightarrow d \rho$ - main background
 - $\gamma d \rightarrow d \pi \pi$ - phase space background
-
- Model the run conditions:
 - Bremsstrahlung photon beam
 - Reverse CLAS torus field
 - Assume t -channel dominance (slope 2 GeV^2)

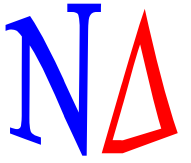


Parametric Monte Carlo

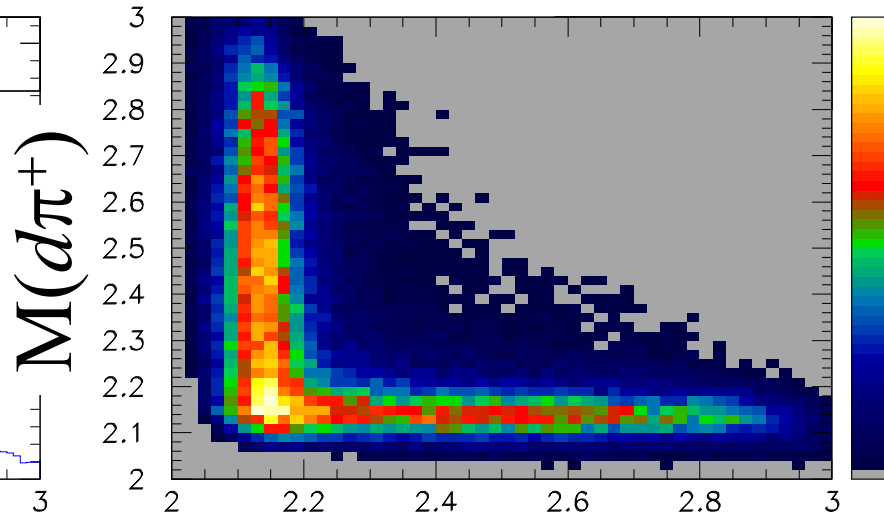
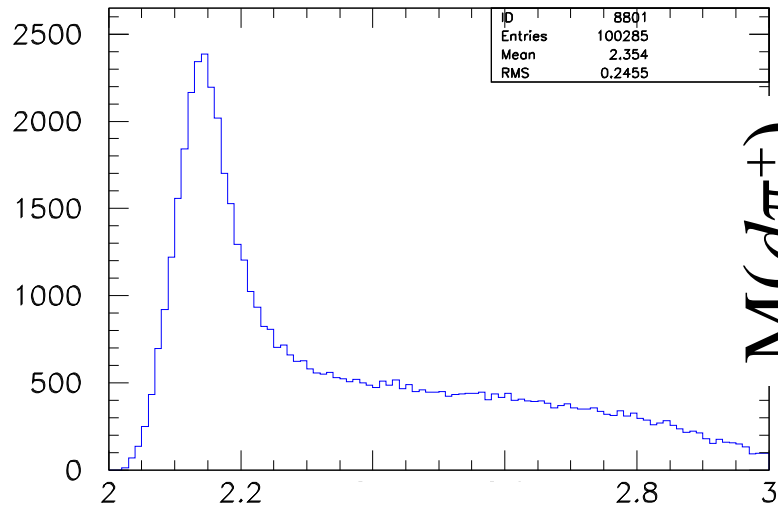


- $\gamma d \rightarrow d \pi^+ \pi^-$
phase space
background

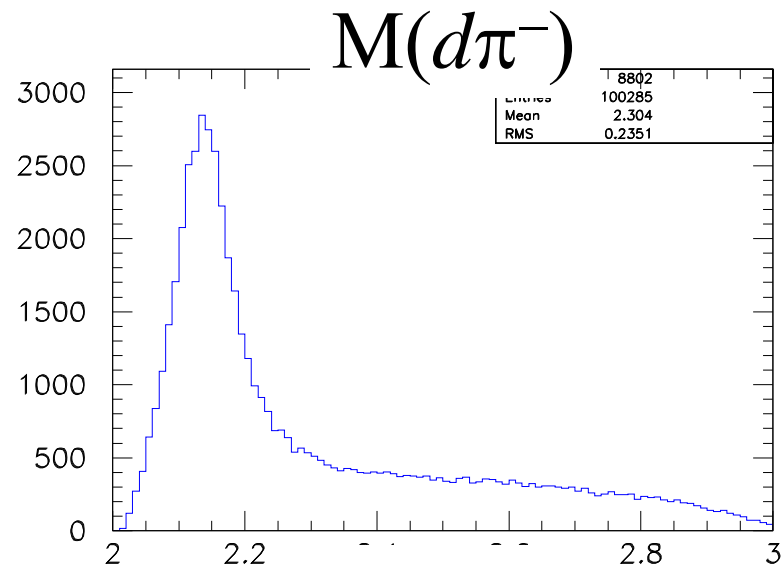


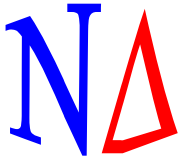


Parametric Monte Carlo

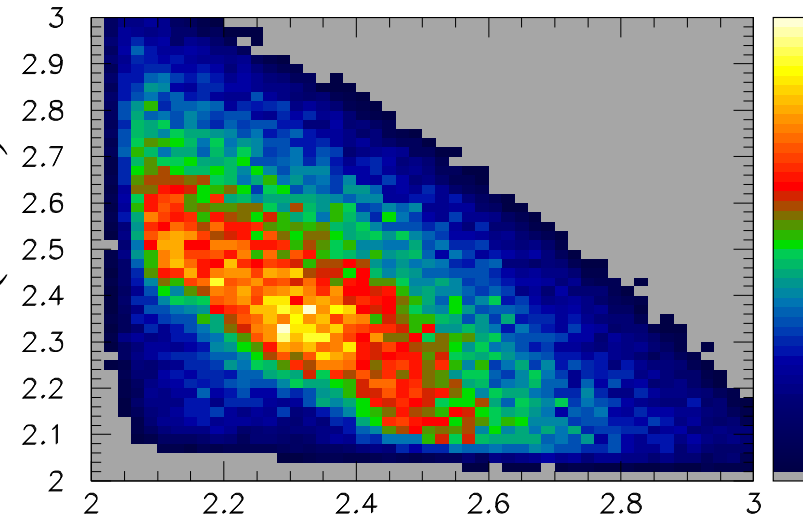
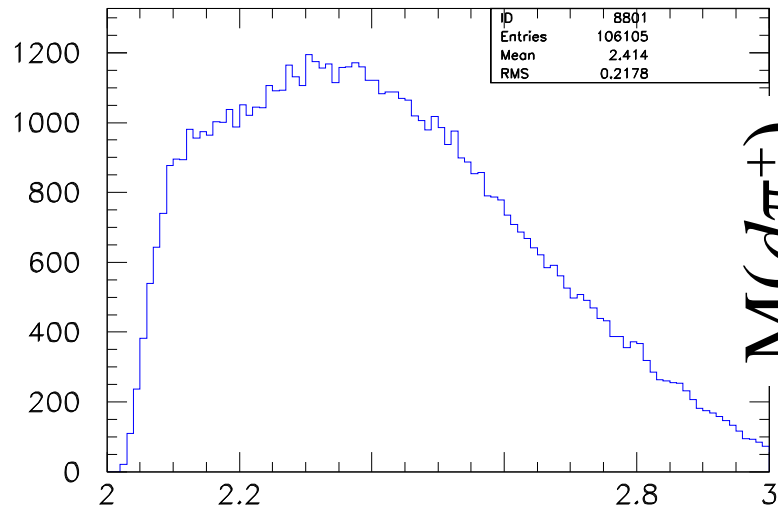


- $\gamma d \rightarrow \{d \pi^\pm\} \pi^\mp$
signal events

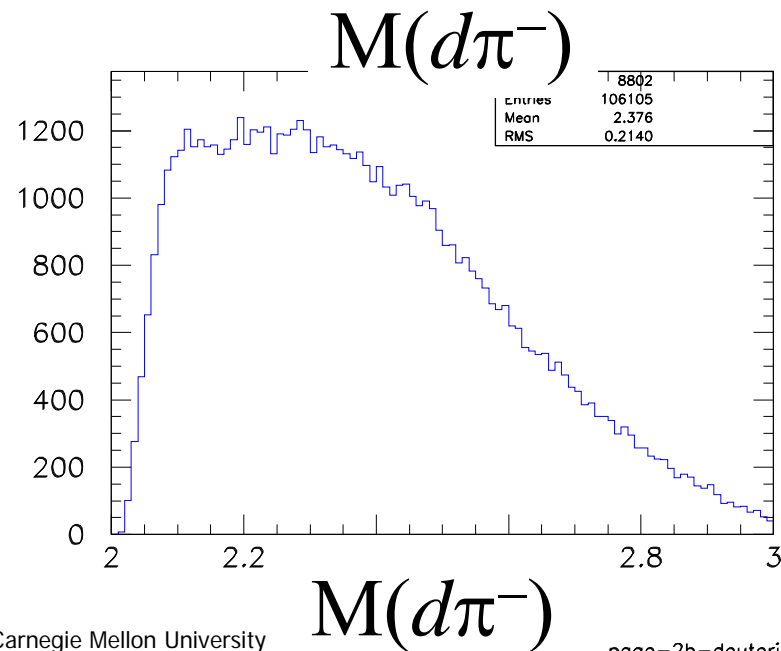


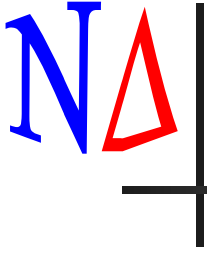


Parametric Monte Carlo



- $\gamma d \rightarrow d \pi^+ \pi^-$
 ρ background



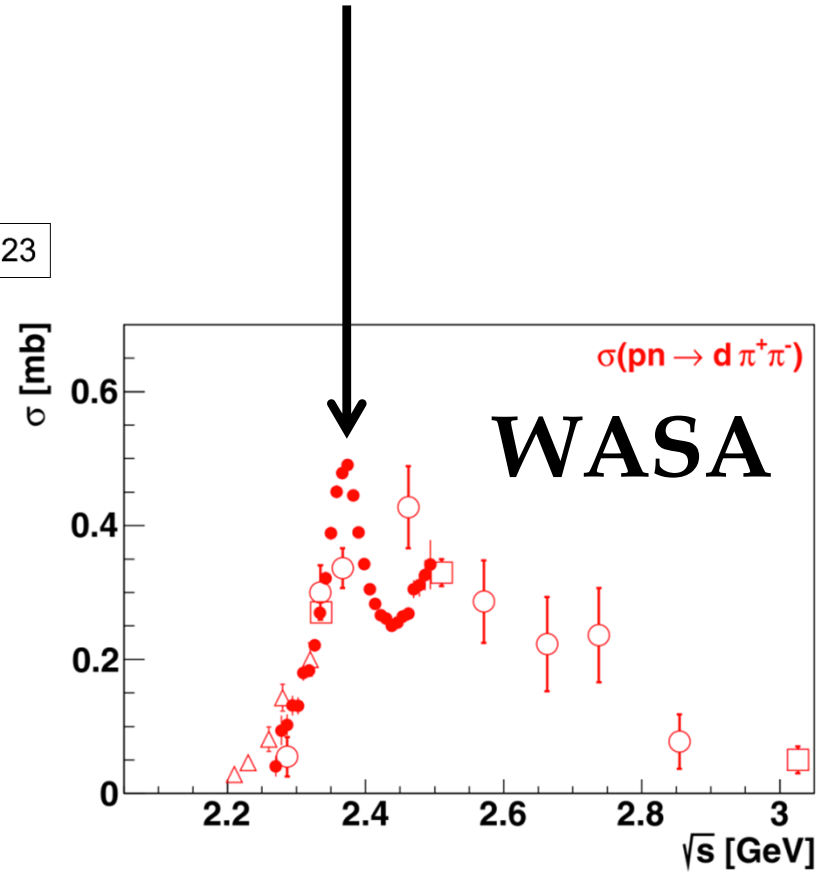
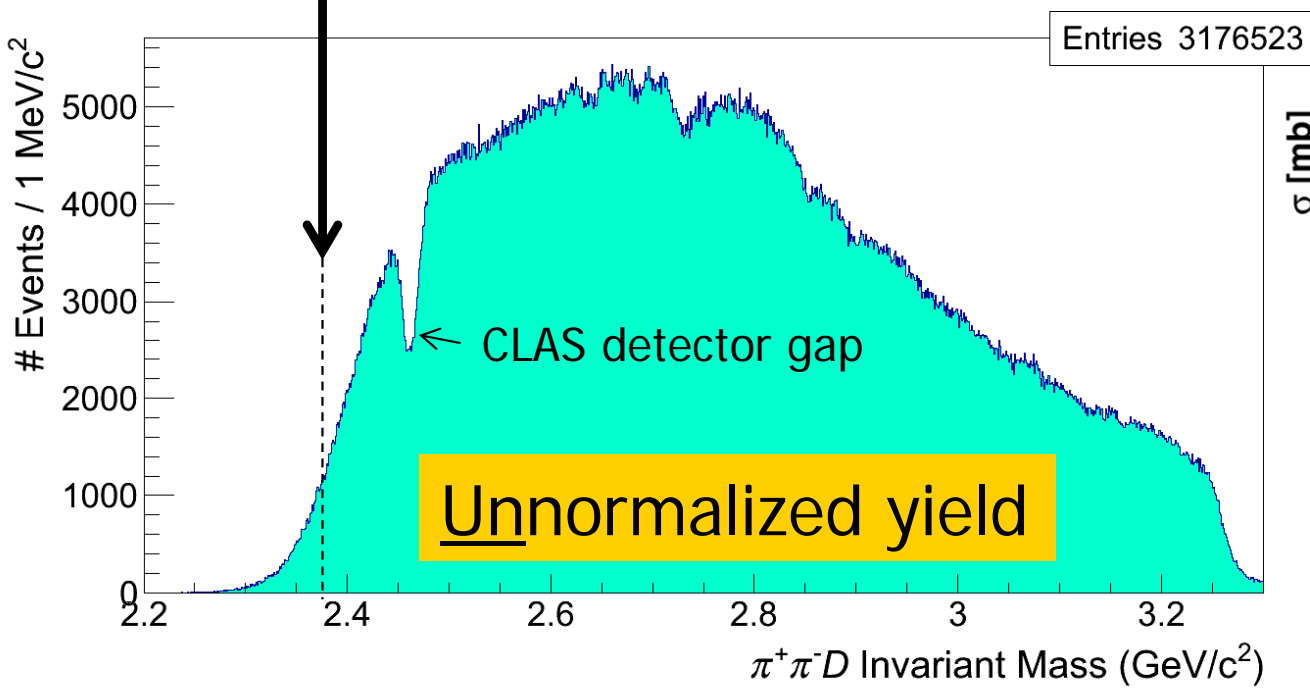


- Preliminary CLAS data showing
 - No sign of a “ $\Delta\Delta$ ” signal
 - Evidence for ρ background
 - Evidence for a “ $N\Delta$ ” signal

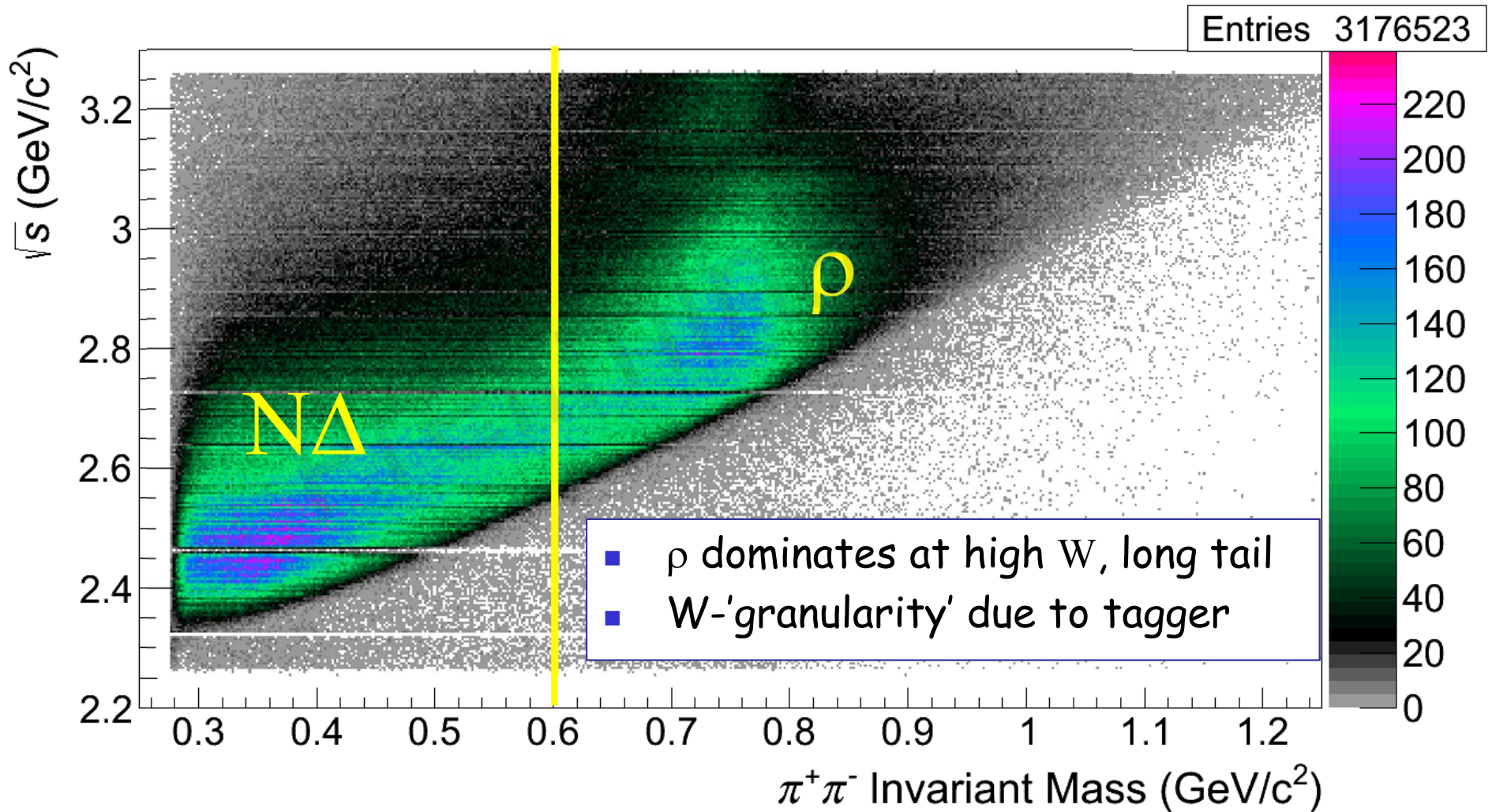
$N\Delta$ | $d\pi^+\pi^-$ Invariant Mass

- Gash at $W = 2.46 \text{ GeV}/c^2$: known gap in CLAS coverage
- No $\Delta\Delta$ visible in CLAS/g13 (maybe not formed in γd)
- Recall WASA@COSY claims $\Delta\Delta$ at $W = 2.37 \text{ GeV}/c^2$ in $pn \rightarrow d\pi^+\pi^-$

No hint of a " $\Delta\Delta$ " bump!

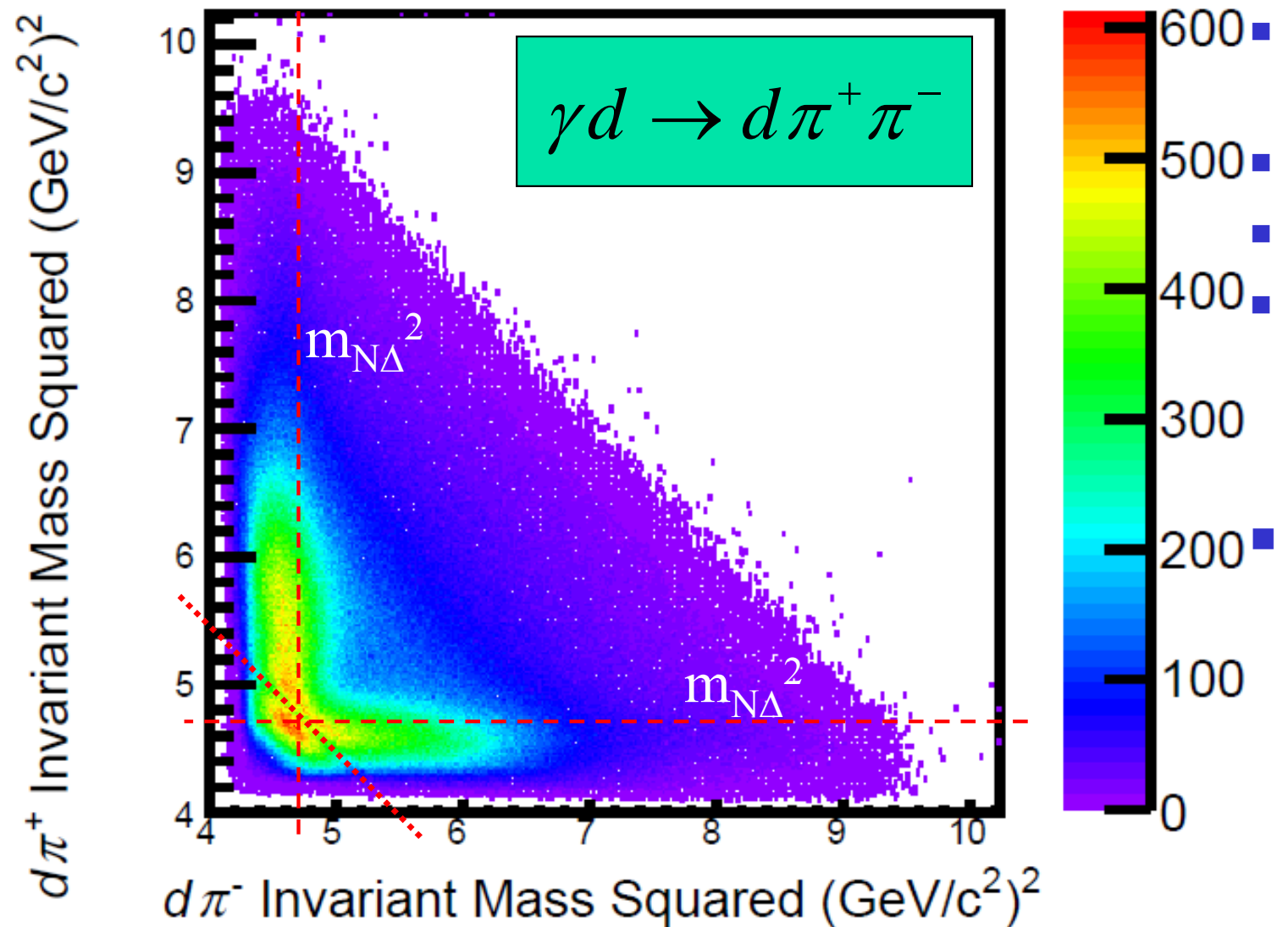


$N\Delta$ | $\gamma d \rightarrow d \rho, \rho \rightarrow \pi^+ \pi^-$ background



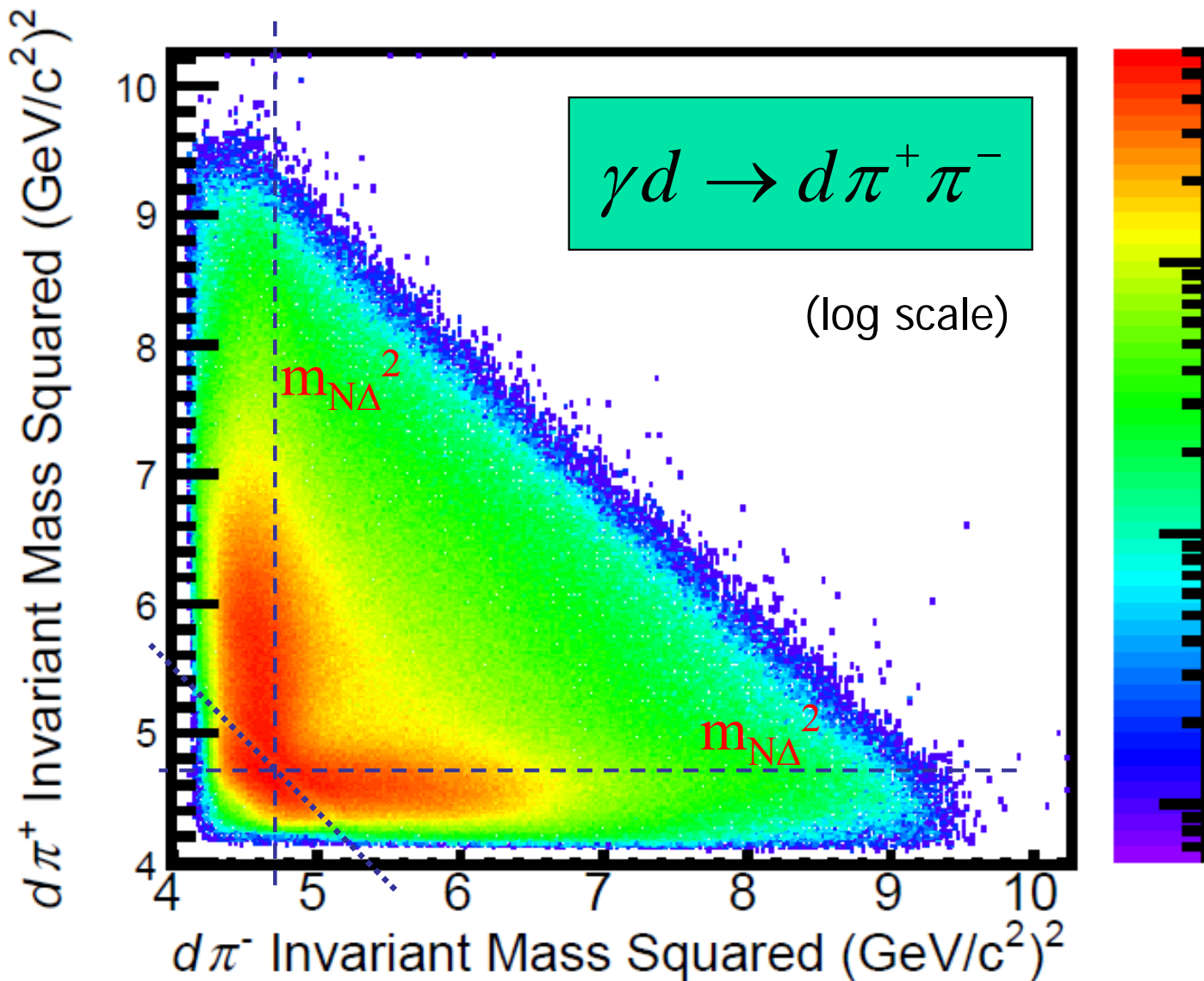
N Δ

Dalitz Plot: $d\pi^+$ vs. $d\pi^-$

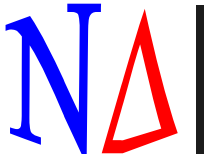


- 600 ■ Acceptance-corrected CLAS (g13) data
- 500 ■ $-0.75 < \cos\theta_{\pi^\pm} < 0.94$
- 400 ■ $2.45 < W < 3.15$ GeV
- 300 ■ $W \sim \text{constant on diag.}$
- 200 ■ ■ Gap at $W=2.45$ GeV due to missing tagger channel
- 100 ■ **Clear preference for $d\pi^\pm$ correlation near the $N\Delta$ mass!**
- 0 ■

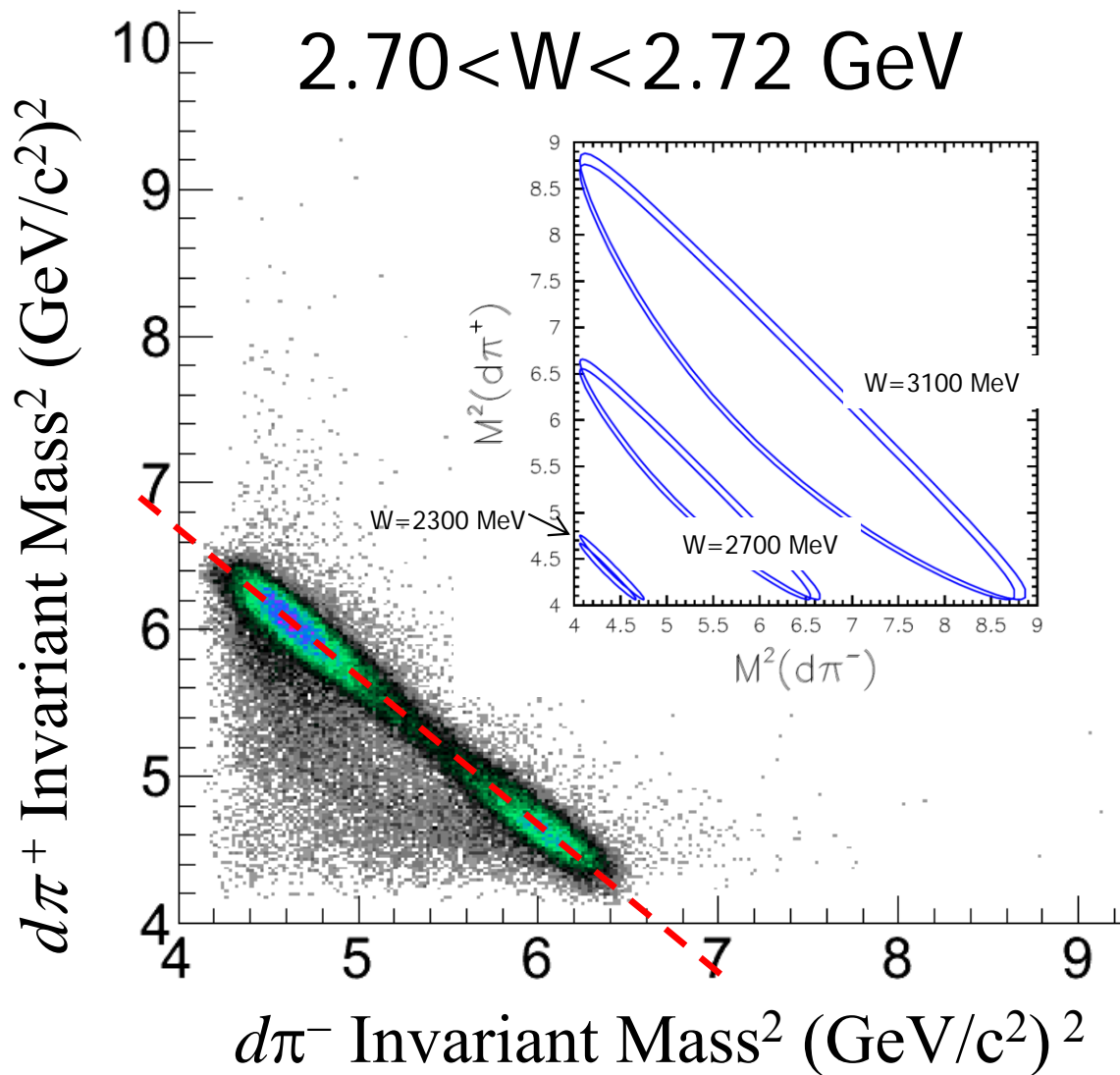
$N\Delta$ | Dalitz Plot: $d\pi^+$ vs. $d\pi^-$



- Acceptance-corrected CLAS (g13) data
- $-0.75 < \cos\theta_{\pi^\pm} < 0.94$
- $2.45 < W < 3.15$ GeV
- $W \sim \text{constant}$ on diag.
 - Gap at $W=2.45$ GeV due to missing tagger channel
- **Clear preference for $d\pi^\pm$ correlation near the $N\Delta$ mass!**



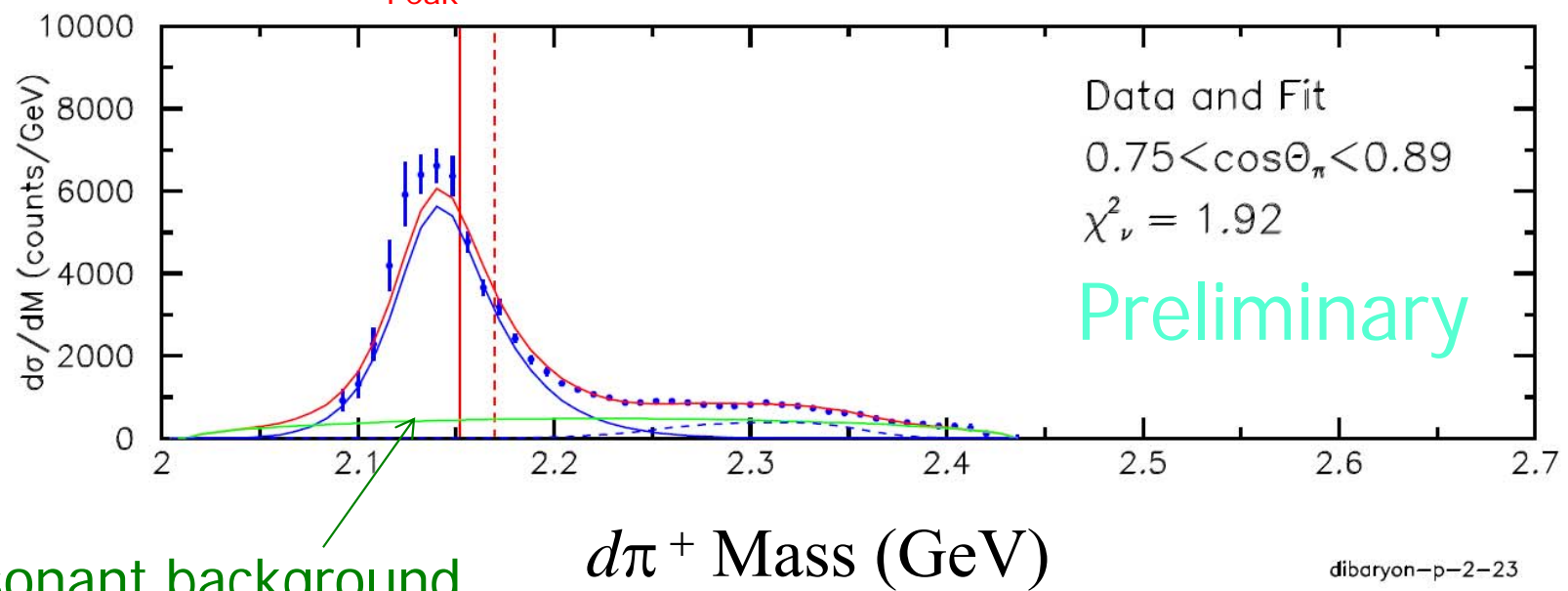
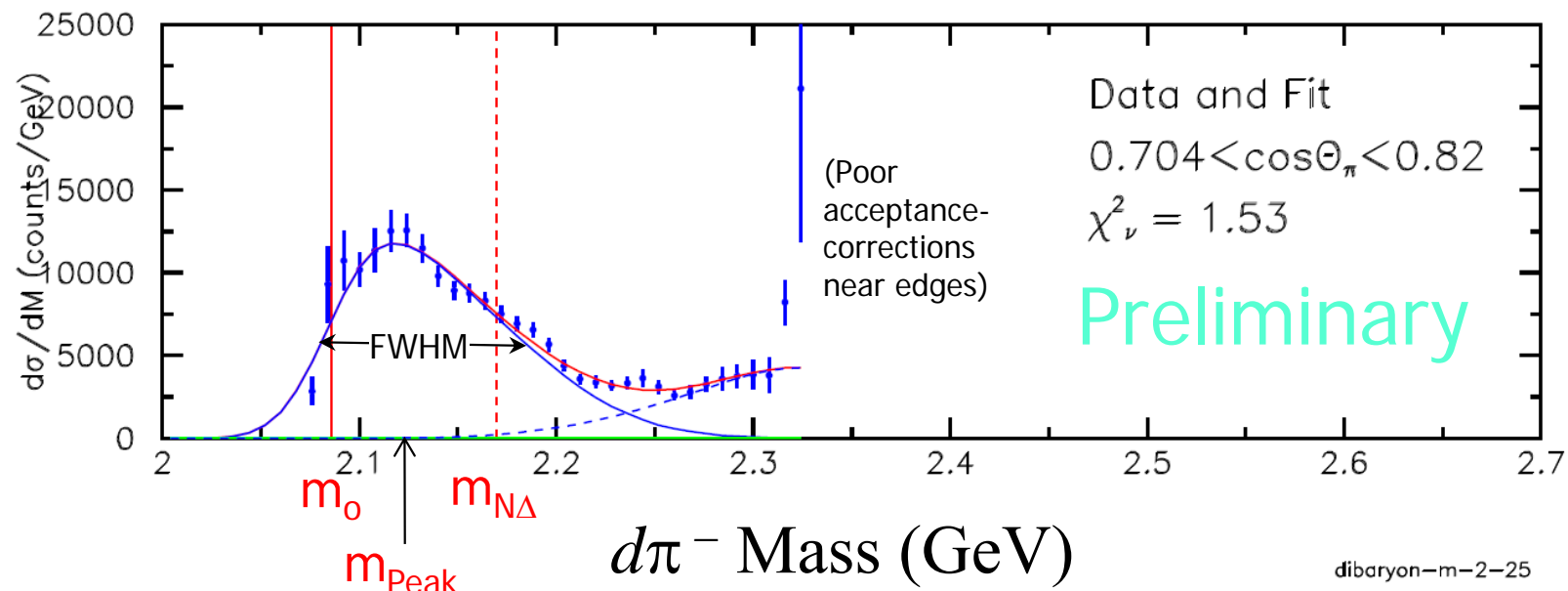
Fit to Resonance-like Shapes



- Use narrow data slices in $W = \sqrt{s}$
- Assume a Breit-Wigner line shape
- Let $d\pi$ system decay to $N\Delta$ (L=0), $d\pi$ (L=1), and NN (L=2)
- ρ not cut away; model as P.S. background
- Incoherent amplitudes
- Following fits are prelude to PWA analysis

$N\Delta$

$\gamma d \rightarrow (d\pi) \pi \quad 2.55 < W < 2.60 \text{ GeV}$



Non-resonant background

N Δ | Fit to Resonance-like Shapes

$$\frac{d\sigma}{dm} \sim \left\{ \frac{1}{p_{\gamma d}^{cm}} \right\} \frac{m_0^2 \Gamma_i \Gamma_f}{(m_0^2 - m^2)^2 + m_0^2 (\Gamma_{N\Delta}^{L=0} + \Gamma_{\pi d}^{L=1} + \Gamma_{pp}^{L=2})^2}$$

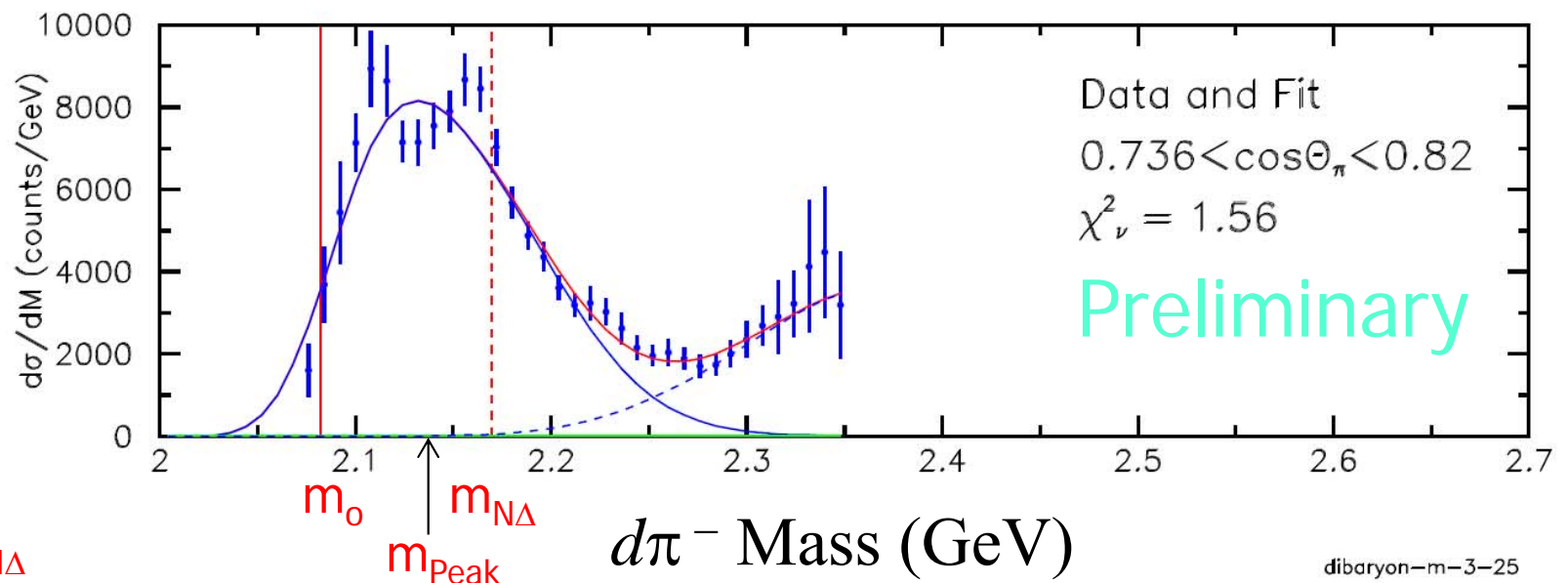
Let the fit "choose"
the preferred shape
from L=0,1,2

$$\Gamma_{pp}^{L=2} = \alpha_{pp} \Gamma_0 \left(\frac{q^{pp}}{q_0^{pp}} \right)^{2L+1=5} \left(\frac{m}{m_0} \right) (B'_{L=2}(q, q_0))^2$$

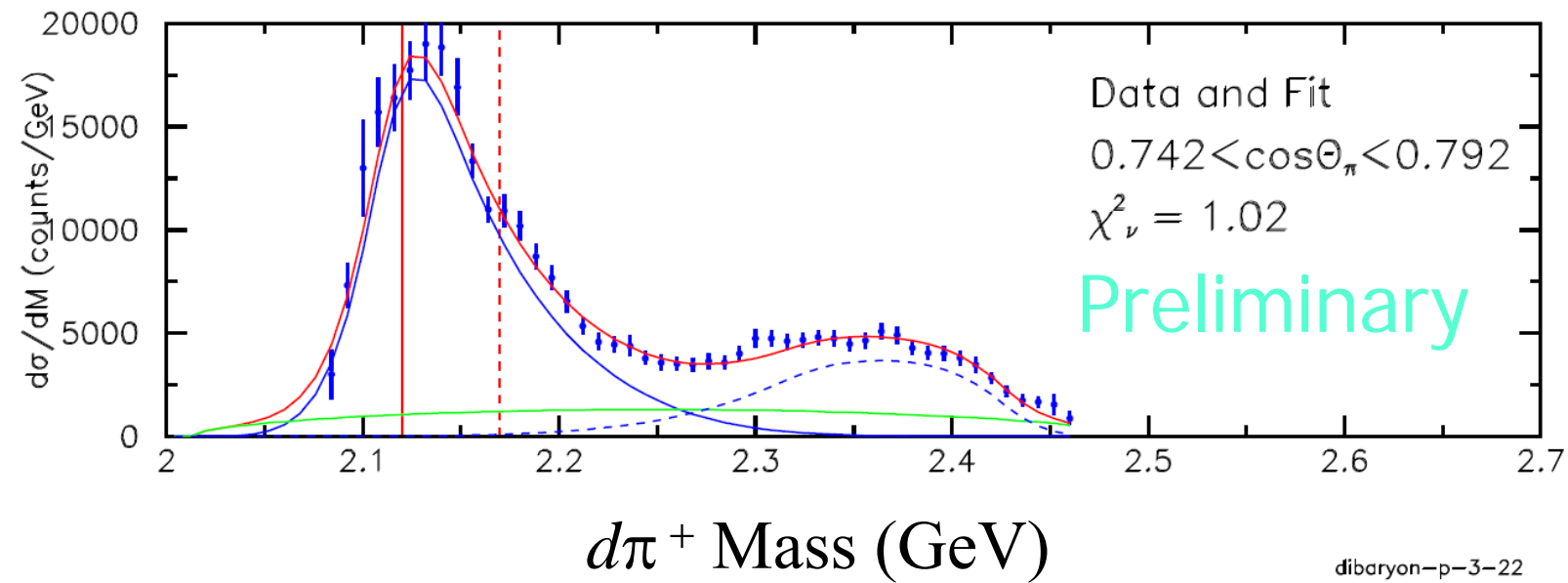
$$\Gamma_{\pi d}^{L=1} = \alpha_{\pi d} \Gamma_0 \left(\frac{q^{\pi d}}{q_0^{\pi d}} \right)^{2L+1=3} \left(\frac{m}{m_0} \right) (B'_{L=1}(q, q_0))^2 = \Gamma_f \hat{=} \Gamma_i$$

$$\Gamma_{N\Delta}^{L=0} = \alpha_{N\Delta} \Gamma_0 \left(\frac{q^{N\Delta}}{q_0^{N\Delta}} \right)^{2L+1=1} \left(\frac{m}{m_0} \right) (B'_{L=0}(q, q_0))^2 \xrightarrow{\text{Non-relativistic}} \alpha_{N\Delta} \Gamma_0 \left(\frac{m}{m_0} \right) (1)$$

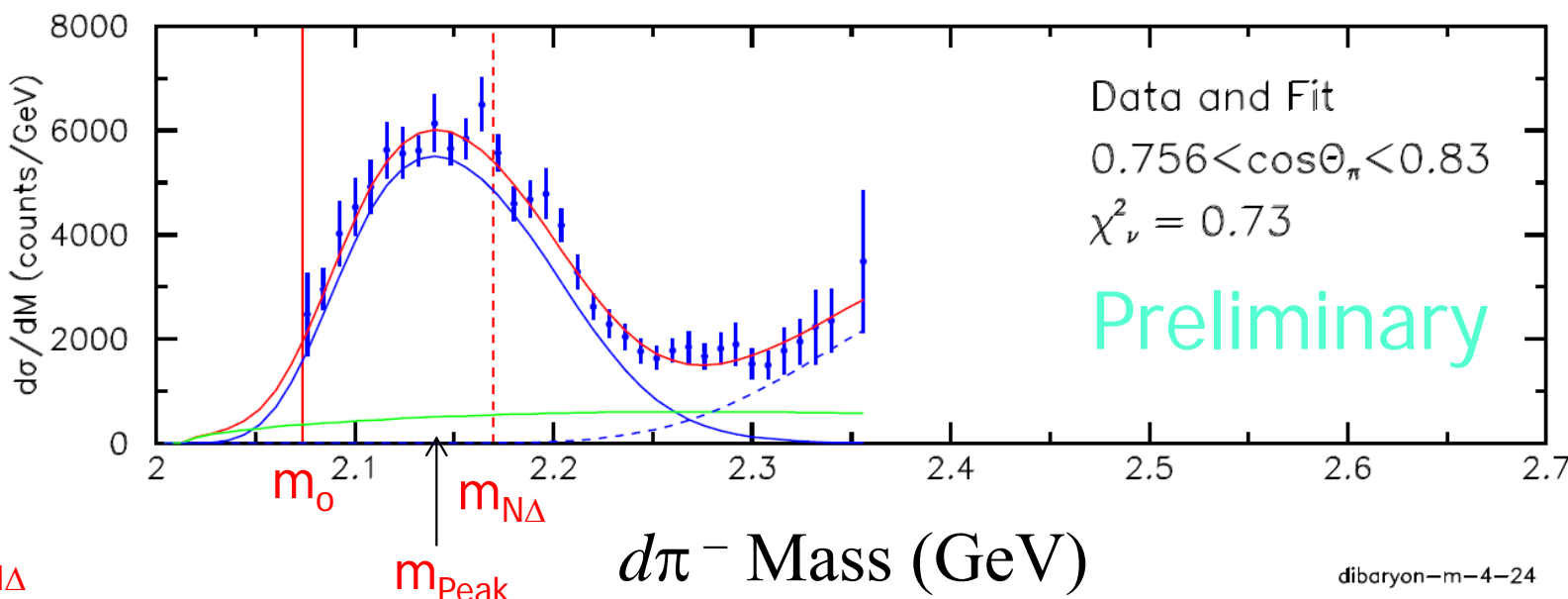
$N\Delta$ | $\gamma d \rightarrow (d\pi) \pi$ $2.60 < W < 2.65$ GeV



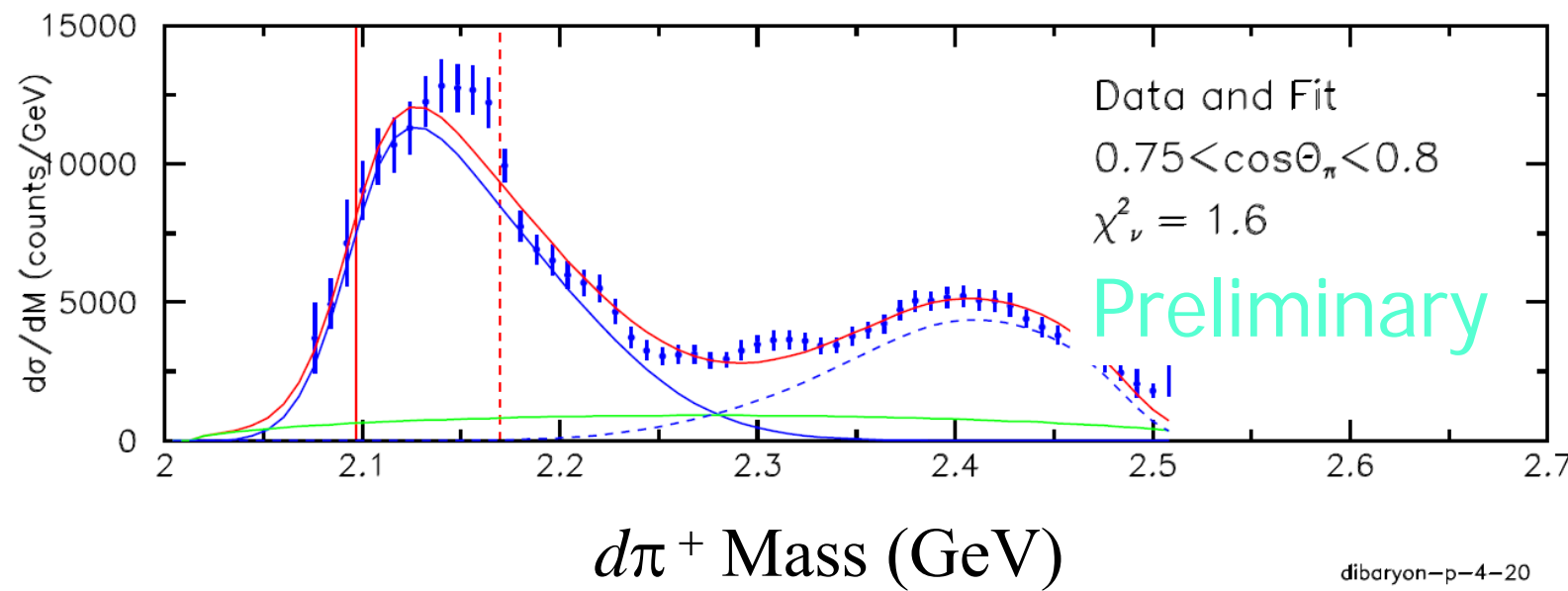
Evidently,
 $m_{Peak} < m_{N\Delta}$



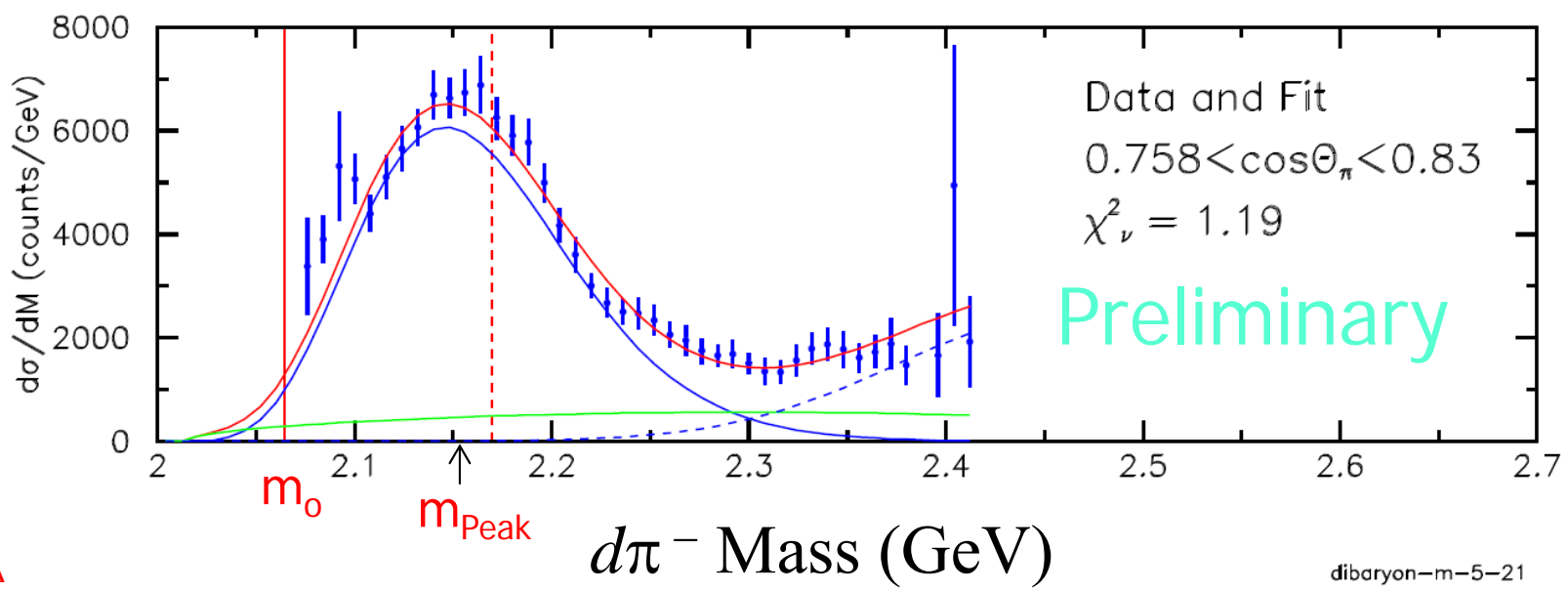
$N\Delta$ | $\gamma d \rightarrow (d\pi) \pi$ $2.65 < W < 2.70$ GeV



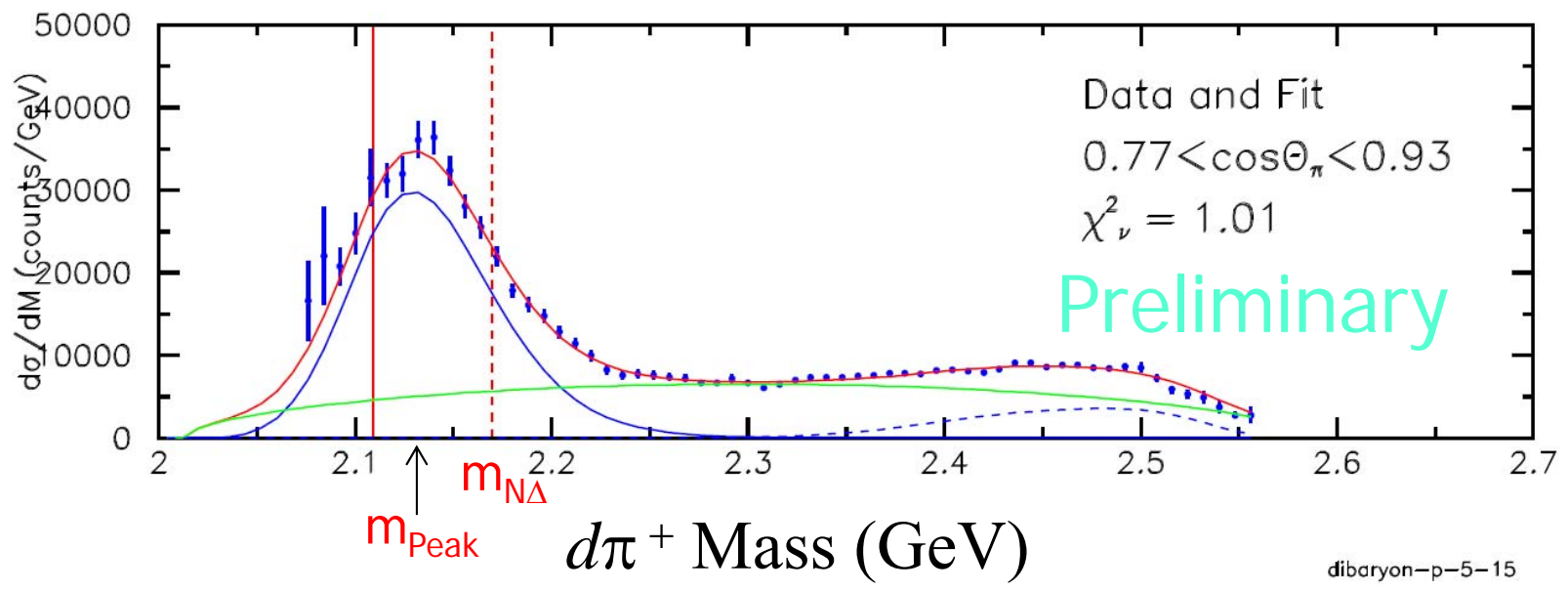
Evidently,
 $m_{Peak} < m_{N\Delta}$



$N\Delta$ | $\gamma d \rightarrow (d\pi) \pi$ $2.70 < W < 2.75$ GeV



Evidently,
 $m_{\text{Peak}} < m_{N\Delta}$

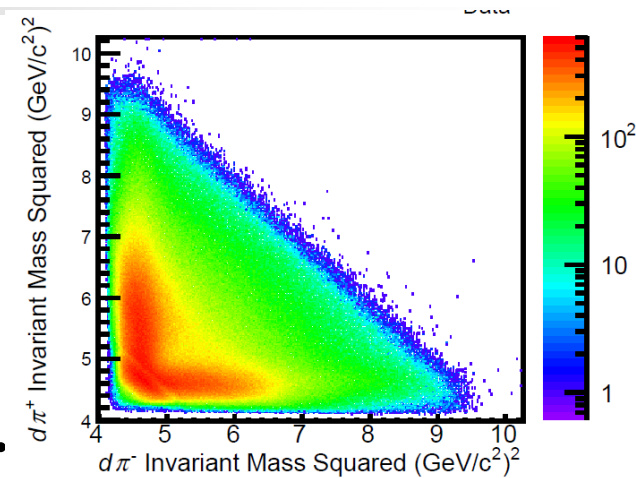


N Δ Observations

- Peaks are all below the N Δ centroid, but widths are not identical: $\cos \theta_\pi$ dependent
- Very preliminary result:
 - $m_{\text{peak}} = 2115 \pm 10 \text{ MeV}/c^2$
 - $\text{FWHM} = 125 \pm 25 \text{ MeV}$
- We have remaining acceptance issues near high and low edges
- Fits "choose" non-relativistic BW line shapes with $\Gamma_{\pi d}^{L=1} \hat{=} \Gamma_i$ numerator only few %
L = 1, 2 decay branches denominator

N Δ | Summary/Conclusion

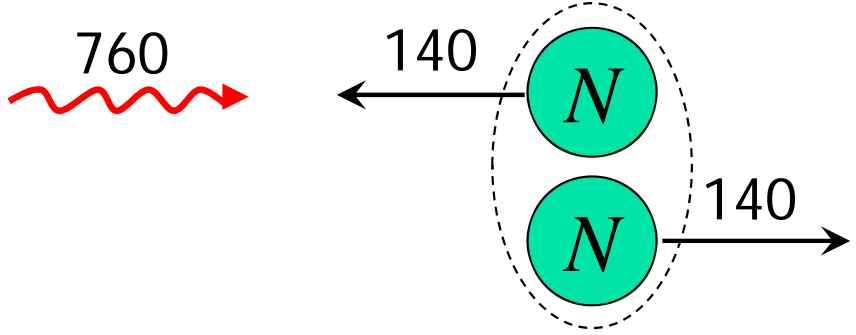
- Big $\pi^\pm d$ signal seen in CLAS photo-production data, peaking below the N Δ mass.
 - Strongest at forward pion angle.
- Resonance mass and width depends on line-shape model, ρ treatment, amplitude interferences...
- We are NOT now claiming that this $d\pi$ -system bump is necessarily the expected resonant \mathcal{D}_{12} state... but it could be. Caveats:
 - Final/initial state interactions, other dynamics...
 - Scattering matrix poles vs. peaks in spectra...



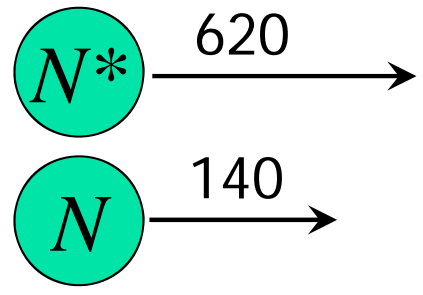
N Δ | Supplemental slides

N Δ | Why not Deuteron Breakup?

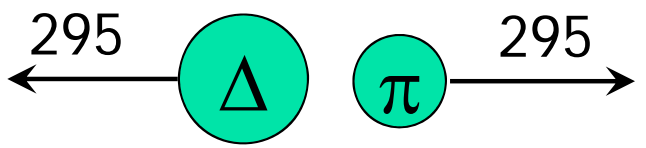
- Would the system survive on the way to forming an N Δ State?
 - Fermi motion helps!
- Let $\gamma d \rightarrow NN^*(1520) \rightarrow N\Delta\pi$, <170 MeV/c Fermi motion, and let N^* decay along z-axis



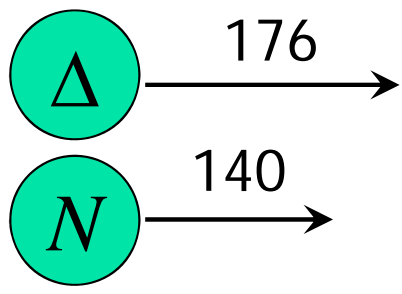
1) $\gamma N \rightarrow N^*$ Lab Frame



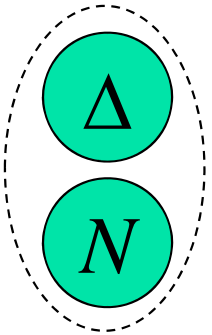
2) N^*N Lab Frame



3) $N^*(1520)$ Rest Frame



4) ΔN Lab Frame



Relative Kinetic E \cong 0. MeV

5) ΔN c.m. Frame

$N\Delta$ Theory Approaches for $\Delta\Delta$

- Group theory predicts both states $I J^P = 0 3^+$ (D_{03} a.k.a. d^*) and $I J^P = 3 0^+$ (D_{30})
- Hidden-color configurations make both bound, but D_{03} more so:
 - Chiral-quark model
 - 2393 vs. 2440 MeV
 - Quark Delocalization Color Screening Model
 - 2357 vs. 2423 MeV

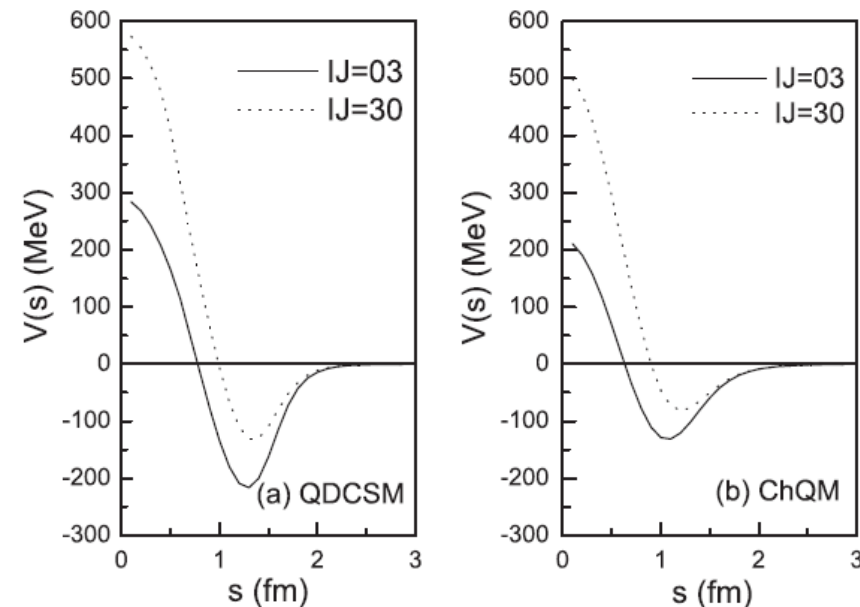


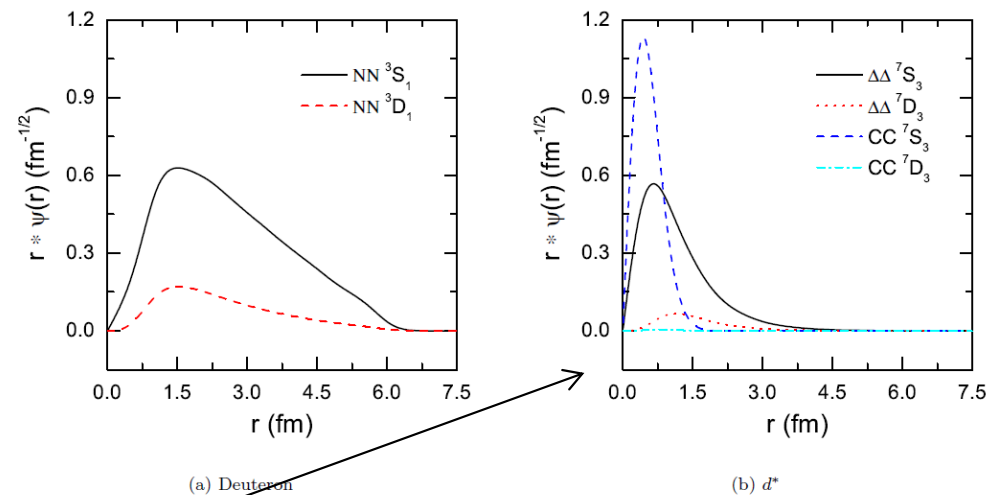
FIG. 1. The potentials of S -wave $\Delta\Delta$ for $IJ^P = 03^+$ and $IJ^P = 30^+$ cases within two quark models.

H. Huang, J. Ping, F. Wang, Phys Rev C 89, 034001 (2014)

N Δ | Theory Approaches for $\Delta\Delta$

- Most exotic interpretation for d^* ($I J^P = 0 3^+$): a "hexa-quark" dominated structure
- Chiral Quark Model with Resonating Group Method

- Mass 2.38 to 2.42 GeV
- 2/3 hidden color configuration (CC)



- RMS size 0.76 - 0.88 fm (!)
- "Narrow" (~ 70 MeV), since CC component does not break up directly

CLAS Experiment

- Photoproduction:
 - Targets: unpolarized LH_2 , polarized p, & HD-ice
 - Beams: unpolarized, circular, linear, to $\sim 5 \text{ GeV}$
 - Reconstructed $\text{K}^+p\pi^-(\pi^0)$ or $\text{K}^+\pi^+\pi^-(n)$
 - 20×10^9 triggers $\rightarrow 1.41 \times 10^6$ $\text{KY}\pi$ events in g11a
- Electroproduction:
 - Q^2 from ~ 0.5 to $\sim 3 (\text{GeV}/c)^2$
 - Structure functions from Rosenbluth and beam-helicity separations